

CSE211: Compiler Design

Oct. 20, 2020

- **Topic:** ASTs and 3 address code.
Local value numbering

- **Questions:**

*Questions/comments about
homework?*

*What are some compiler
optimizations you know about?*

Announcements

- Module 2 has been revamped
- Homeworks:
 - Homework 2 will be posted on Oct. 22
 - Homework 1 is due on Oct. 29
- Thanks to those who have posted!
- Come to the LSD seminar!

Module 2

- This week:
 - 3 address code
 - local value numbering
- Next week:
 - Flow analysis
- Third week:
 - SSA
 - Homework overview

CSE211: Compiler Design

Oct. 20, 2020

- **Topic:** ASTs and 3 address code.
Local value numbering

- **Questions:**

Questions/comments about homework?

What are some compiler optimizations you know about?

```
float hoist = z[const];  
for (...) {  
    x[i] = y[i] * hoist;  
}
```

3 address code IR

- Each instruction consists of 3 “addresses”
 - Address here means a virtual register or value
- represented many ways:

```
rx = ry op rz;
```

```
r5 = r3 + r6;
```

```
r6 = r0 * r7;
```

3 address code IR

- Each instruction consists of 3 “addresses”
 - Address here means a virtual register or value
- represented many ways:

$rx \leftarrow ry \ op \ rz;$

$r5 \leftarrow r3 \ + \ r6;$

$r6 \leftarrow r0 \ * \ r7;$

3 address code IR

- Each instruction consists of 3 “addresses”
 - Address here means a virtual register or value
- represented many ways:

```
rx = op ry, rz;
```

```
r5 = add r3, r6;
```

```
r6 = mult r0, r7;
```

3 address code IR

- Each instruction consists of 3 “addresses”
 - Address here means a virtual register or value
- some instructions don't fit the pattern:

```
store ry, rz;
```

```
r5 = copy r3;
```

```
r6 = call(r0, r1, r2, r3...);
```


3 address code IR

- Each instruction consists of 3 “addresses”
 - Address here means a virtual register or value
- Other information:
 - Annotated
 - Typed
 - Alignment

```
r5 = r3 + r6; !dbg !22  
r6 = r0 *(int32) 67;  
store(r1,r2), aligned 8
```

3 address code IR

- Each instruction consists of 3 “addresses”
 - Address here means a virtual register or value
- Control flow: branches and labels:

```
br r0, label1, label2;
```

```
br label1;
```

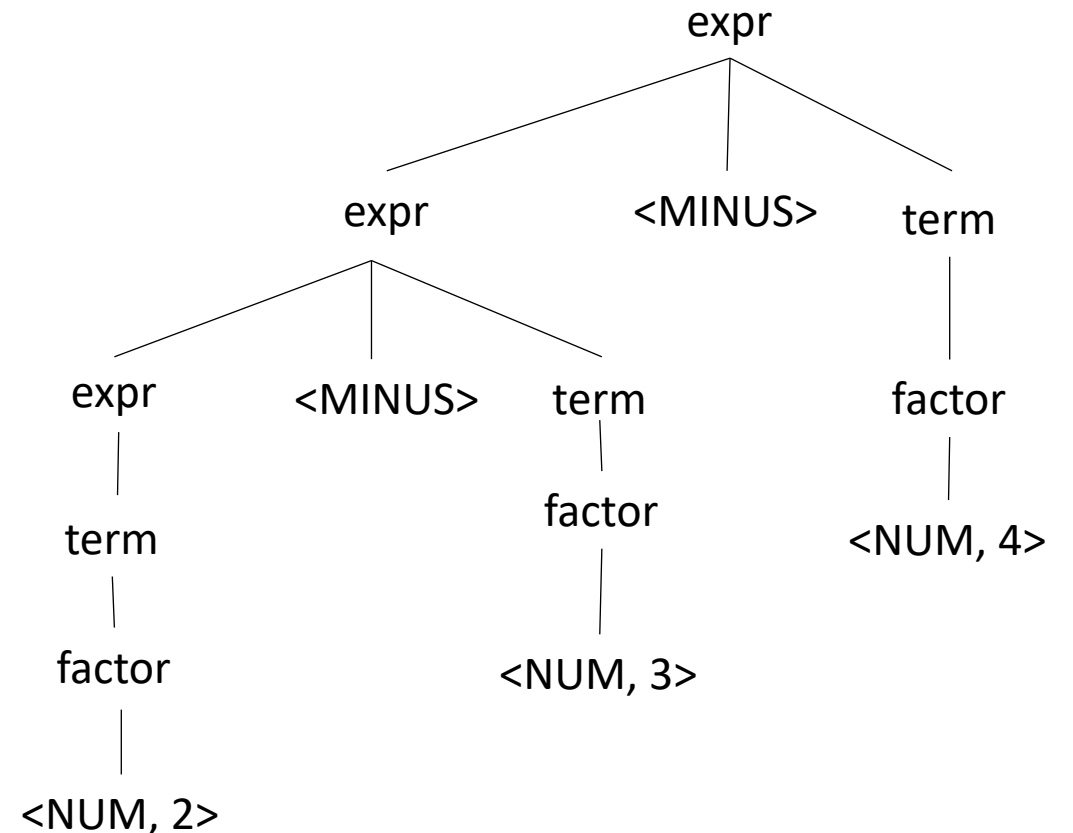
Creating 3 address code from AST

Abstract Syntax Trees

- Remember the expression parse tree

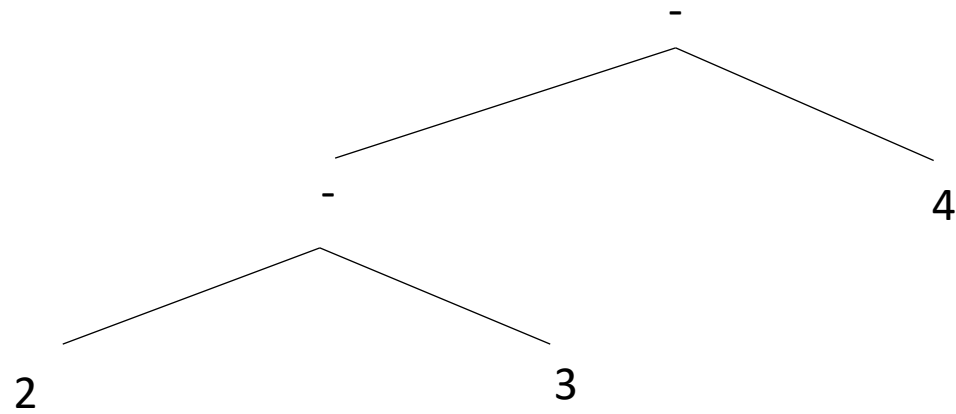
input: 2-3-4

Operator	Name	Productions
+,-	Expr	: Expr + Term Expr - Term Term
*,/	Term	: Term * Pow : Term / Pow Pow
^	Pow	: Factor ^ Pow Factor
()	Factor	: (Expr) NUM



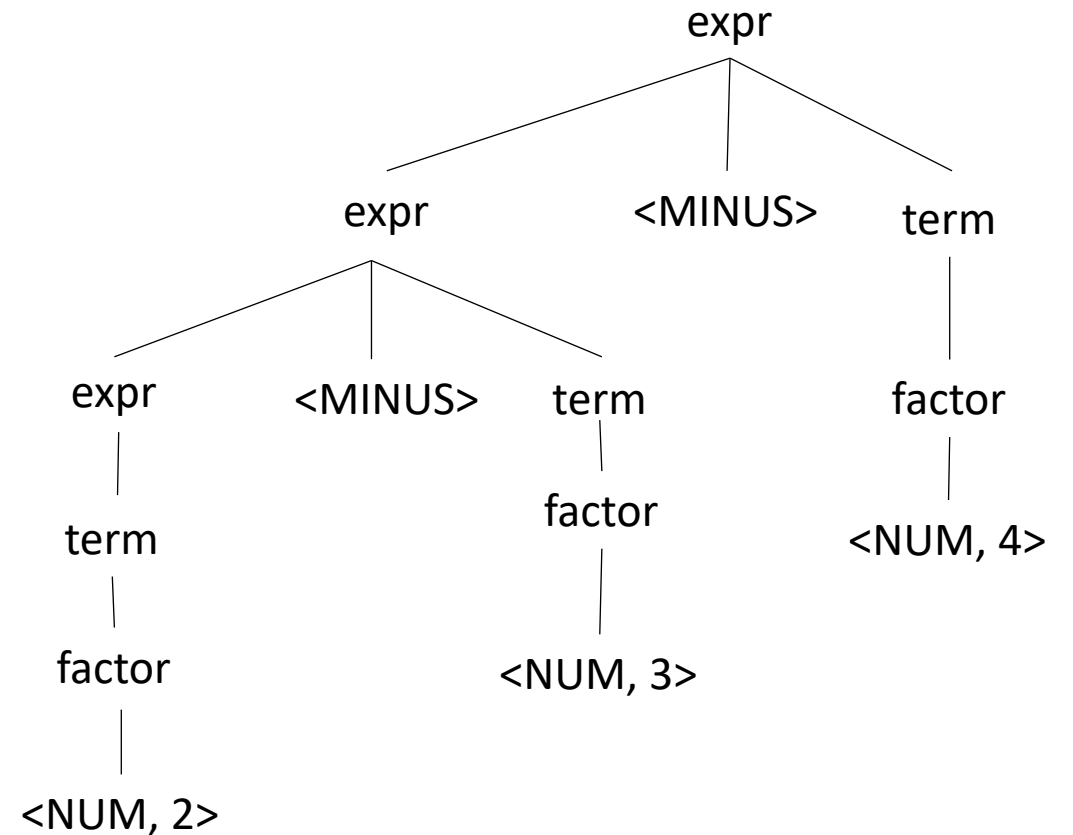
Abstract Syntax Trees

- Remember the expression parse tree



Much more compact!

