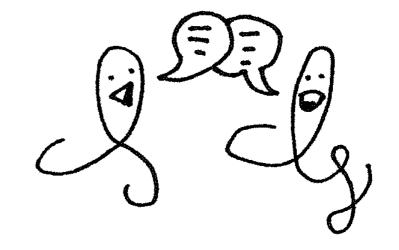
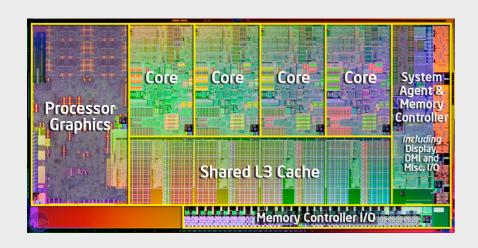
Abstractions for {Expressive, Efficient} Parallel and Distributed Computing

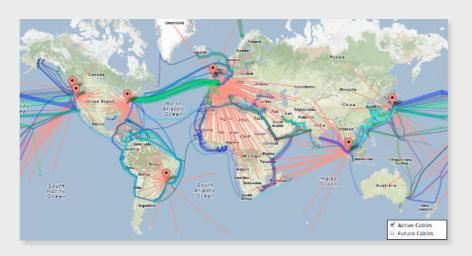
Lindsey Kuper Assistant Professor, Computer Science and Engineering UC Santa Cruz

Jane Street Tech Talk January 24, 2019

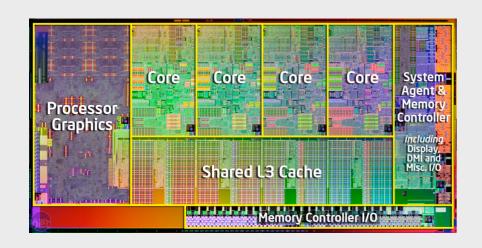




Parallel systems



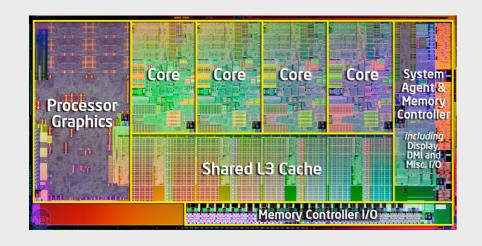
Distributed systems





Distributed systems

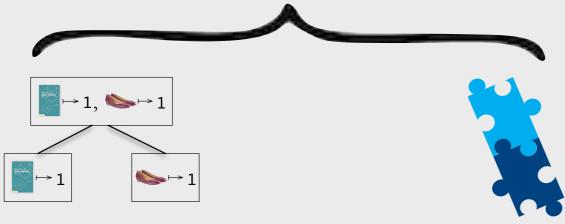
language-based approaches





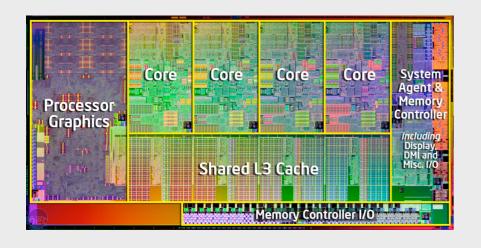
Distributed systems

language-based approaches



Lattice-based data structures (LVars) for deterministic programming [POPL '14, PLDI '14, FHPC '13, WoDet '14]

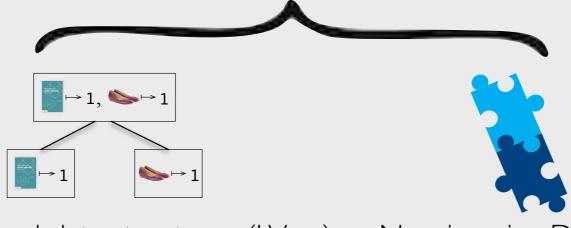
Non-invasive DSLs for productive parallelism [ECOOP'17]





Distributed systems

language-based approaches

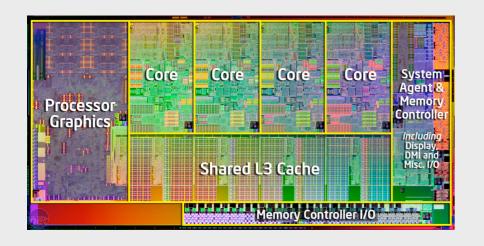


Lattice-based data structures (LVars) for deterministic programming [POPL'14, PLDI'14, FHPC'13, WoDet'14]

Non-invasive DSLs for productive parallelism [ECOOP'17]



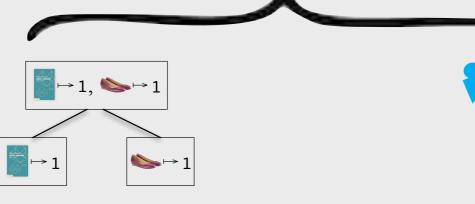
Guiding principle: Find the right **high-level abstractions** to enable **efficient** computation





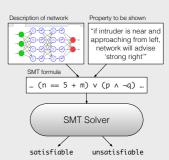
Distributed systems

language-based approaches



Lattice-based data structures (LVars) for deterministic programming [POPL'14, PLDI'14, FHPC'13, WoDet'14]

Non-invasive DSLs for productive parallelism

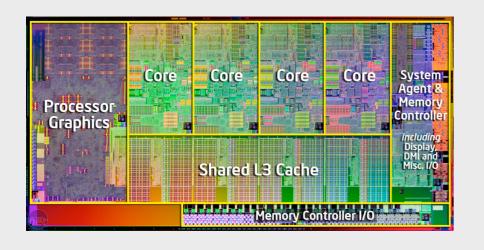


SMT-based verification of neural networks
[SysML'18]



Guiding principle:

Find the right high-level abstractions to enable efficient computation

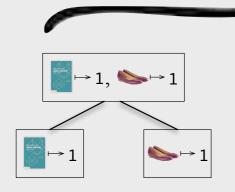




Parallel systems

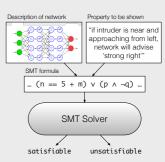
Distributed systems

language-based approaches



Lattice-based data structures (LVars) for deterministic programming [POPL '14, PLDI '14, FHPC '13, WoDet '14]

Non-invasive DSLs for productive parallelism [ECOOP'17]

