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Evaluation of mortality trajectories in evolutionary biodemography

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An important task in evolutionary biodemography is to determine the schedule of survival and reproduction as the outcome of natural selection acting on life histories. We do this by using a model in which the state of the organism is characterized by mass and accumulated damage, both of which are affected by activity and which affect the rate of mortality. Focusing on growth during the juvenile period, we determine the level of activity that maximizes reproductive value. Given this, we are able to project forward and determine the trajectory of mortality for an individual following the optimal life history, given the physiological and reproductive parameters. We show that there are two main classes of juvenile mortality trajectories: U-shaped (such as recently reported for prereproductive humans) and steadily declining and we are able to connect the shape of the mortality trajectory with the physiological and reproductive parameters characterizing the life history. Our work shows the importance of state in models of evolutionary biodemography and the power of modern computational methods to illuminate biological process.

free-radical theory | disposable soma | life history theory | dynamic programming

Demography is, in part, the study of the implications of a schedule of survival and mortality. The goal is to describe patterns, understand pattern and process, and predict the consequences of change on those patterns. Evolutionary biodemography asks about the origins of such schedules, in the context of evolution of life histories by natural selection. Evolutionary biodemography seeks to merge demography with evolutionary thinking (2–6). The result, for example, will be to use the comparative method to explore similarities and differences of patterns across species and to understand the patterns and mechanisms of vital statistics as the result of evolution by natural (and sometimes artificial) selection. Raymond Pearl, one of the founders of quantitative population biology, understood the importance of doing this but lacked the mathematical tools to do so. For example, with John Miner (7) he wrote “For it appears clear that there is no one universal ‘law’ of mortality. . . different species may differ in the age distribution of their dying just as characteristically as they differ in their morphology” and that “But what is wanted is a measure of the individual’s total activities of all sorts, over its whole life; and also a numerical expression that will serve as a measure of net integrated effectiveness of all of the environmental forces that have acted upon the individual throughout its life”. With the development of state-dependent life history theory (8–10), the tools now exist.

Here we respond to the challenge of Wachter (11), who noted that the evolutionary theories of aging generally fail to be able to predict the characteristics of mortality trajectories. To do this, we apply a recent development in state-dependent life history theory (12) that accounts for activity, the generation of cellular damage through metabolism and reinforcement of damage, repair of damage, and the mortality consequences of damage. This approach may be thought of as a fusion of the free-radical theory of aging (13) and the disposable soma theory (14) in an optimal life history context. Other efforts along these lines have

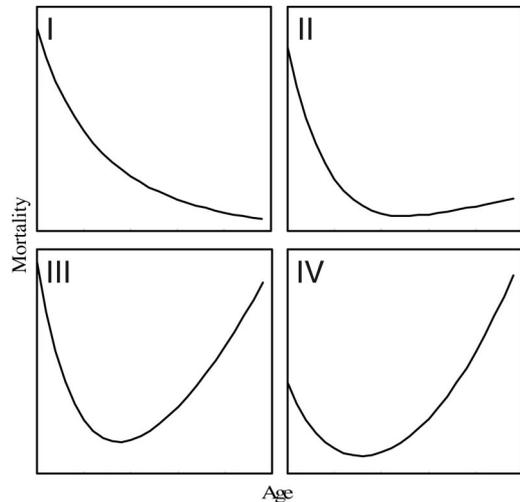


Fig. 1. The four classes of mortality trajectories produced by our modeling framework are steadily declining or broadly U-shaped.

developed simplified models with limited numbers of parameters (15, 16) or constructed models specific to a given system (17–19). In framing the aging problem as one driven by energy acquisition as well as allocation, our model is analogous to that recently developed by Yearsley *et al.* (20). However, our approach differs from these prior approaches in three important respects. First, the mortality trajectories we find are not *a priori* governed by a particular functional form but rather are an emergent property of the life history optimization. Thus, the range of trajectories that are possible is not constrained to lie within some traditional family of functions. Second, we focus on the development of mortality trajectories before the onset of maturation. Clearly, this departure from the traditional approach leaves open the question of what happens after maturation. Nevertheless, we obtain worthwhile insights into the shape of prereproductive mortality trajectories. Third, rather than focusing on parameters attributable to a particular species, we attempt to enumerate all of the trajectory shapes possible within a fairly broad range of the parameter space. We used 3,000 parameter sets to characterize the mortality trajectories that this framework is capable of producing. After visual inspection of all 3,000 optimal mortality trajectories, four main classes of shapes emerged (Fig. 1). We tabulated the frequency with which each trajectory shape occurred and note the fitness and final size associated with each