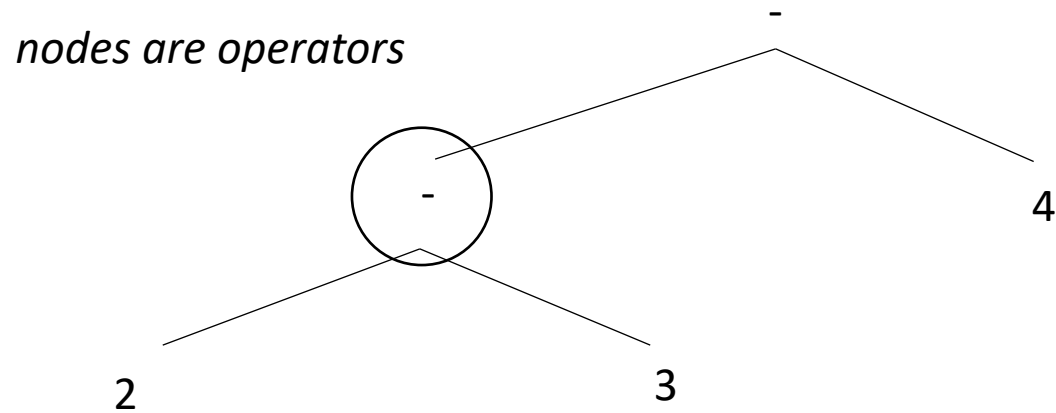
input: 2-3-4



Abstract Syntax Trees

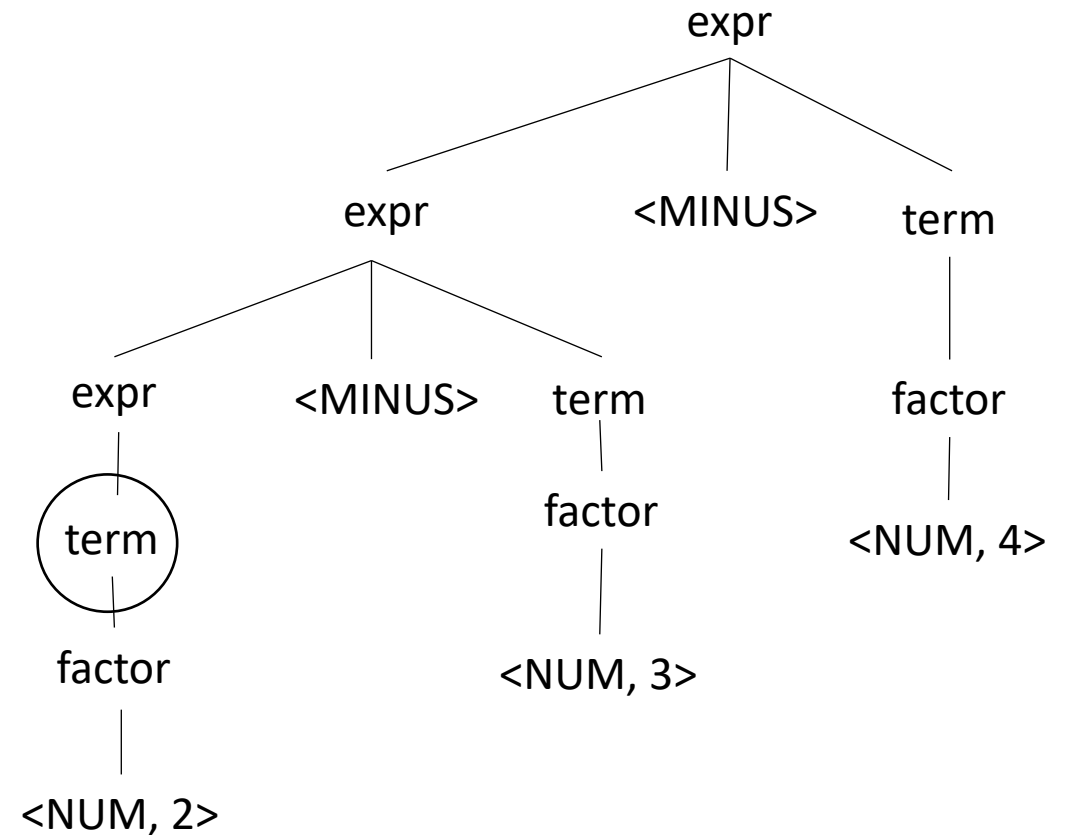
- Remember the expression parse tree

input: 2-3-4



Much more compact!

nodes are production rules



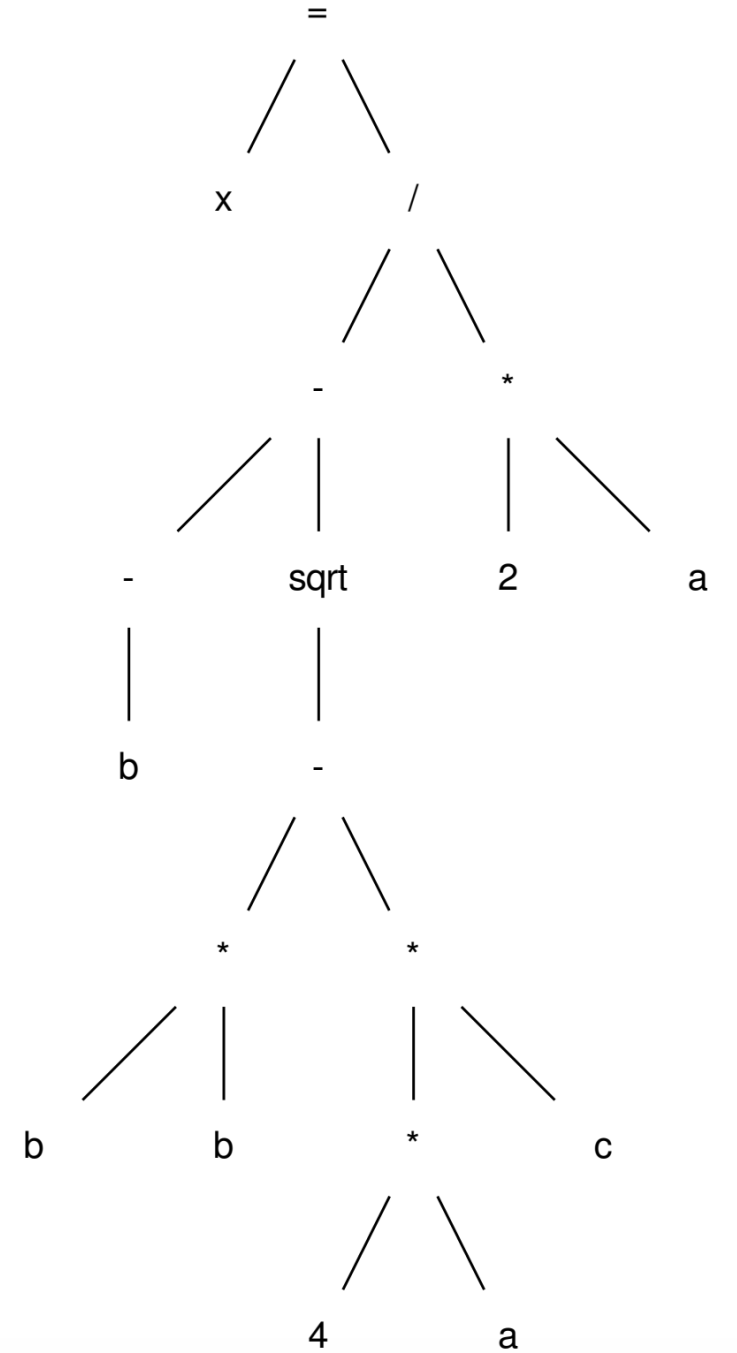
Abstract Syntax Trees

- Easier to see bigger trees, e.g. quadratic formula:

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

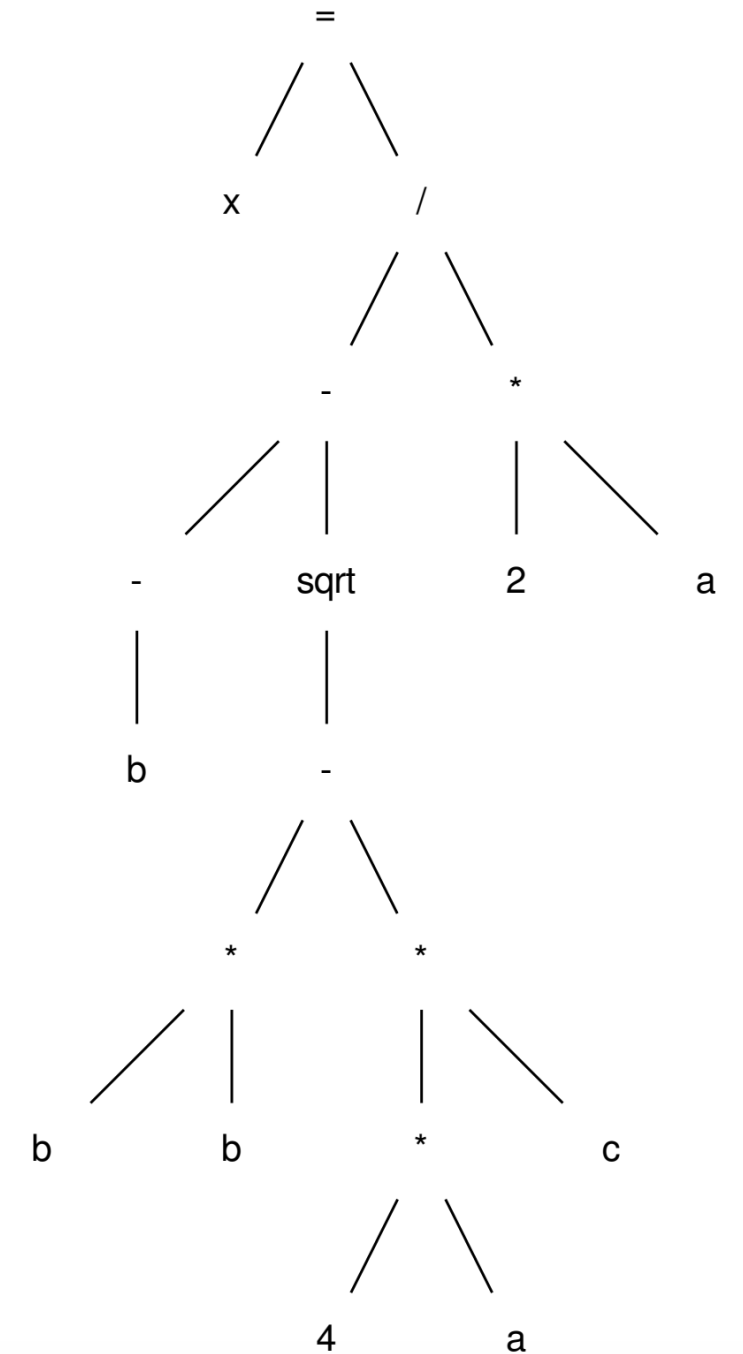
$$x = (-b - \text{sqrt}(b*b - 4 * a * c)) / (2*a)$$

$$x = (-b - \text{sqrt}(b*b - 4 * a * c)) / (2*a)$$



Convert this code to 3 address code

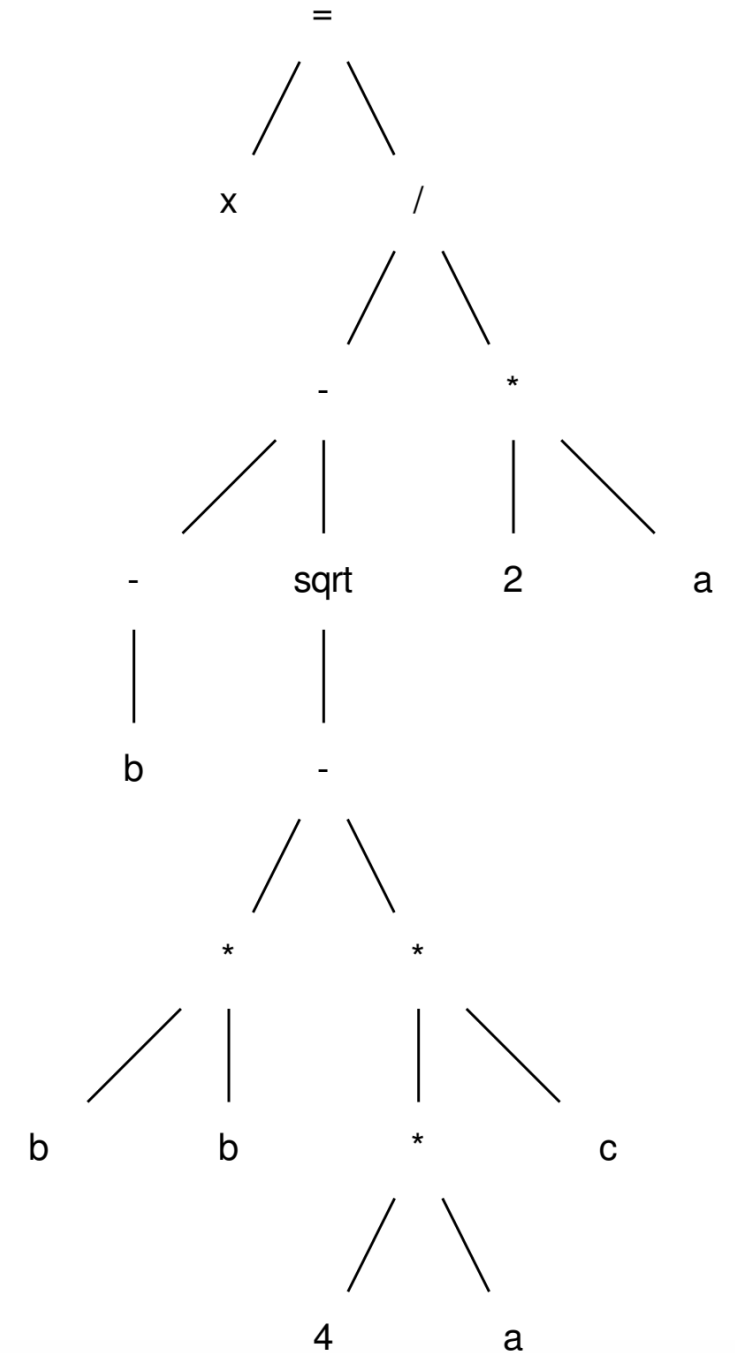
post-order traversal, creating virtual registers