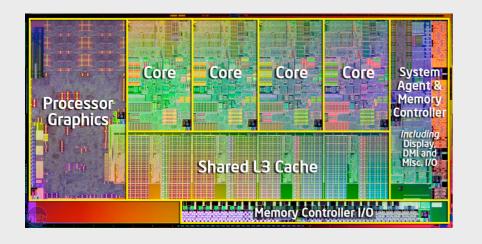


SMT-based verification of neural networks
[SysML'18]



Guiding principle:

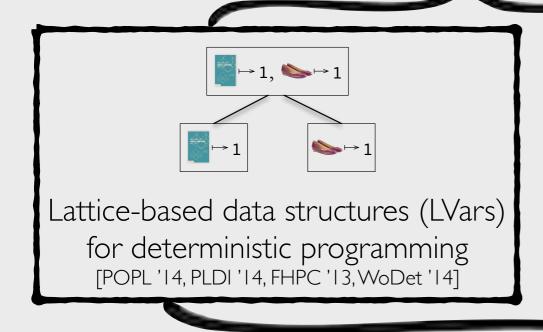
Find the right high-level abstractions to enable efficient computation





Distributed systems

language-based approaches







SMT-based verification of neural networks
[SysML'18]



Guiding principle:

Find the right high-level abstractions to enable efficient computation



data Item = Book | Shoes | ...



```
data Item = Book | Shoes | ...

p :: IO (Map Item Int)
p = do cart <- newIORef empty</pre>
```

```
data Item = Book | Shoes | ...

p :: IO (Map Item Int)
p = do cart <- newIORef empty</pre>
```















```
landin:lvar-examples lkuper$ make map-ioref-data-race
 ghc -02 map-ioref-data-race.hs -rtsopts -threaded
 [1 of 1] Compiling Main
                                                                                                                                                                                                 ( map-ioref-data-race.hs, map-ioref-data-race.o )
Linking map-ioref-data-race ...
while true; do ./map-ioref-data-race +RTS -N2; done
[(Book,1),(Shoes,1)][(Shoes,1)][(Book,1),(Shoes,1)][(Shoes,1)][(Book,1),(Shoes,1)][(Book,1)
),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)]
 )][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1)
),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)]
 )][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1)
),(Shoes,1)][(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Shoes,1)][(Book,1),(Shoes
  ,1)][(Book,1),(Shoes,1)][(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoe,1)][(Book,1),(S
s,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoe,1)][(
 k,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)]
 s,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Shoes,1)][(Book,1),(Sho
 es,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoe,1)][(Book,1),(Shoe,1)][(Book,1),(Shoe,1)][(B
ok,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoe,1)][(Book,1),(Shoe,1)][(Book,1),(Shoe,1)][(Book,1),(Shoe,1)][(Book,1),(Shoe,1)][(Book,1),(Shoe,1)][(Boo
 ook,1),(Shoes,1)][(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(
 Book, 1), (Shoes, 1)][(Shoes, 1)][(Book, 1), (Shoes, 1)][(Book, 1), (Shoes, 1)][(Book, 1), (Shoes, 1)][
 (Book, 1), (Shoes, 1)][(Book, 1), (Shoes, 1)][(Shoes, 1)][(Book, 1), (Shoes, 1)][(Book, 1), (Shoes, 1)]
 [(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),
 (Shoes,1)][(Book,1),(Shoes,1)][(Book,1)][(Book,1),(Shoes,1)][(Shoes,1)][(Book,1),(Shoes,1)
[[(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1)][(Book,1),(Shoes,1)]
[(Shoes,1)][(Shoes,1)][(Book,1),(Shoes,1)][(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)]
 ,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book
 ,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoe,1)][(Book,1),(Shoe,1)][(Book,1),(Shoe,1)][(Book,1),(Shoe,1)][(Book,1),(Shoe,1)][(Book
k,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)]
```



```
landin:lvar-examples lkuper$ make map-ioref-data-race
  ghc -02 map-ioref-data-race.hs -rtsopts -threaded
  [1 of 1] Compiling Main
                                                                                                                                                                                                   ( map-ioref-data-race.hs, map-ioref-data-race.o )
 Linking map-ioref-data-race ...
                                                                                  /man-ioref-data-race +RTS -N2; done
  [(Book,1),(Shoes,1)] (Shoes,1)][(Book,1),(Shoes,1)][(Shoes,1)][(Book,1),(Shoes,1)][(Book,1
,(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)]
  )][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1)
  ),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)]
  )][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1)
  ),(Shoes,1)][(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Shoes,1)][(Book,1),(Shoes
   ,1)][(Book,1),(Shoes,1)][(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoe,1)][(Book,1),(S
  s,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoe,1)][(
  k,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoe
  s,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Shoes,1)][(Book,1),(Sho
  es,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoe,1)][(Book,1),(Shoe,1)][(Book,1),(Shoe,1)][(B
  ok,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Shoes,1)][(B
  ook,1),(Shoes,1)][(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(
  Book, 1), (Shoes, 1)][(Shoes, 1)][(Book, 1), (Shoes, 1)][(Book, 1), (Shoes, 1)][(Book, 1), (Shoes, 1)][
  (Book, 1), (Shoes, 1)][(Book, 1), (Shoes, 1)][(Shoes, 1)][(Book, 1), (Shoes, 1)][(Book, 1), (Shoes, 1)]
  [(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),
  (Shoes,1)][(Book,1),(Shoes,1)][(Book,1)][(Book,1),(Shoes,1)][(Shoes,1)][(Book,1),(Shoes,1)
 [[Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1)][(Book,1),(Shoes,1)]
 [(Shoes,1)][(Shoes,1)][(Book,1),(Shoes,1)][(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)]
  ,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoe,1)][(Book,1),(Shoe,1)][(Book,1),(Shoe,1)][(Book,1),(Shoe,1)][(Book