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accumulated damage through their effects on fecundity and mortality after the growth interval. Evaluation of this expression would require dynamical assumptions beyond those already presented. To simplify, we use a product of two power functions to approximate the size and damage dependence of residual reproductive value, i.e.,

$$V(X, D) = X^{\phi_X} (1 + D)^{-\phi_D}, \quad [7]$$

where the exponents for size ϕ_X and damage ϕ_D are treated as parameters and allowed to range widely.

Working backwards through the growth interval, we define a fitness function $F(x, d, t)$ by

$$F(x, d, t) = \max_a \{V(X(T), D(T)|X(t) = x, D(t) = d)\}, \quad [8]$$

so that $F(x, d, t)$ is the maximum fitness at the end of the growth interval $[t, T]$ taken over activity levels at each instant of time throughout the interval. When $t = T$, fitness is given by the residual reproductive value. That is, we have (from Eq. 7) $F(x, d, T) = V(x, d) = x^{\phi_X}(1 + d)^{-\phi_D}$.

For previous times, $F(x, d, t)$ satisfies an equation of dynamic programming (8–10)

$$F(x, d, t) = \max_a \{(1 - M(x, d, a)dt)F(x + dX, d + dD, t + dt)\}, \quad [9]$$

which is solved backwards in time, from $t = T - dt$ to $t = 0$. Essentially, Eq. 9 works backwards through time calculating present reproductive value by discounting the future reproductive value with the probability of surviving the time interval. The boundaries of the size – damage grid were chosen such that they had no effect on the optimal trajectories for the starting sizes we used. In some of our initial runs, the upper bound for damage was low enough to influence the outcome and mortality plateaus were observed. At $t = 0$, $F(x, d, 0)$ is the maximum value of F (lifetime reproductive output) attainable given initial size and damage. At each time and state, we generate the optimal level of activity $a^*(x, d, t)$, which can then be used to predict growth trajectories by application of Eqs. 1 and 2. For all simulations, we

set $T = 5$ and in general we used $dt = 0.05$, but setting $dt = 0.001$ did not change the results.

All of the physiological and life history parameters in the model have mechanistic interpretations and could in principle be determined experimentally (the parameters governing damage, though, may be more difficult to quantify). However, the range of plausible parameter combinations is too broad to investigate completely. So, to analyze the model, we adopted a Monte Carlo approach. We defined ranges for each parameter such that a reasonable amount of growth could occur in the interval $[0, T]$ and that there was some nonzero probability of surviving to the end of the growth interval. We acknowledge that this approach leaves open the question of what happens to mortality trajectories beyond the ranges from which we sampled. However, preliminary sampling outside the ranges reported here did not produce any new trajectory types. For each parameter, this range was divided into up to 30 distinct values (see ref. 12, Table 1) resulting in $>10^{10}$ possible parameter combinations. Because this space is too large for complete enumeration, we randomly chose 10,000 parameter sets from these possible combinations and evaluated the optimal life history for each. Parameter sets from this range that produced implausible results (e.g., that the optimal growth trajectory was to never grow) were discarded, leaving $\approx 3,000$ viable parameter sets. The vast majority of nonviable parameter sets resulted in damage accumulation rates that were so costly as to eliminate the feasibility of growth.

To analyze the influence of the different physiological and life history parameters on the resultant mortality trajectories, we used linear and quadratic discriminant functions (30) on the original parameter set and an augmented set that included all pairwise products. Using leave-one-out cross-validation as a model selection criterion, we found that a linear model in the augmented parameter space was optimal and had a cross-validation classification success of 76%.

All of the analyses reported here were carried out by using code written by SM in Matlab v. 6.5 (Mathworks, Natick, MA). This code is available upon request.

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