Convert this code to 3 address code

post-order traversal, creating virtual registers

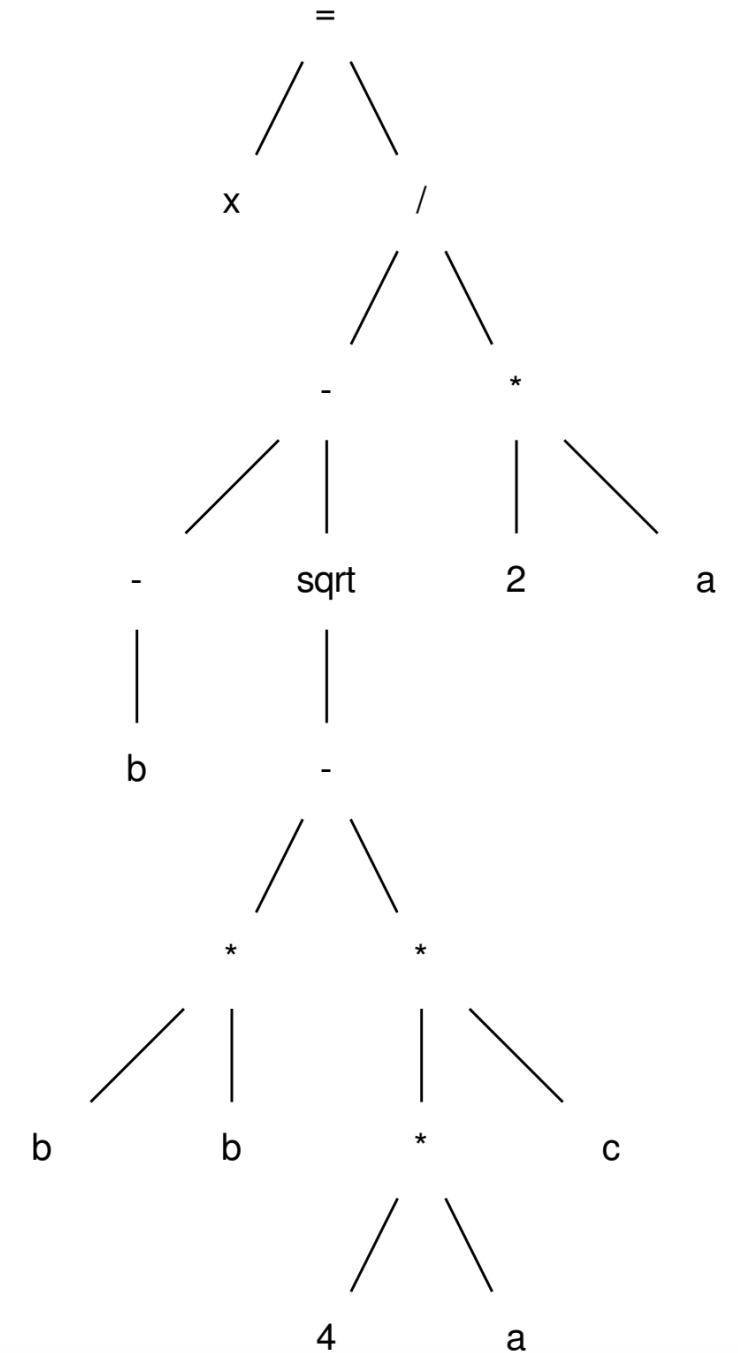
```
r0 = neg(b);
```



Convert this code to 3 address code

post-order traversal, creating virtual registers

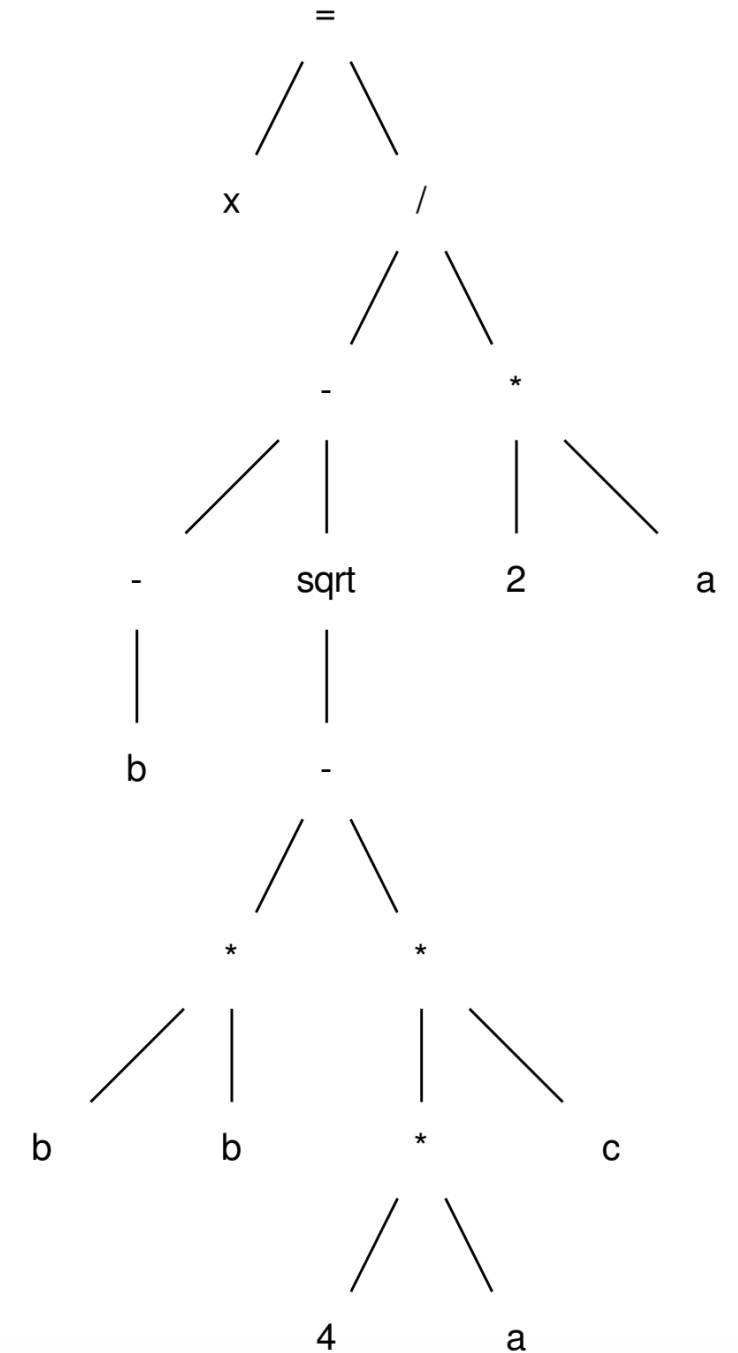
```
r0 = neg(b);  
r1 = b * b;
```



Convert this code to 3 address code

post-order traversal, creating virtual registers

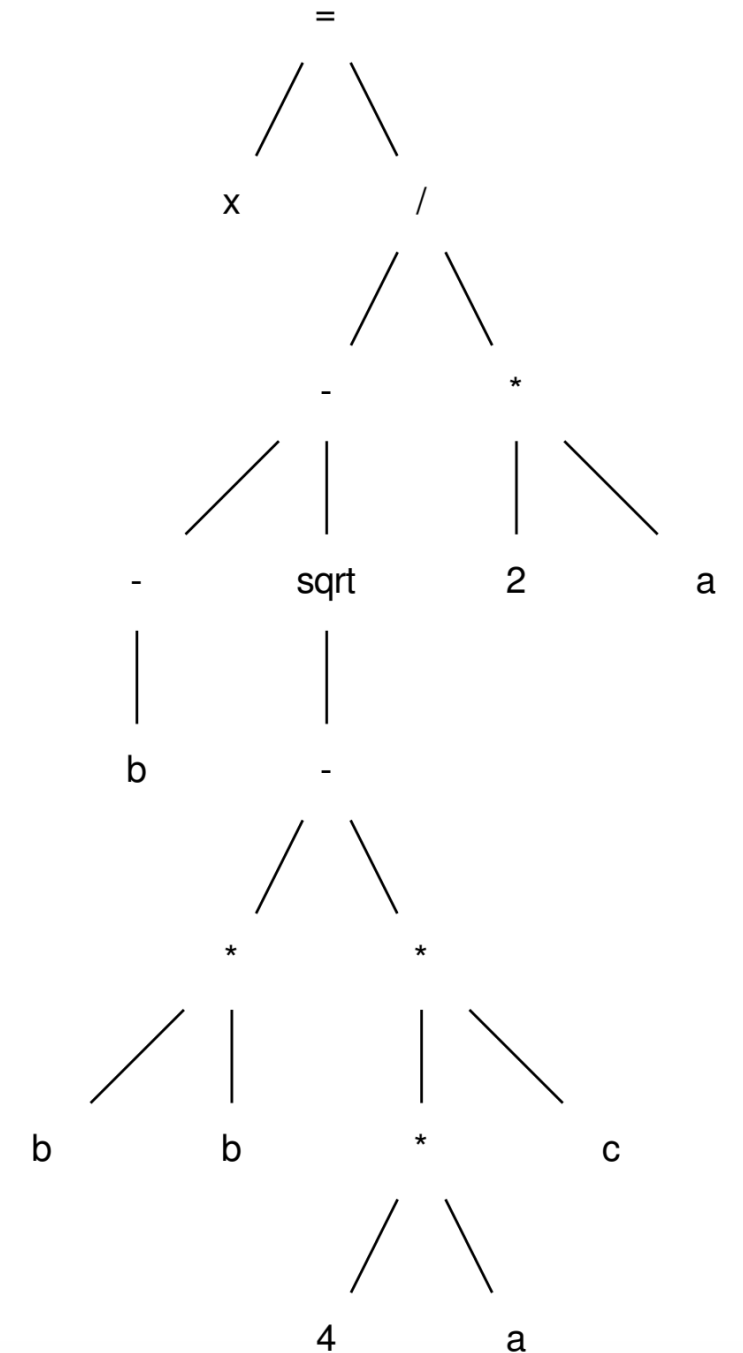
```
r0 = neg(b);  
r1 = b * b;  
r2 = 4 * a;
```



Convert this code to 3 address code

post-order traversal, creating virtual registers

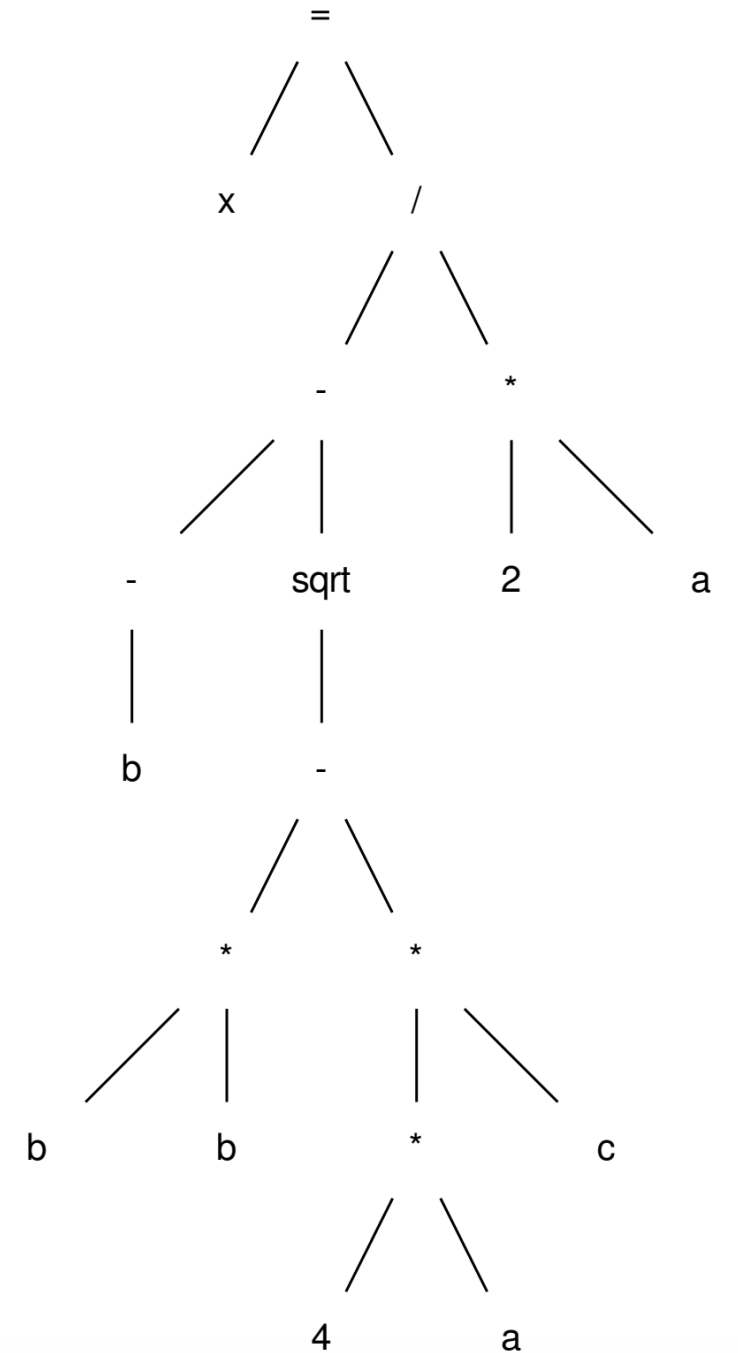
```
r0 = neg(b);  
r1 = b * b;  
r2 = 4 * a;  
r3 = r2 * c;
```