  ,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoe,1)][(Book,1),(Shoe,1)][(Book,1),(Shoe,1)][(Book,1),(Shoe,1)][(Book,1),(Shoe,1)][(Book
  k,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)]
```



```
landin:lvar-examples lkuper$ make map-ioref-data-race
 ghc -02 map-ioref-data-race.hs -rtsopts -threaded
 [1 of 1] Compiling Main
                                                                                                                                                                     ( map-ioref-data-race.hs, map-ioref-data-race.o )
Linking map-ioref-data-race ...
                                                                      /man-ioref-data-race +RTS -N2; done
                                                                                           (Shoes,1)] (Book,1),(Shoes,1) [(Shoes,1)] (Book,1),(Shoes,1)][(Book,1
\Gamma(Book,1),(Shoes,1)
J, (Shoes, 1), (Shoes, 1)
 )][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1)
 ),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)]
 )][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1)
),(Shoes,1)][(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Shoes,1)][(Book,1),(Shoes,1)][(Shoes,1)][(Book,1),(Shoes,1)][(Shoes,1)][(Book,1),(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1
  ,1)][(Book,1),(Shoes,1)][(Shoes,1)] (Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)]
 s,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)]
 k,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoe
 s,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Shoes,1)][(Book,1),(Sho
 es,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoe,1)][(Book,1),(Shoe,1)][(Book,1),(Shoe,1)][(B
ok,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Shoes,1)]
 ook,1),(Shoes,1)][(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)]
 Book, 1), (Shoes, 1)][(Shoes, 1)][(Book, 1), (Shoes, 1)][(Book, 1), (Shoes, 1)][(Book, 1), (Shoes, 1)][
 (Book, 1), (Shoes, 1)][(Book, 1), (Shoes, 1)][(Shoes, 1)][(Book, 1), (Shoes, 1)][(Book, 1), (Shoes, 1)]
 [(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),
 (Shoes,1)][(Book,1),(Shoes,1)][(Book,1)][(Book,1),(Shoes,1)][(Shoes,1)][(Book,1),(Shoes,1)]
                                     1) (Shoes, 1)][(Book, 1), (Shoes, 1)][(Book, 1), (Shoes, 1)][(Book, 1)][(Book, 1), (Shoes, 1)]
      [(Shoes,1)] (Shoes,1)][(Book,1),(Shoes,1)][(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes
 , 1) | [(Βοοκ, 1), (Shoes, 1)] [(Βοοκ, 1), (Shoes, 1)] [(Βοοκ, 1), (Shoes, 1)] [(Βοοκ, 1), (Shoes, 1)]
 ,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Shoes,1)] (Book
 k,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)](Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(
```



```
landin:lvar-examples lkuper$ make map-ioref-data-race
 ghc -02 map-ioref-data-race.hs -rtsopts -threaded
 [1 of 1] Compiling Main
                                                                                                                                                                   ( map-ioref-data-race.hs, map-ioref-data-race.o )
Linking map-ioref-data-race ...
                                                                     /man-ioref-data-race +RTS -N2; done
                                                                                          (Shoes,1)] (Book,1),(Shoes,1) [(Shoes,1)] (Book,1),(Shoes,1)][(Book,1
\Gamma(Book,1),(Shoes,1)
J, (Shoes, 1), (Shoes, 1)
 )][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1)
 ),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)]
 )][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1)
),(Shoes,1)][(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Shoes,1)][(Book,1),(Shoes,1)][(Shoes,1)][(Book,1),(Shoes,1)][(Shoes,1)][(Book,1),(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1)][(Shoes,1
  ,1)][(Book,1),(Shoes,1)][(Shoes,1)] (Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)]
 s,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)]
 k,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoe
 s,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Shoes,1)][(Book,1),(Sho
 es,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoe,1)][(Book,1),(Shoe,1)][(Book,1),(Shoe,1)][(B
ok,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Shoes,1)]
 ook,1),(Shoes,1)][(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)
 Book, 1), (Shoes, 1)][(Shoes, 1)][(Book, 1), (Shoes, 1)][(Book, 1), (Shoes, 1)][(Book, 1), (Shoes, 1)][
 (Book, 1), (Shoes, 1)][(Book, 1), (Shoes, 1)][(Shoes, 1)][(Book, 1), (Shoes, 1)][(Book, 1), (Shoes, 1)]
 [(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),
 (Shoes,1)][(Book,1),(Shoes,1) [(Book,1)] (Book,1),(Shoes,1)][(Shoes,1)][(Book,1),(Shoes,1)]
                                               (Shoes,1) [(Book,1,,(Shoes,1),(Shoes,1) [(Book,1),(Shoes,1)]
      [(Shoes,1)] (Shoes,1)][(Book,1),(Shoes,1)][(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes
 ,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Shoes,1)] (Book
 k,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)][(Book,1),(Shoes,1)](Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(Shoes,1)][(Βοοκ,1),(
```



