$\qquad$
$\qquad$ 1

1. Tree Traversal: (40 points:)

(a) (10 points:) Given the image above, what is the level-order traversal of the tree?

$$
50 \Rightarrow 30 \Rightarrow 75 \Rightarrow 20 \Rightarrow 40 \Rightarrow 20 \Rightarrow 90 \Rightarrow 25 \Rightarrow 55 \text { => } 95 \text { => } 100
$$

(b) (10 points:) Given the image above, what is the pre-order traversal of the tree?

$$
50 \Rightarrow 30 \Rightarrow 20 \Rightarrow 25 \Rightarrow 40 \Rightarrow 75 \text { => } 60 \Rightarrow 55 \text { => } 90 \Rightarrow 95 \text { A> } 100
$$

(c) (10 points:) Given the image above, what is the in-order traversal of the tree?

$$
20 \Rightarrow 25 \Rightarrow>30 \Rightarrow 40 \Rightarrow 50 \Rightarrow 55 \Rightarrow>60 \Rightarrow 75 \Rightarrow>95 \Rightarrow>100 \Rightarrow>90
$$

(d) (10 points:) Given the image above, what is the post-order traversal of the tree?

$$
25 \Rightarrow>20 \Rightarrow>40 \Rightarrow>30 \Rightarrow 55 \Rightarrow>60 \Rightarrow 100 \Rightarrow 95 \Rightarrow 90 \Rightarrow 75 \text { => } 50
$$

$\qquad$
$\qquad$ 2
2. Binary Search Tree: (40 points:)


In all the questions below, nodes will be referred to by its key field. So, the root is referred to as node 50 .
(a) (10 points:)

Yes/No: Does the tree above have the properties of a binary search tree?
No
(b) (10 points:)

If not, redraw the tree so that it is a proper binary search tree. Make the minimal amount of change necessary.

$\qquad$
$\qquad$ 3
(c) (10 points:)

Draw where node 57 will be inserted on the original figure above.

(d) (10 points:)

Which node is the successor of node 50 ?

55
(e) (Bonus: 5 points:)

Using the space below, draw the tree after node 30 is deleted.

$\qquad$ Login: $\qquad$ 4
3. QuadTree: (20 points:)


The image above is $400 \times 400$. The different shapes vary in size from $100 \times 100$, $100 \times 200,300 \times 300,200 \times 100$, and $100 \times 50$ (width $x$ height). Using the convention in your program for ordering quadtree children (NW, NE, SW, SE), draw the quadree representation of the image. Label the leaf nodes as R (red), G (green), or B (blue). Note: keep subdividing the tree if a quadrant is not a uniform color. You don't need to specify top-left and bottom-right coordinates.