Convert this code to 3 address code

post-order traversal, creating virtual registers

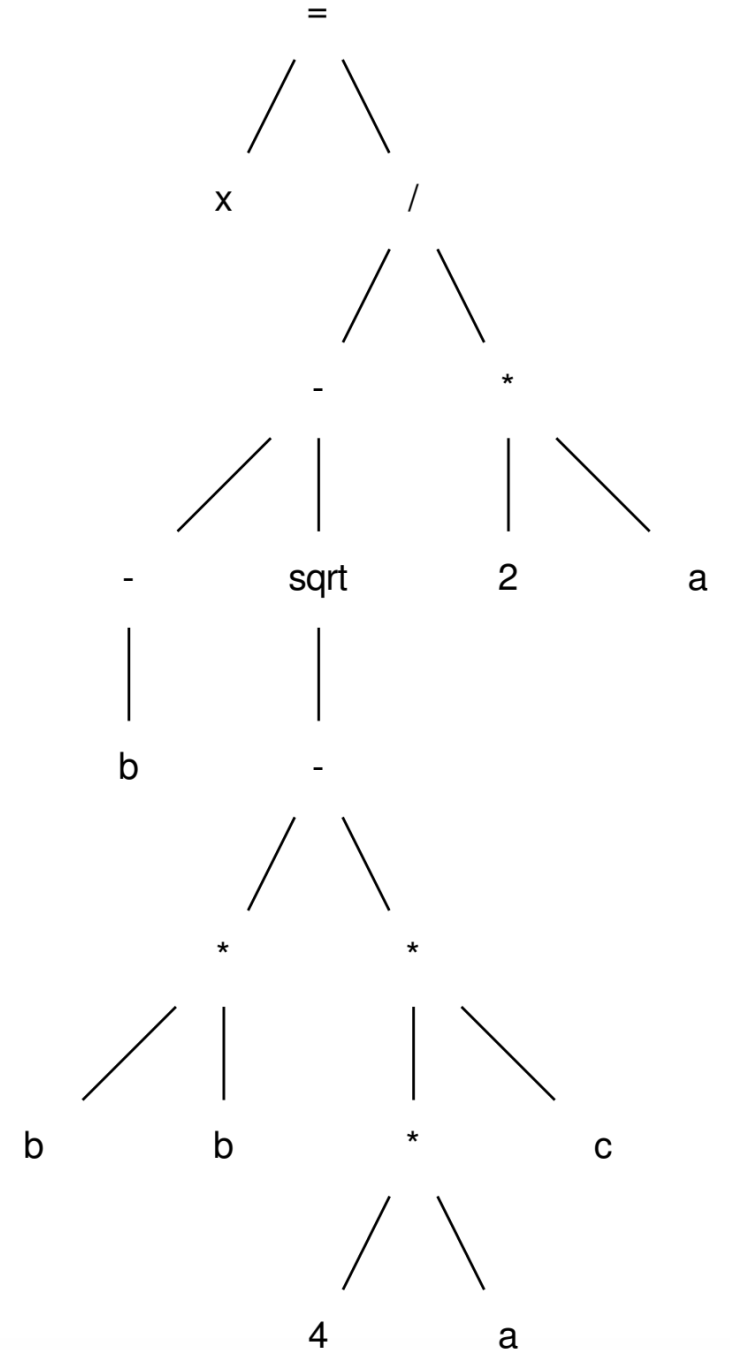
```
r0 = neg(b);  
r1 = b * b;  
r2 = 4 * a;  
r3 = r2 * c;  
r4 = r1 - r3;
```



Convert this code to 3 address code

post-order traversal, creating virtual registers

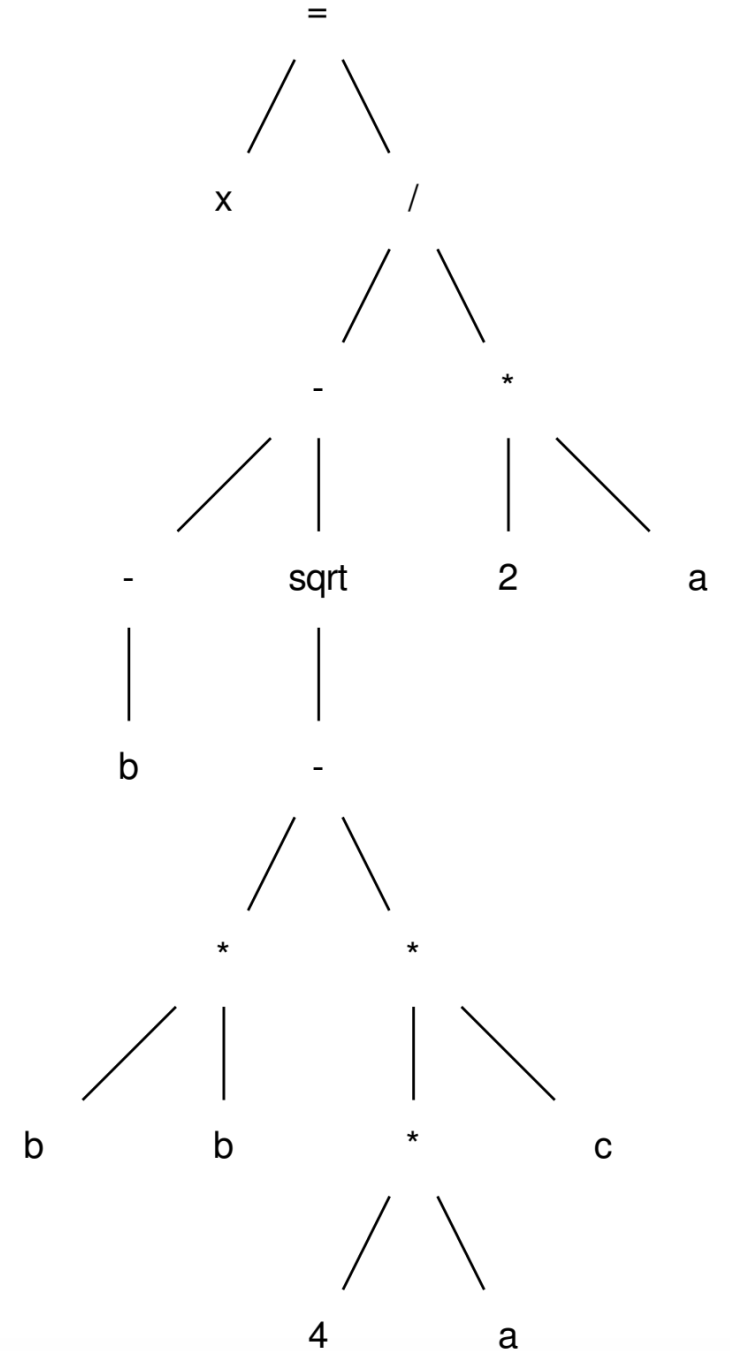
```
r0 = neg(b);  
r1 = b * b;  
r2 = 4 * a;  
r3 = r2 * c;  
r4 = r1 - r3;  
r5 = sqrt(r4);
```