if we want determinism, we have to share nicely



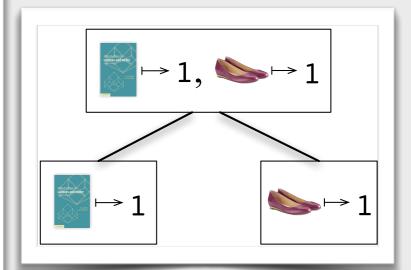
```
data Item = Book | Shoes | ...
p :: IO (Map Item Int)
p = do cart <- newIORef empty</pre>
       a1 <- async (atomicModifyIORef cart</pre>
                (insert Book 1))
       a2 <- async (atomicModifyIORef cart</pre>
                (insert Shoes 1))
       res <- async (do waitBoth a1 a2
                          readIORef cart)
       wait res
```





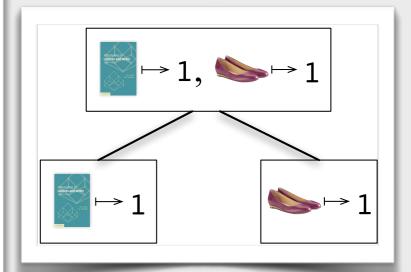








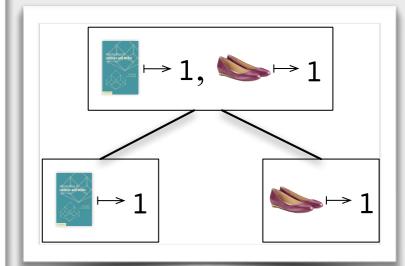




LVars: multiple commutative and inflationary writes, blocking threshold reads
[FHPC '13]



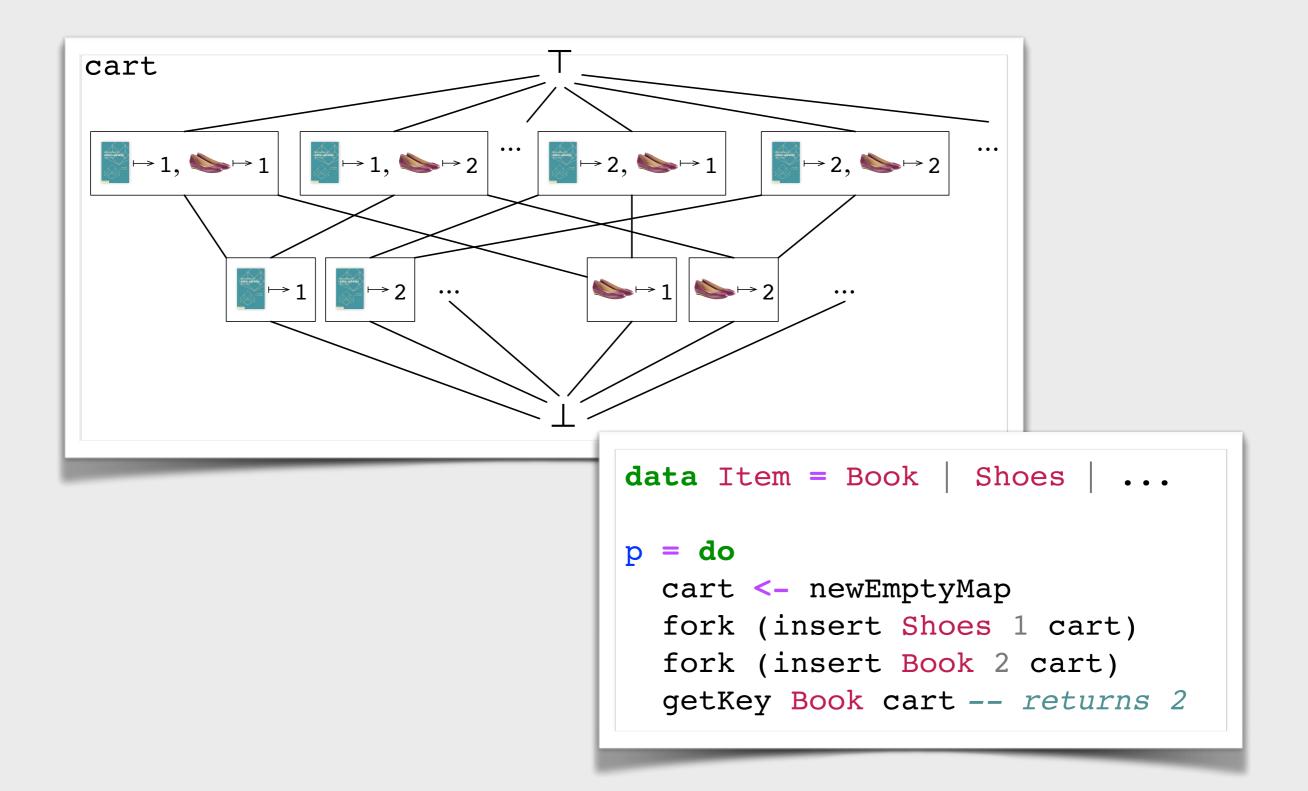


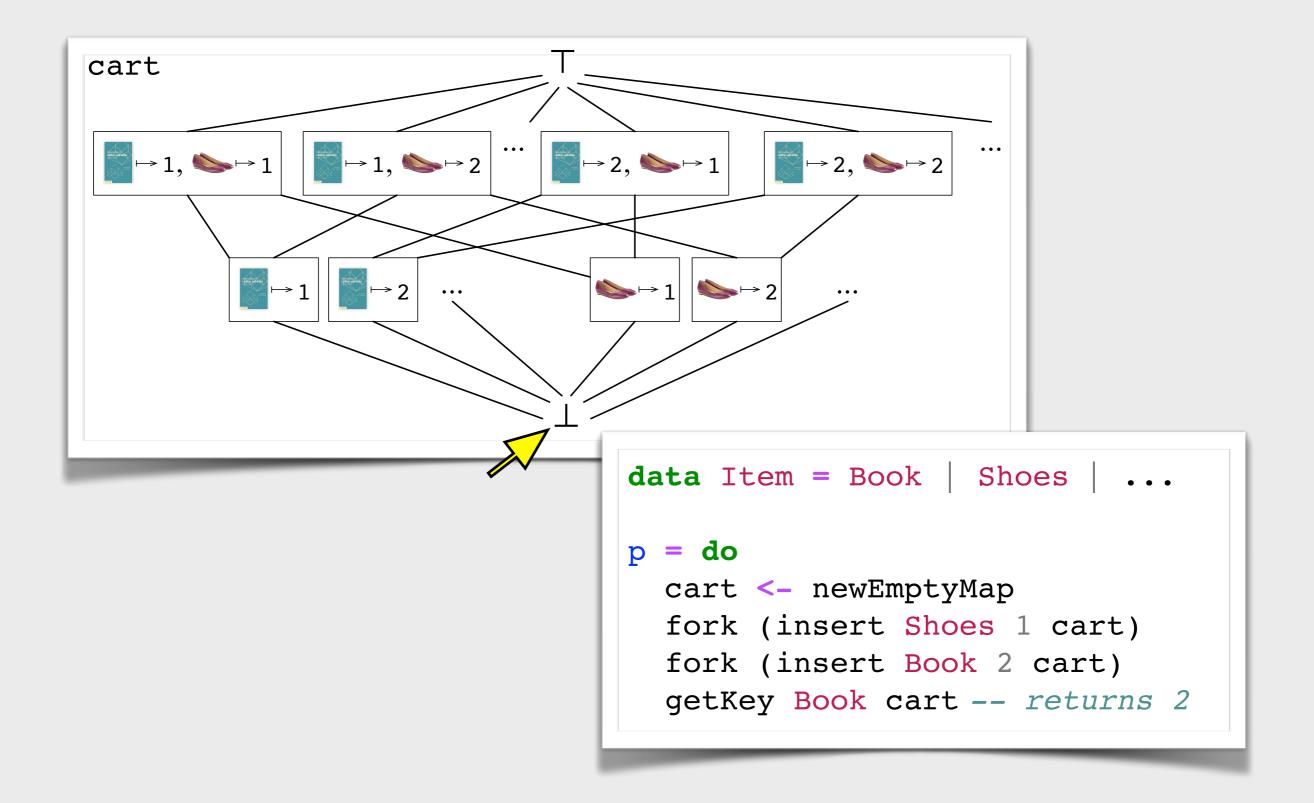


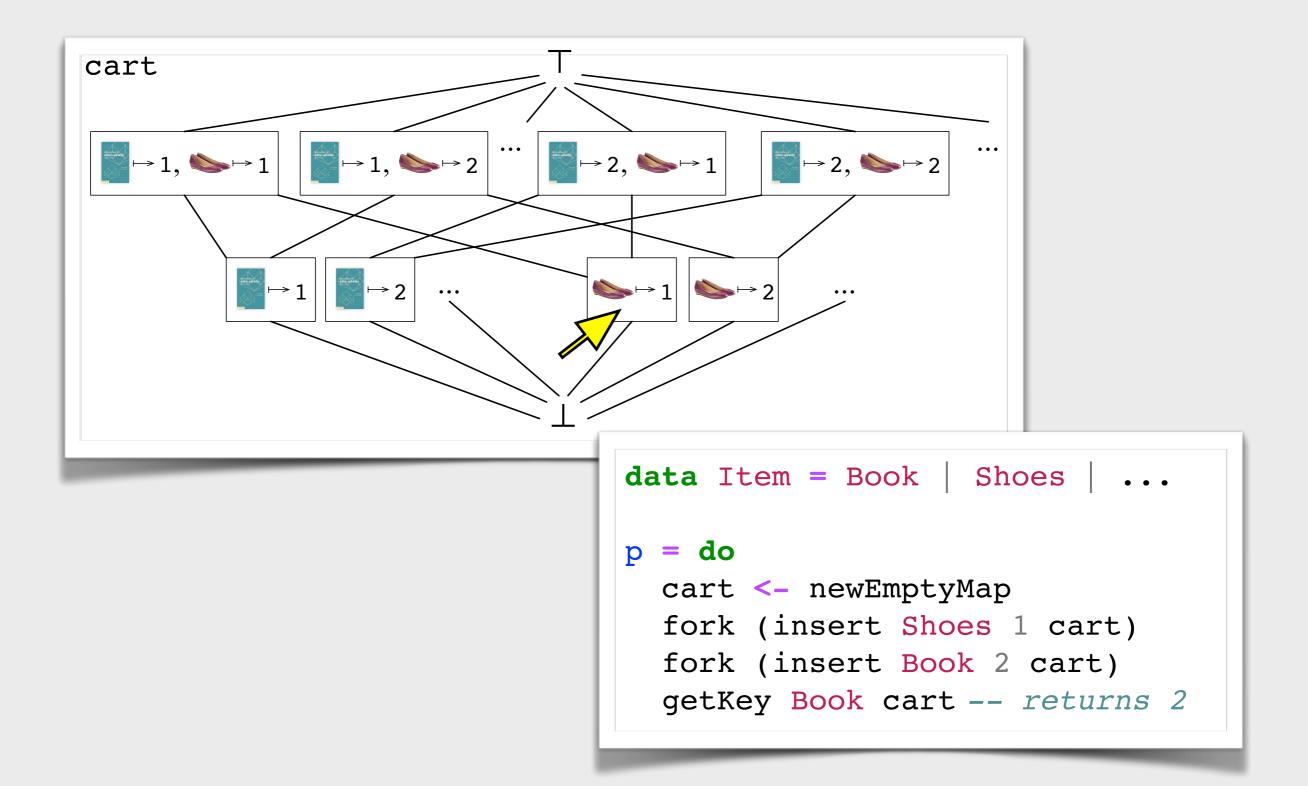
LVars: multiple commutative and inflationary writes, blocking threshold reads
[FHPC '13]