Convert this code to 3 address code

post-order traversal, creating virtual registers

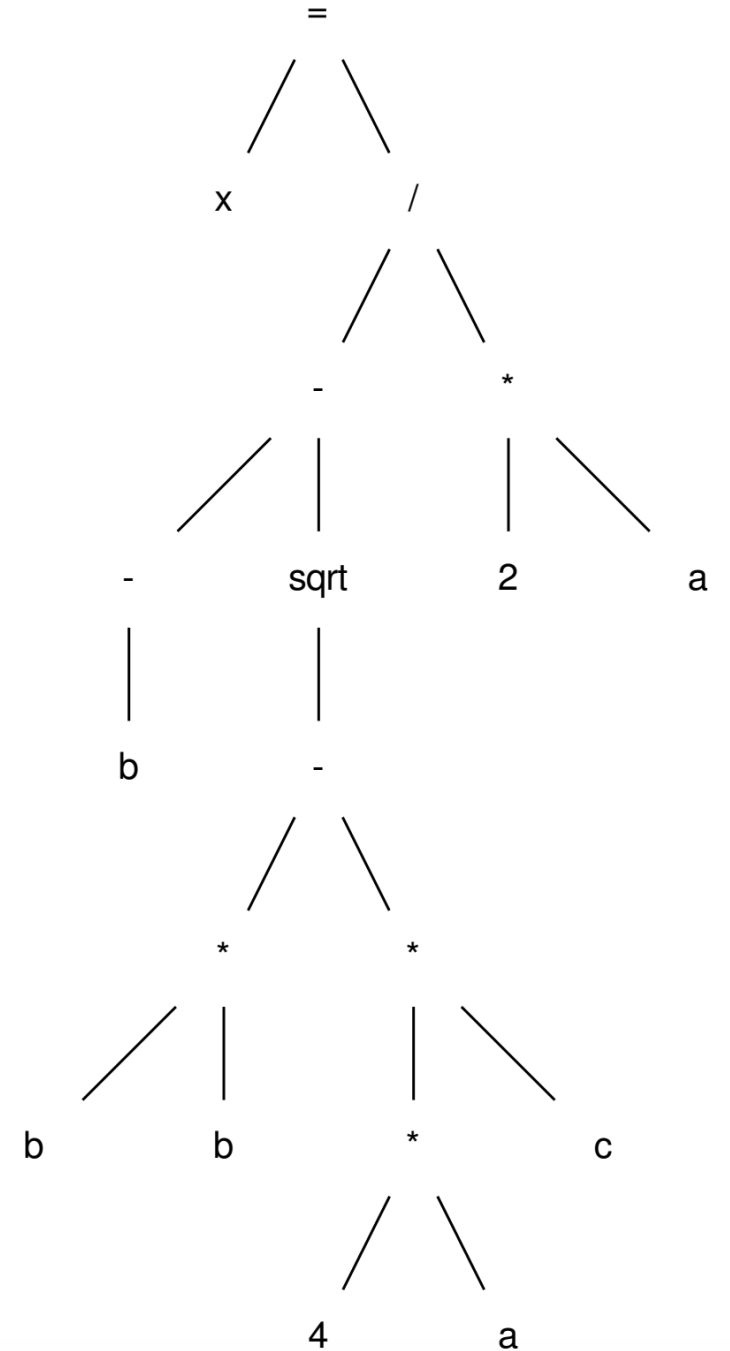
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r0 = neg(b);  
r1 = b * b;  
r2 = 4 * a;  
r3 = r2 * c;  
r4 = r1 - r3;  
r5 = sqrt(r4);  
r6 = r0 - r5;
```



Convert this code to 3 address code

post-order traversal, creating virtual registers

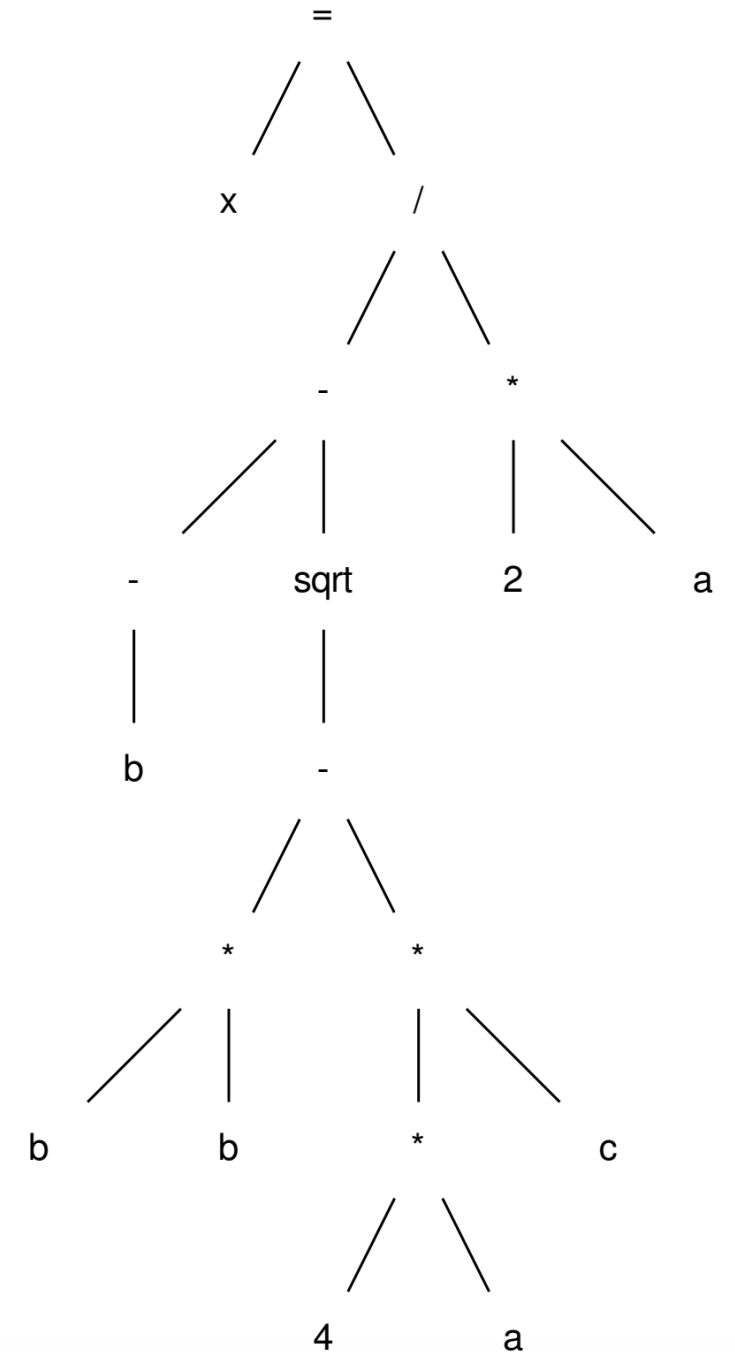
```
r0 = neg(b);  
r1 = b * b;  
r2 = 4 * a;  
r3 = r2 * c;  
r4 = r1 - r3;  
r5 = sqrt(r4);  
r6 = r0 - r5;  
r7 = 2 * a;
```



Convert this code to 3 address code

post-order traversal, creating virtual registers

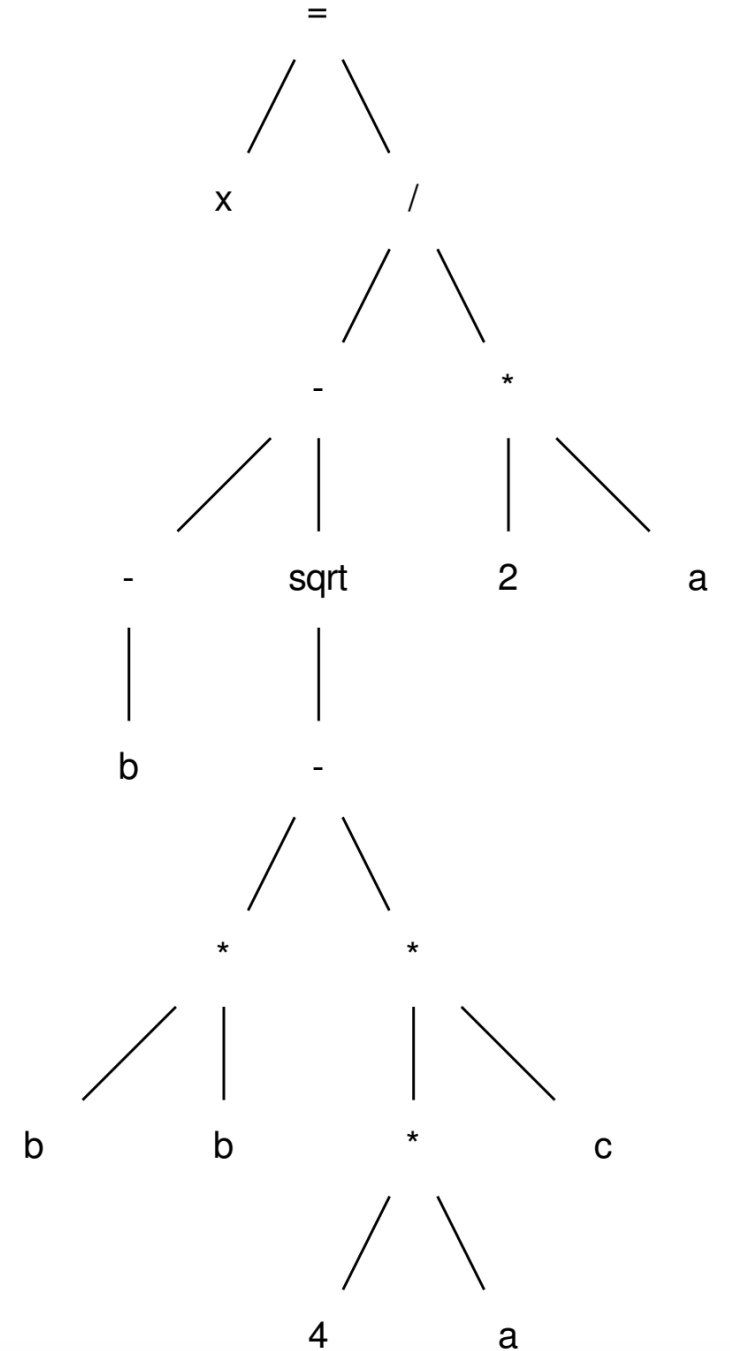
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r0 = neg(b);  
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r2 = 4 * a;  
r3 = r2 * c;  
r4 = r1 - r3;  
r5 = sqrt(r4);  
r6 = r0 - r5;  
r7 = 2 * a;  
r8 = r6 / r7;
```



Convert this code to 3 address code

post-order traversal, creating virtual registers

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r0 = neg(b);  
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r2 = 4 * a;  
r3 = r2 * c;  
r4 = r1 - r3;  
r5 = sqrt(r4);  
r6 = r0 - r5;  
r7 = 2 * a;  
r8 = r6 / r7;  
x = r8;
```

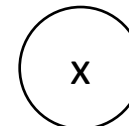


3 address code use-case

What now?

We can make a data-dependency graph (DDG)

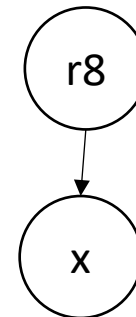
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r0 = neg(b);  
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```



What now?

We can make a data-dependency graph (DDG)

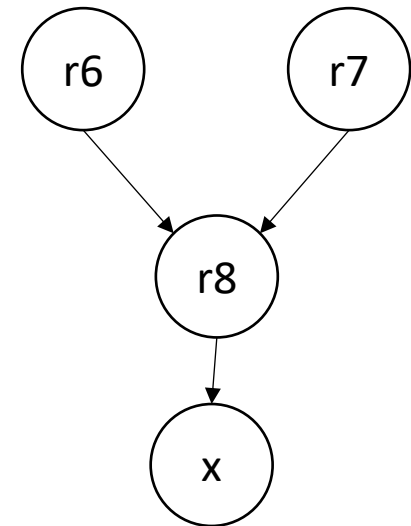
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x = r8;
```



What now?

We can make a data-dependency graph (DDG)

```
r0 = neg(b);
```

```
r1 = b * b;
```

```
r2 = 4 * a;
```

```
r3 = r2 * c;
```

```
r4 = r1 - r3;
```

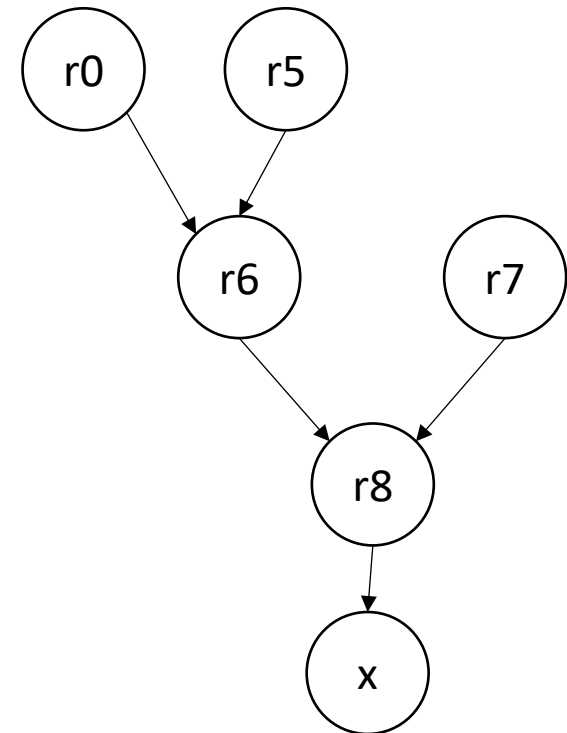
```
r5 = sqrt(r4);
```

```
r6 = r0 - r5;
```

```
r7 = 2 * a;
```

```
r8 = r6 / r7;
```

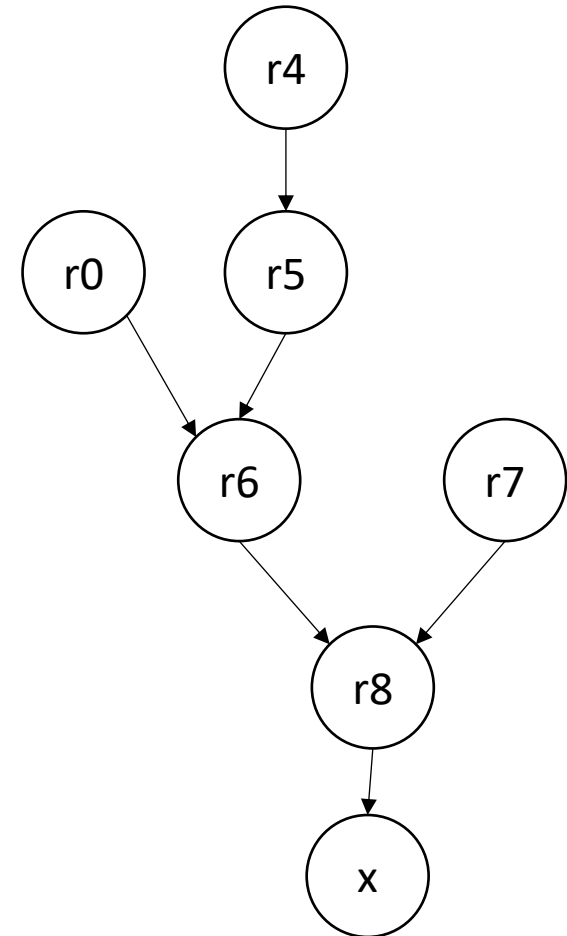
```
x = r8;
```



What now?