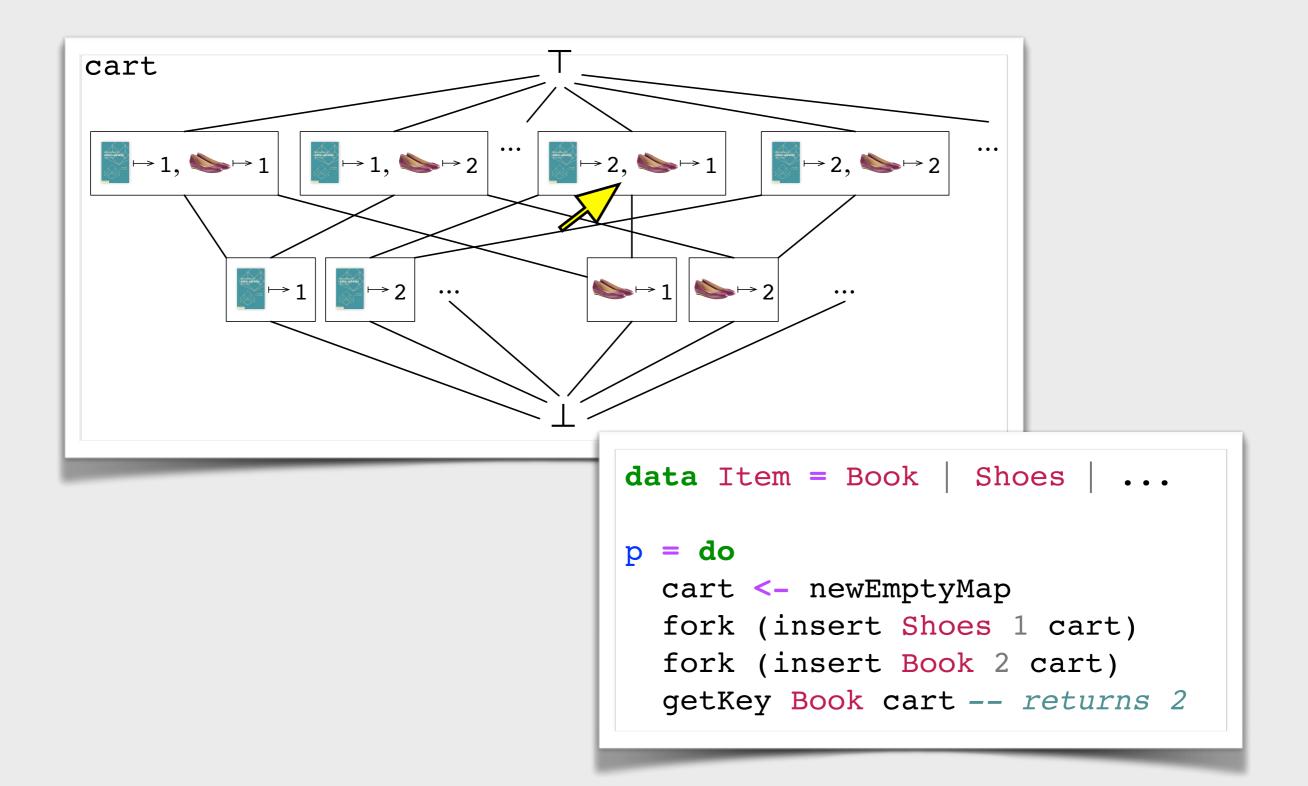


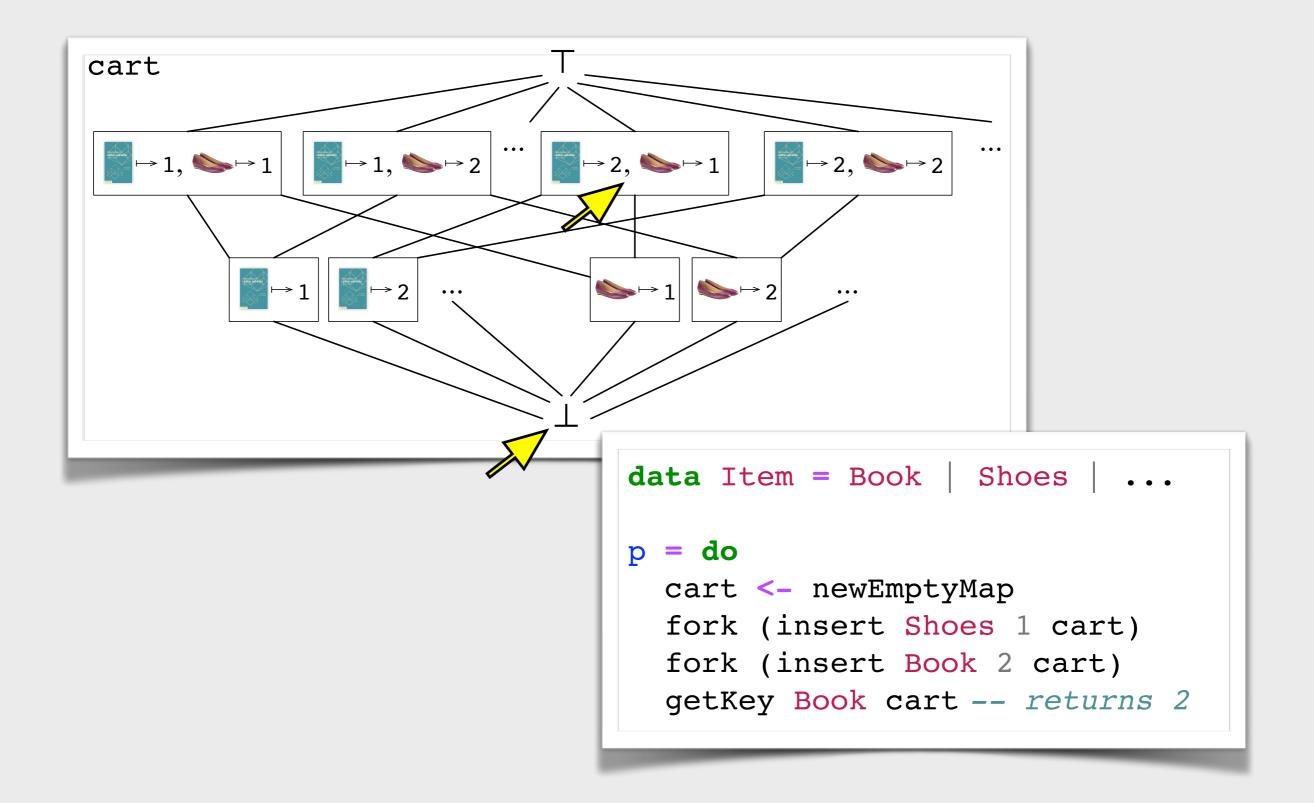
^{*} actually a bounded join-semilattice

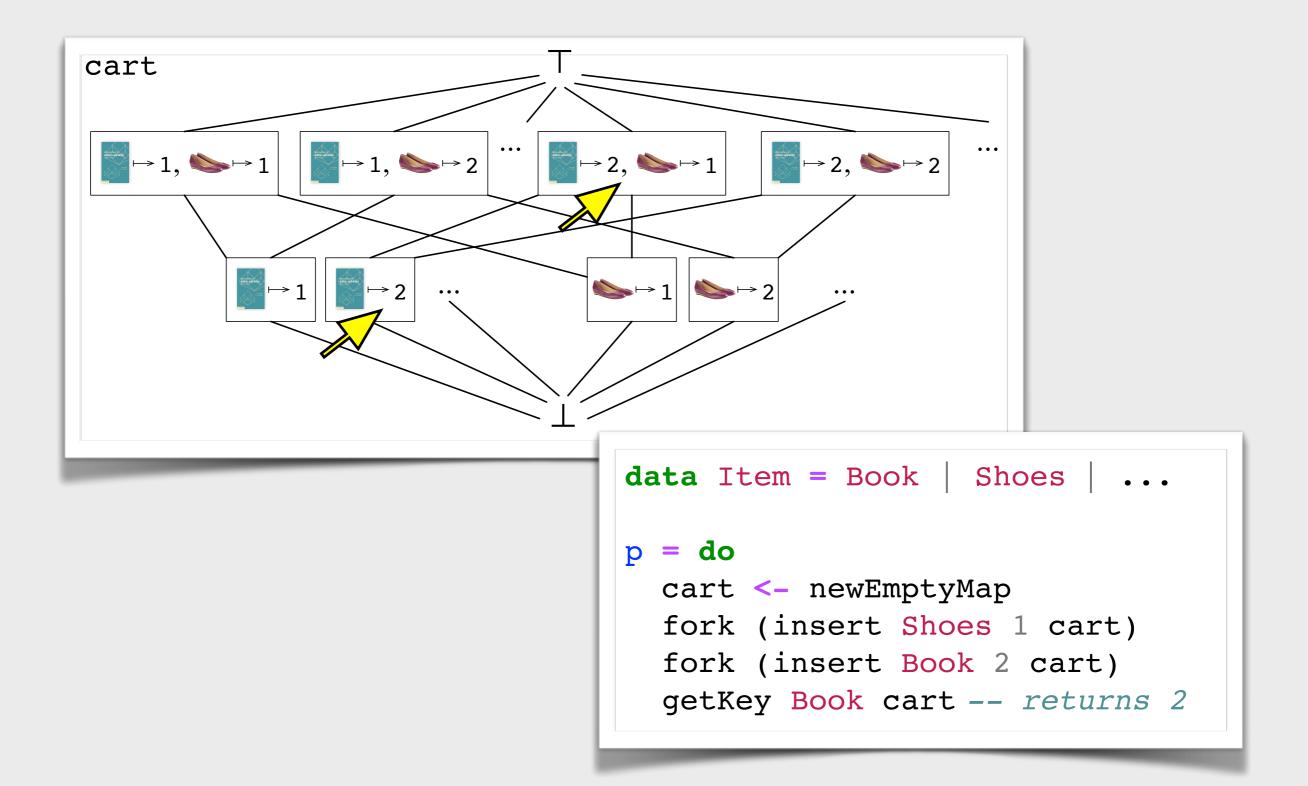


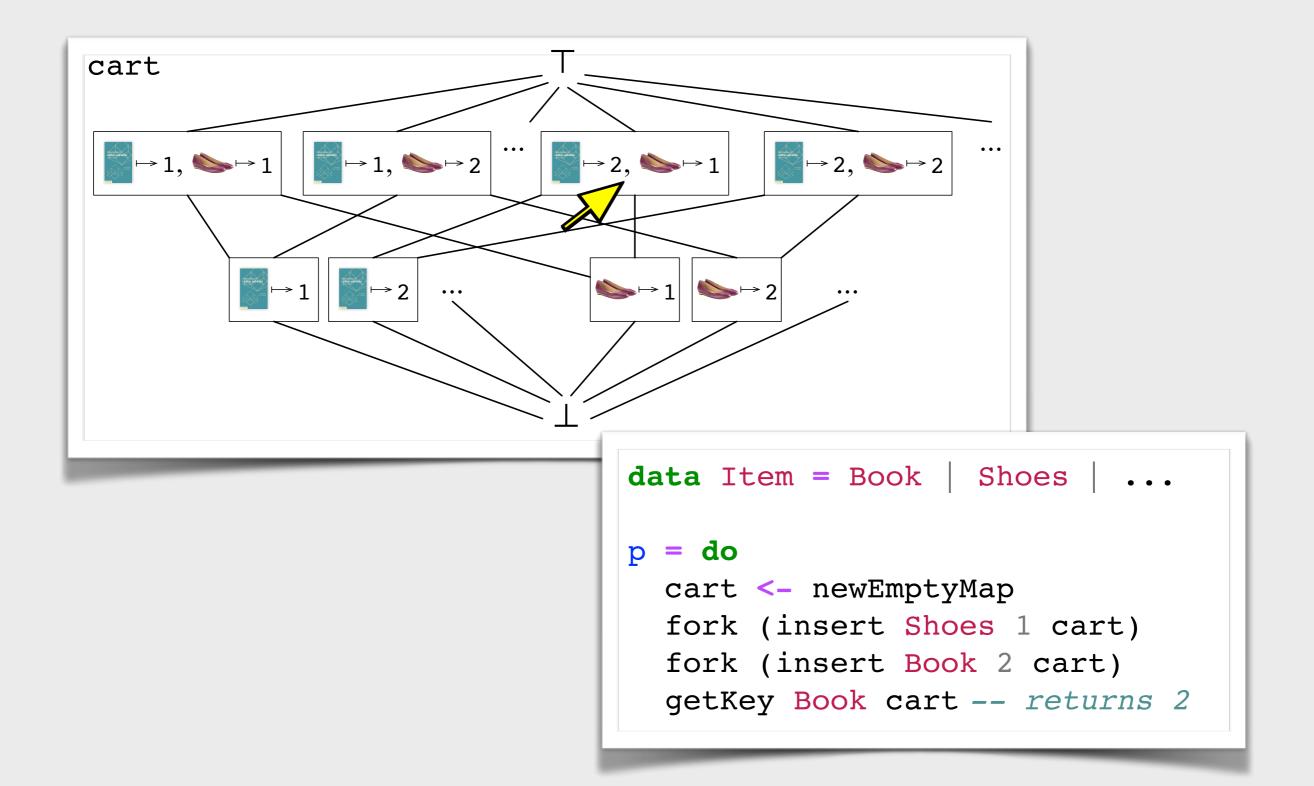


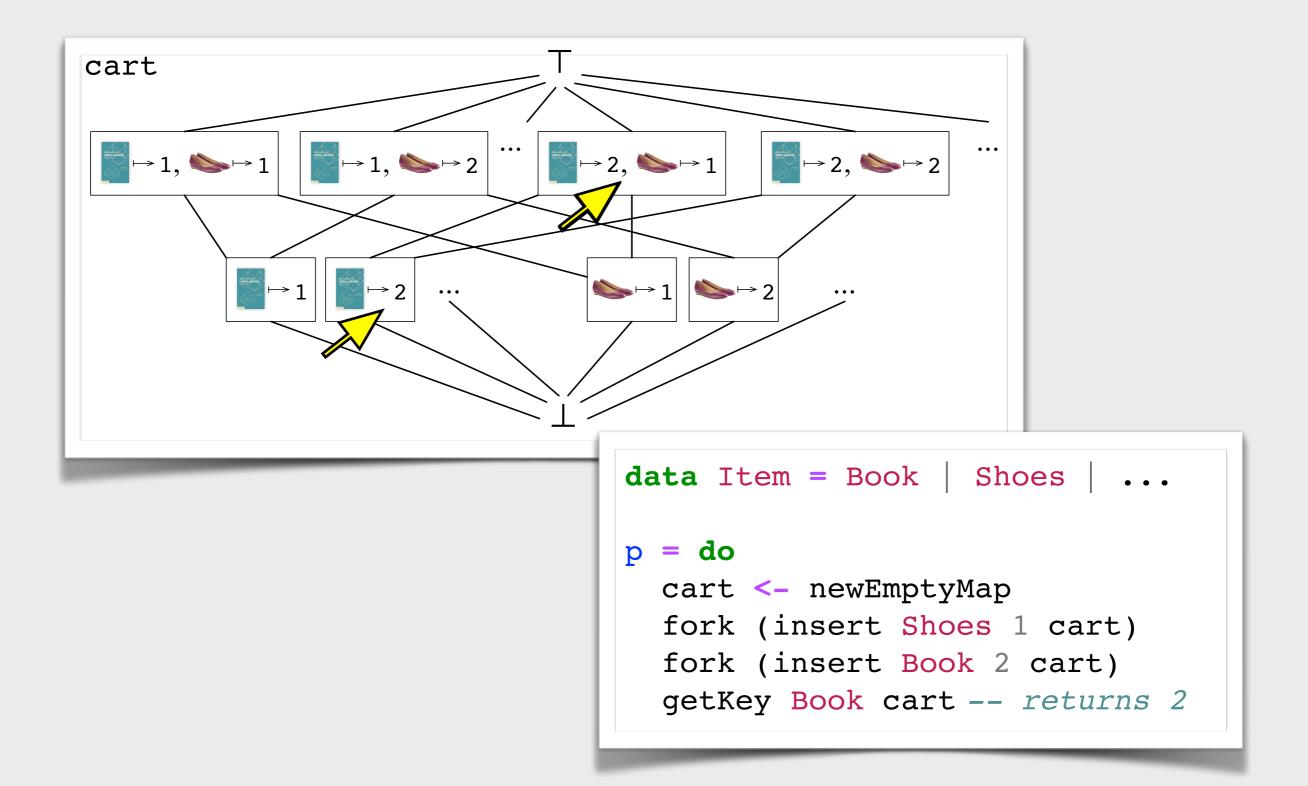