We can make a data-dependency graph (DDG)

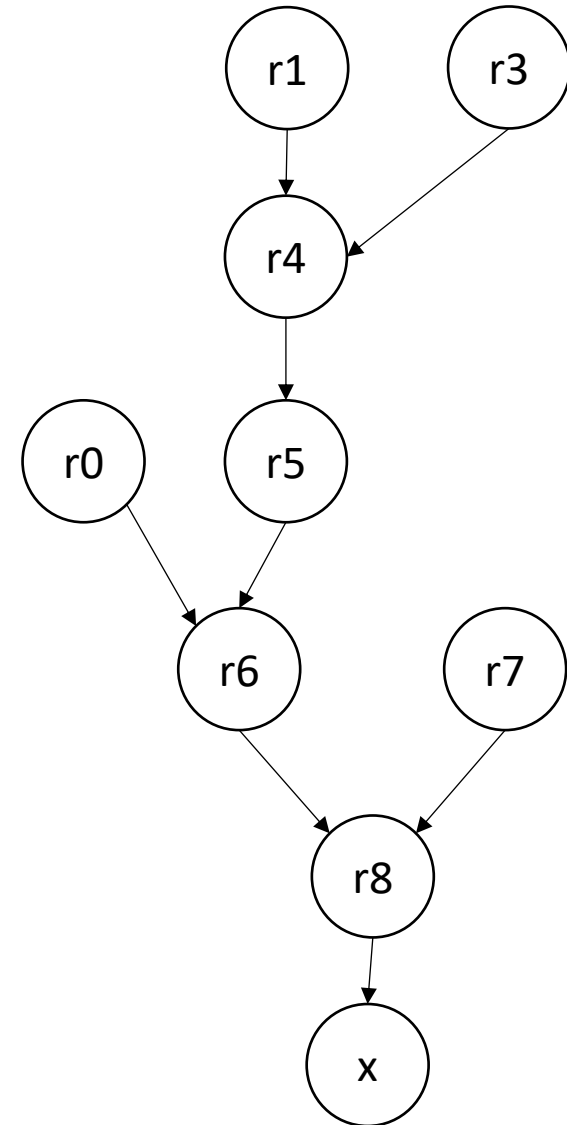
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r3 = r2 * c;  
r4 = r1 - r3;  
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r7 = 2 * a;  
r8 = r6 / r7;  
x = r8;
```



What now?

We can make a data-dependency graph (DDG)

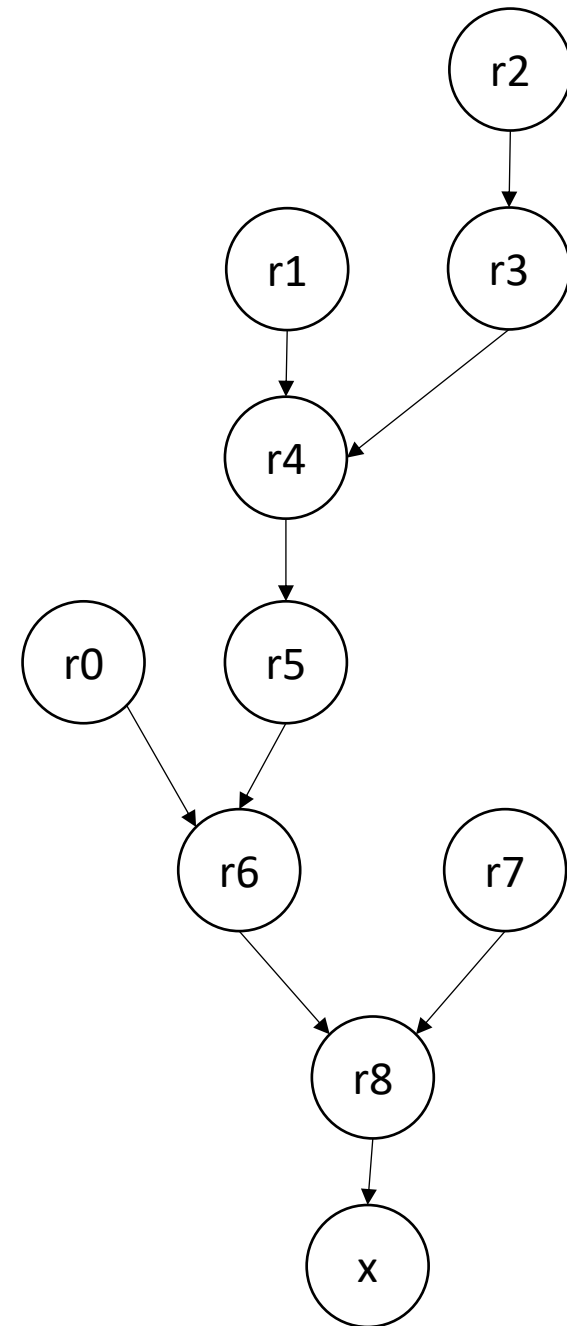
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x = r8;
```



What now?

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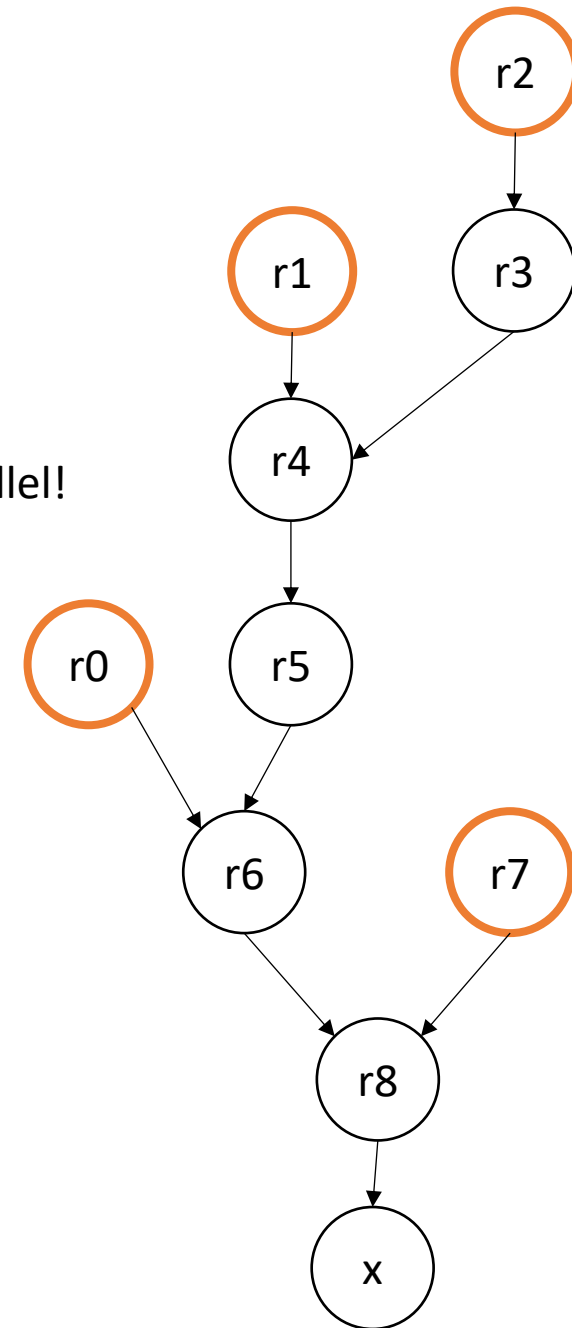


What now?

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r5 = sqrt(r4);  
r6 = r0 - r5;  
r7 = 2 * a;  
r8 = r6 / r7;  
x = r8;
```

can be done in parallel!



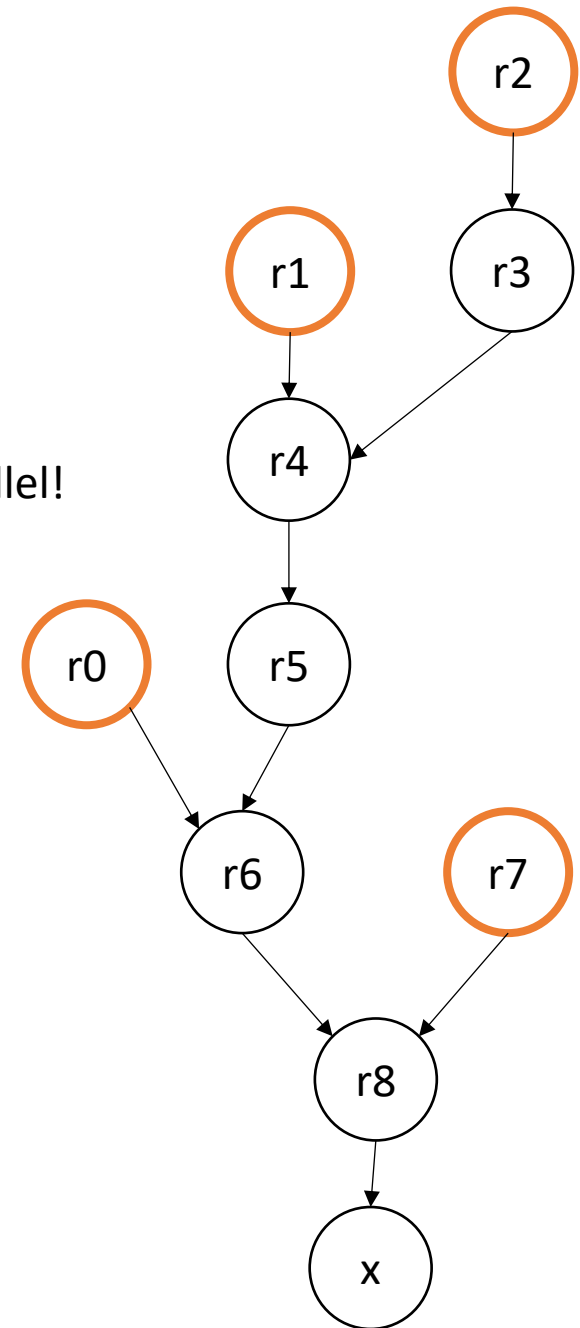
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r1 = b * b;  
r2 = 4 * a;  
r3 = r2 * c;  
r4 = r1 - r3;  
r5 = sqrt(r4);  
r6 = r0 - r5;  
r7 = 2 * a;  
r8 = r6 / r7;  
x = r8;
```

Can be hoisted!

can be done in parallel!



What now?

We can make a data-dependency graph (DDG)

```
r0 = neg(b);
```

```
r1 = b * b;
```

```
r2 = 4 * a;
```

```
r3 = r2 * c;
```

```
r4 = r1 - r3;
```

```
r5 = sqrt(r4);
```

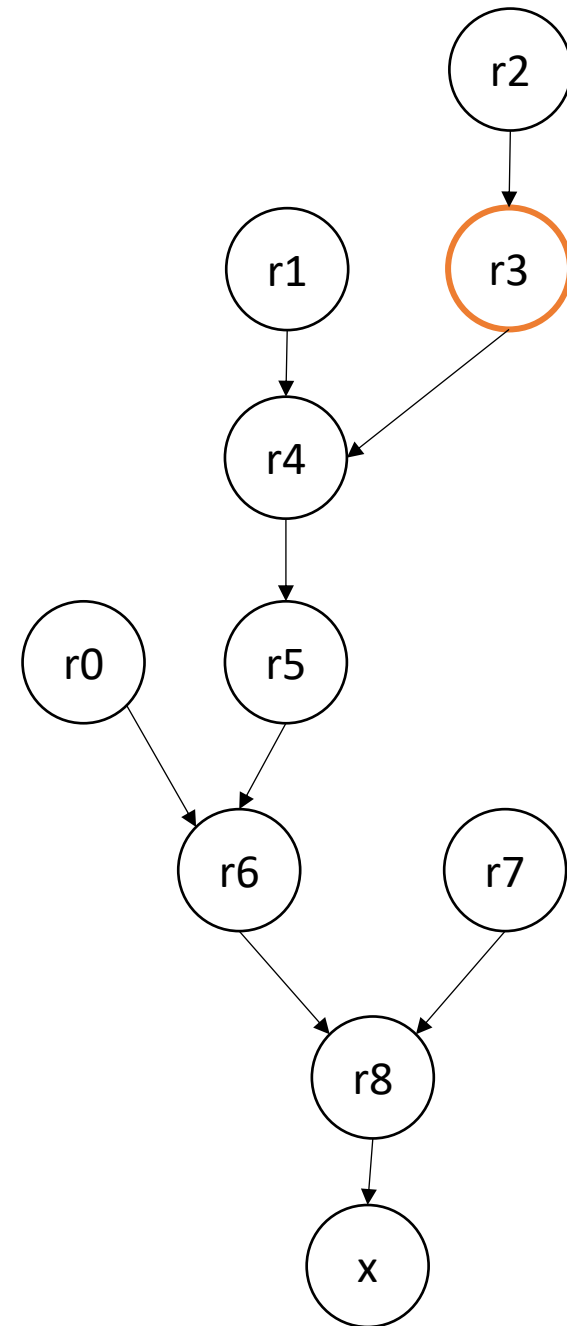
```
r6 = r0 - r5;
```

```
r7 = 2 * a;
```

```
r8 = r6 / r7;
```

```
x = r8;
```

should we hoist this one?



back to 3 address code

```
x = expr0;
```

```
y = expr1;
```

```
z = expr2;
```

- Convert each expression to an AST.
- Convert each AST to 3 address code.
- Sequence each expression.

What about control flow?

- 3 address code typically contains a conditional branch:

```
br <reg>, <label0>, <label1>
```

if the value in <reg> is true, branch to <label0>, else branch to label1

```
br <label0>
```

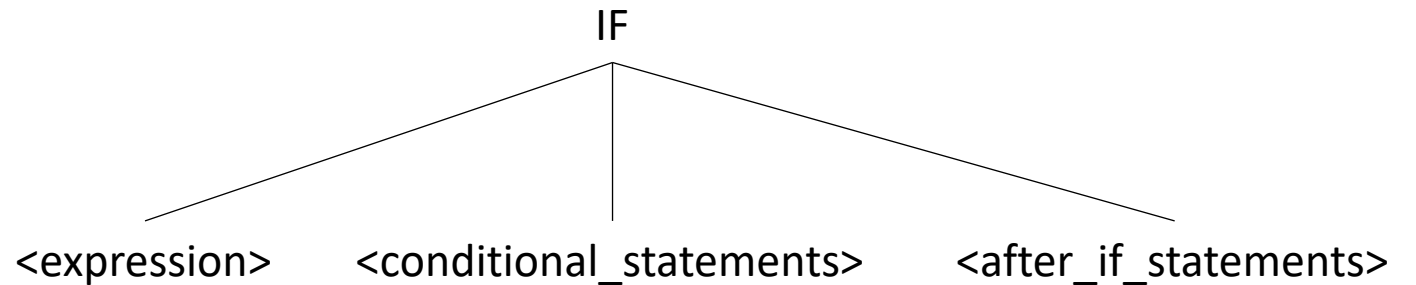
unconditional branch

What about control flow?

```
r0 = <expression>;  
br r0, inside_if, after_if;
```

```
inside_if:  
<conditional_statements>;
```

```
after_if:  
<after_if_statements>;
```



What about control flow?

beginning_label:

r0 = <expression>

br r0, inside_loop, after_loop;

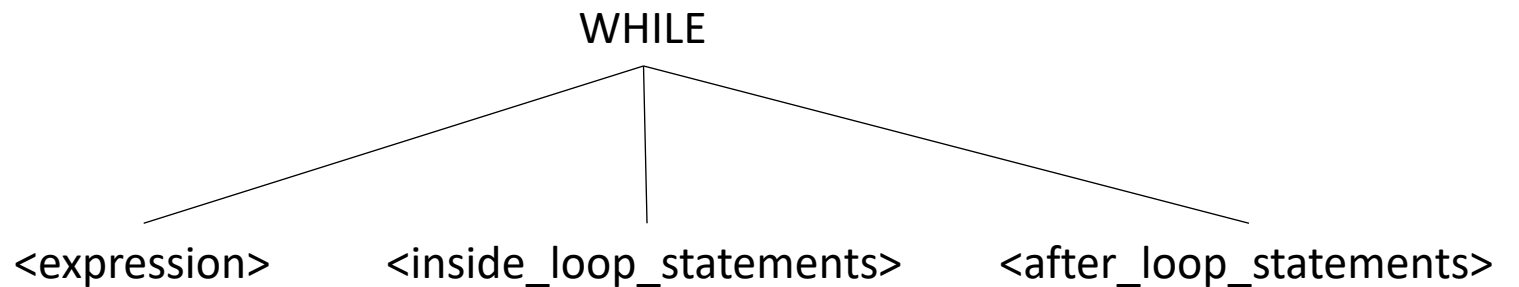
inside_loop:

<inside_loop_statements>

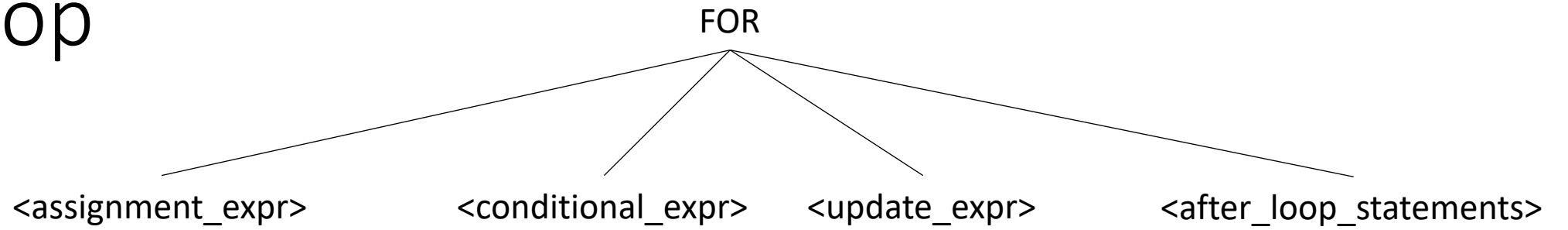
br beginning_label;

after_loop:

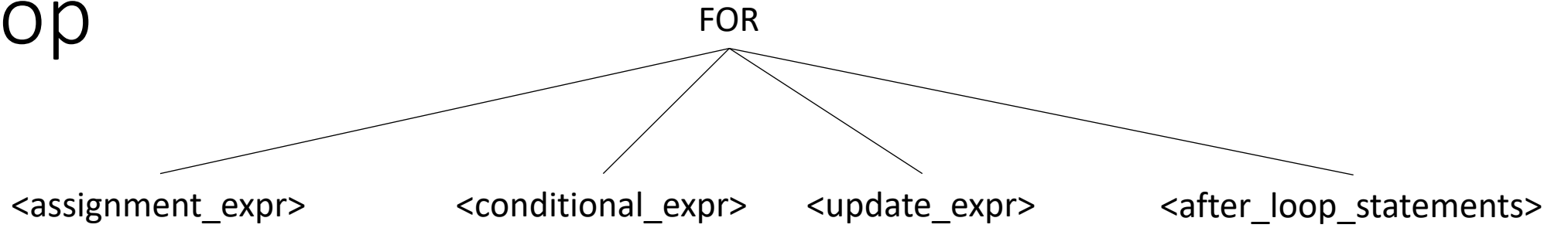
<after_loop_statements>



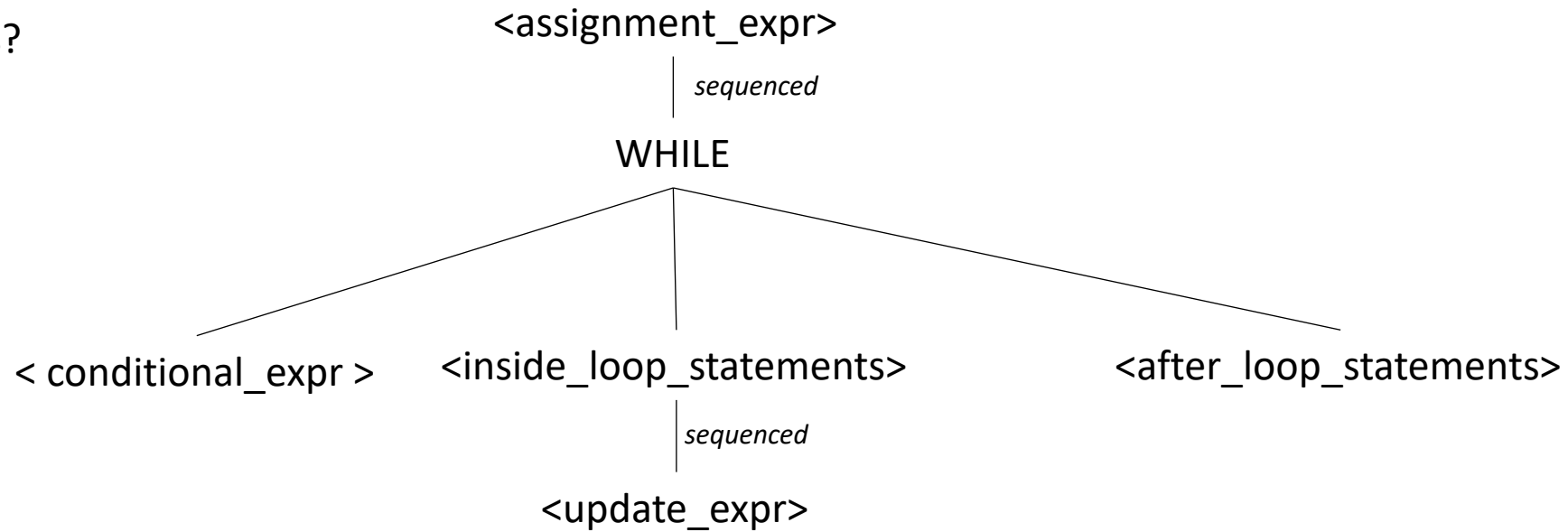
For loop



For loop



Pros and cons?



IR Program structure

- A sequence of 3 address instructions
- Programs can be split into Basic Blocks:
 - A sequence of 3 address instructions such that:
 - There is a single entry, single exit
- Important property: an instruction in a basic block can assume that all preceding instructions will execute

IR Program structure

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Single Basic Block

```
Label_x:  
op1;  
op2;  
op3;  
br label_z;
```

IR Program structure

- A sequence of 3 address instructions
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Single Basic Block

```
Label_x:  
op1;  
op2;  
op3;  
br label_z;
```

Two Basic Blocks

```
Label_x:  
op1;  
op2;  
op3;  
  
Label_y:  
op4;  
op5;
```

How might they appear in a high-level language?

IR Program structure

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IR Program structure

- A sequence of 3 address instructions
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 - There is a single entry, single exit
- Important property: an instruction in a basic block can assume that all preceding instructions will execute

How might they appear in a high-level language?

Four Basic Blocks

```
...  
if (x) {  
    ...  
}  
else {  
    ...  
}  
...
```

Two Basic Blocks

Single Basic Block

```
Label_x:  
op1;  
op2;  
op3;  
br label_z;
```

```
Label_x:  
op1;  
op2;  
op3;  
  
Label_y:  
op4;  
op5;
```

Optimization levels

- Local optimizations:
 - Optimizes an individual basic block
- Regional optimizations:
 - Combines several basic blocks
- Global optimizations:
 - operates across an entire procedure
 - what about across procedures?

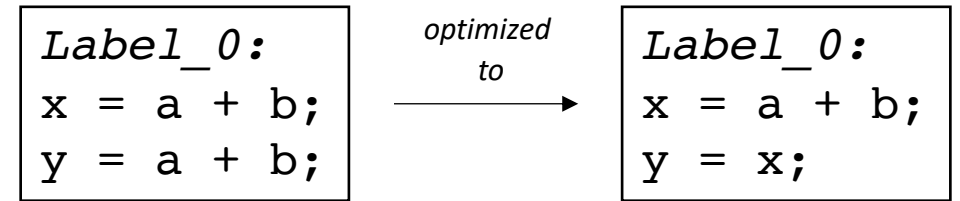
Optimization levels

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```
Label_0:  
x = a + b;  
y = a + b;
```

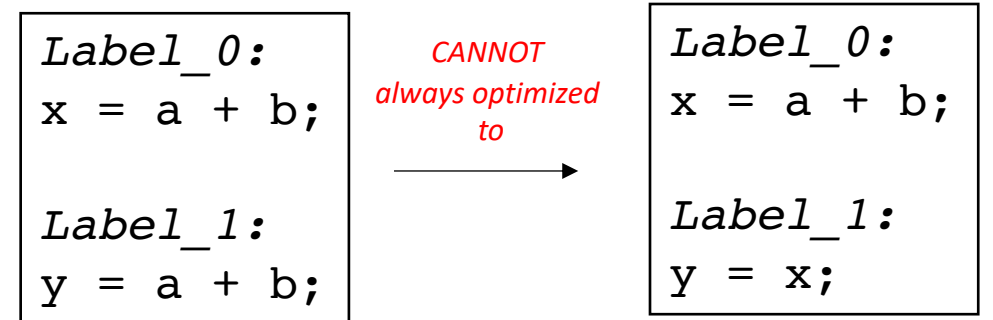
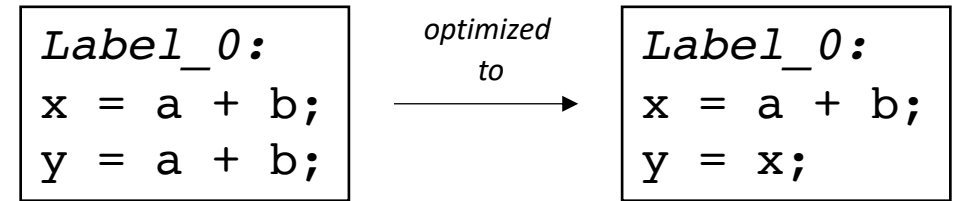
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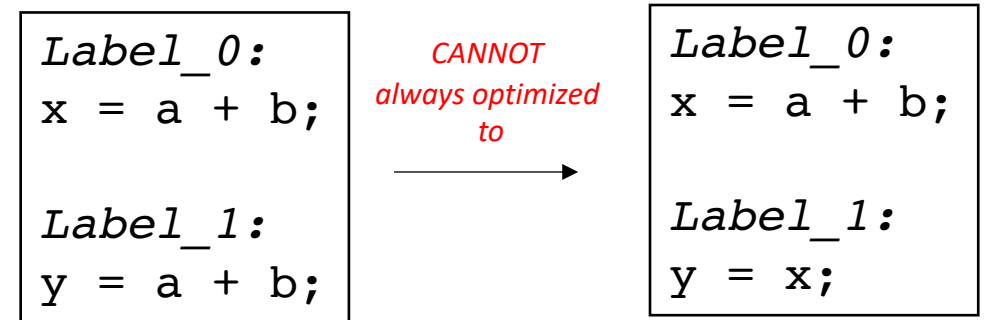
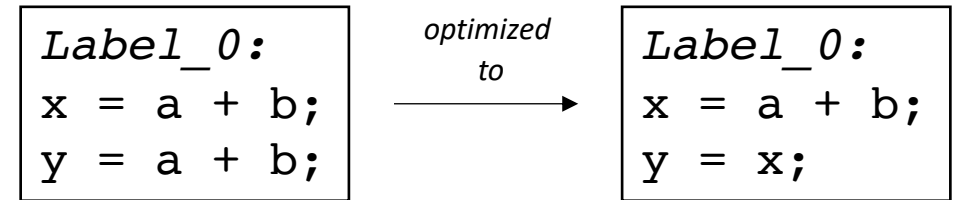
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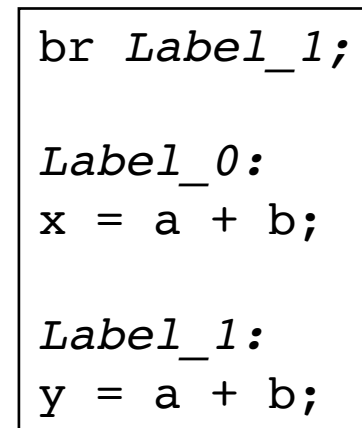


Optimization levels

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 - Optimizes an individual basic block
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 - Combines several basic blocks
- Global optimizations:
 - operates across an entire procedure
 - what about across procedures?



*code could skip Label_0,
leaving x undefined!*



Optimization levels

```
...  
if (x) {  
    ...  
}  
else {  
    x = a + b;  
}  
y = a + b;  
...
```

*at a higher-level,
we cannot replace:
y = a + b.
with
y = x;*

```
x = a + b;  
if (x) {  
    ...  
}  
else {  
    ...  
}  
y = a + b;  
...
```

*But if a and b are
not redefined, then
y = a + b;
can be replaced with
y = x;*

```
Label_0:  
x = a + b;  
y = a + b;
```

*optimized
to*

```
Label_0:  
x = a + b;  
y = x;
```

```
Label_0:  
x = a + b;  
  
Label_1:  
y = a + b;
```

*CANNOT
always optimized
to*

```
Label_0:  
x = a + b;  
  
Label_1:  
y = x;
```

code could skip Label_0

```
br Label_1;  
  
Label_0:  
x = a + b;  
  
Label_1:  
y = a + b;
```

Moving on to a concrete optimization algorithm

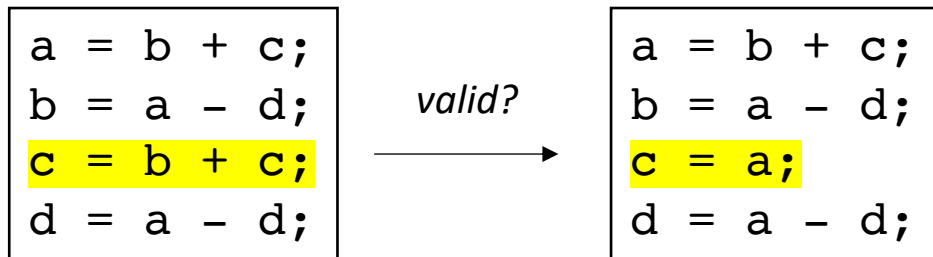
Local Value Numbering

- Local optimization
 - can be extended with the help of flow analysis
- Aims to remove redundant arithmetic instructions

```
a = b + c;  
b = a - d;  
c = b + c;  
d = a - d;
```

Local Value Numbering

- Local optimization
 - can be extended with the help of flow analysis
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Local Value Numbering

- Local optimization
 - can be extended with the help of flow analysis
- Aims to remove redundant arithmetic instructions

```
a = b + c;  
b = a - d;  
c = b + c;  
d = a - d;
```

valid?

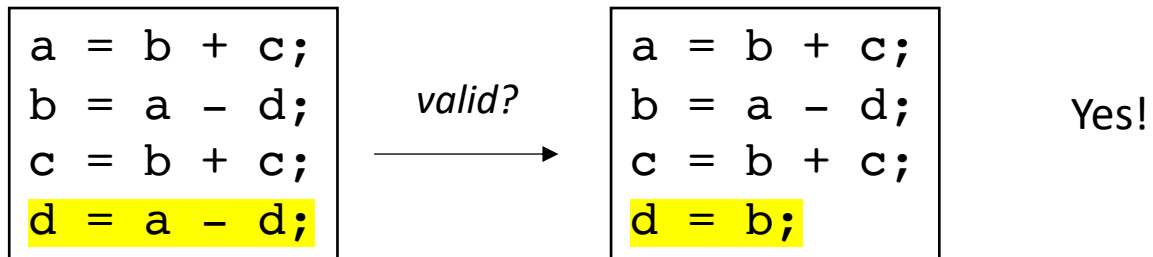


```
a = b + c;  
b = a - d;  
c = a;  
d = a - d;
```

No! Because b is redefined

Local Value Numbering

- Local optimization
 - can be extended with the help of flow analysis
- Aims to remove redundant arithmetic instructions



Local Value Numbering

- Algorithm:
- Provide a number to each variable. Update the number each time the variable is updated.
- Several different implementations. I keep a global counter; increment with new variables or assignments

```
a2 = b0 + c1;  
b4 = a2 - d3;  
c5 = b4 + c1;  
d6 = a2 - d3;
```

Global_counter = 7

Local Value Numbering

- Algorithm:
- Provide a number to each variable. Update the number each time the variable is updated.
- Several different implementations. I keep a global counter; increment with new variables or assignments

```
a2 = b0 + c1;  
b4 = a2 - d3;  
c5 = b4 + c1;  
d6 = a2 - d3;
```

Local Value Numbering

- Algorithm: Now that variables are numbered
- Iterate sequentially through instructions. Keep a hash table of the rhs (numbered variables and operation) mapped to their lhs.
- At each step, check to see if the rhs has already been computed.

```
a2 = b0 + c1;  
b4 = a2 - d3;  
c5 = b4 + c1;  
d6 = a2 - d3;
```

Local Value Numbering

- Algorithm: Now that variables are numbered
- Iterate sequentially through instructions. Keep a hash table of the rhs (numbered variables and operation) mapped to their lhs.
- At each step, check to see if the rhs has already been computed.

→

a2	=	b0	+	c1;
b4	=	a2	-	d3;
c5	=	b4	+	c1;
d6	=	a2	-	d3;

H = {
}

Local Value Numbering

- Algorithm: Now that variables are numbered
- Iterate sequentially through instructions. Keep a hash table of the rhs (numbered variables and operation) mapped to their lhs.
- At each step, check to see if the rhs has already been computed.

→

a2	=	b0	+	c1;
b4	=	a2	-	d3;
c5	=	b4	+	c1;
d6	=	a2	-	d3;

H = {
 "b0 + c1" : a2,
}

Local Value Numbering

- Algorithm: Now that variables are numbered
- Iterate sequentially through instructions. Keep a hash table of the rhs (numbered variables and operation) mapped to their lhs.
- At each step, check to see if the rhs has already been computed.

→

a2 = b0 + c1;
b4 = a2 - d3;
c5 = b4 + c1;
d6 = a2 - d3;

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→

a2 = b0 + c1;
b4 = a2 - d3;
c5 = b4 + c1;
d6 = a2 - d3;

H = {
 "b0 + c1" : "a2",
 "a2 - d3" : "b4",
}

Local Value Numbering

- Algorithm: Now that variables are numbered
- Iterate sequentially through instructions. Keep a hash table of the rhs (numbered variables and operation) mapped to their lhs.
- At each step, check to see if the rhs has already been computed.

→

a2 = b0 + c1;
b4 = a2 - d3;
c5 = b4 + c1;
d6 = a2 - d3;

H = {
 "b0 + c1" : "a2",
 "a2 - d3" : "b4",
}

Local Value Numbering

- Algorithm: Now that variables are numbered
- Iterate sequentially through instructions. Keep a hash table of the rhs (numbered variables and operation) mapped to their lhs.
- At each step, check to see if the rhs has already been computed.

→

a2 = b0 + c1;
b4 = a2 - d3;
c5 = b4 + c1;
d6 = a2 - d3;

H = {
"b0 + c1" : "a2",
"a2 - d3" : "b4",
}

*mismatch due to
numberings!*

Local Value Numbering

- Algorithm: Now that variables are numbered
- Iterate sequentially through instructions. Keep a hash table of the rhs (numbered variables and operation) mapped to their lhs.
- At each step, check to see if the rhs has already been computed.

→

a2 = b0 + c1;
b4 = a2 - d3;
c5 = b4 + c1;
d6 = a2 - d3;

H = {
 "b0 + c1" : "a2",
 "a2 - d3" : "b4",
 "b4 + c1" : "c5",
}

Local Value Numbering

- Algorithm: Now that variables are numbered
- Iterate sequentially through instructions. Keep a hash table of the rhs (numbered variables and operation) mapped to their lhs.
- At each step, check to see if the rhs has already been computed.

→

a2 = b0 + c1;
b4 = a2 - d3;
c5 = b4 + c1;
d6 = a2 - d3;

H = {
 "b0 + c1" : "a2",
 "a2 - d3" : "b4",
 "b4 + c1" : "c5",
}

Local Value Numbering

- Algorithm: Now that variables are numbered
- Iterate sequentially through instructions. Keep a hash table of the rhs (numbered variables and operation) mapped to their lhs.
- At each step, check to see if the rhs has already been computed.

→

a2 = b0 + c1;
b4 = a2 - d3;
c5 = b4 + c1;
d6 = b4;

H = {
 "b0 + c1" : "a2",
 "a2 - d3" : "b4",
 "b4 + c1" : "c5",
}

match!

Next week

- Local value numbering continued:
 - commutative operations
 - register usage
- Introduction to flow analysis:
 - How to create extended basic blocks for local analysis