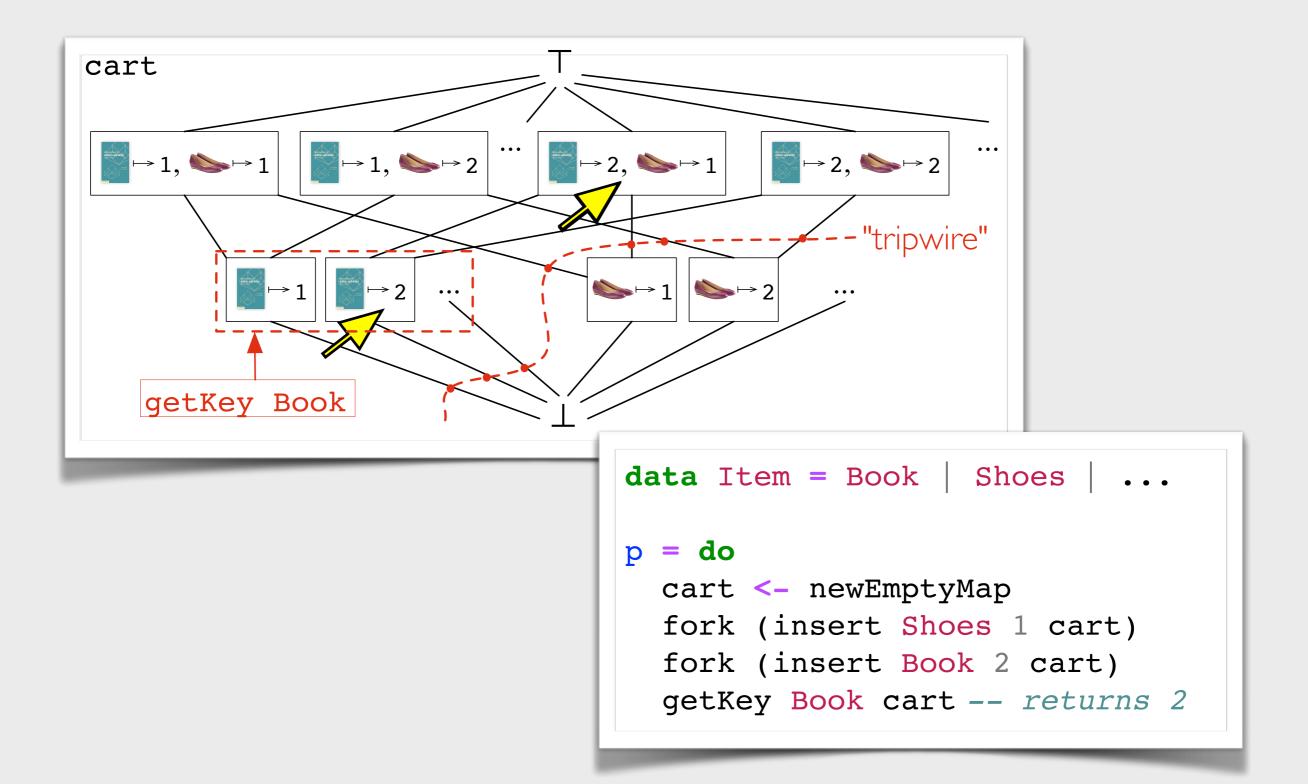


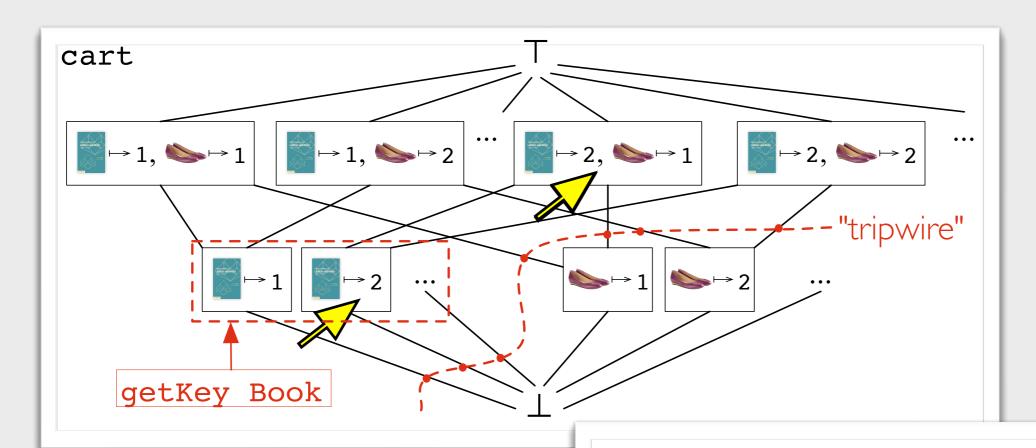








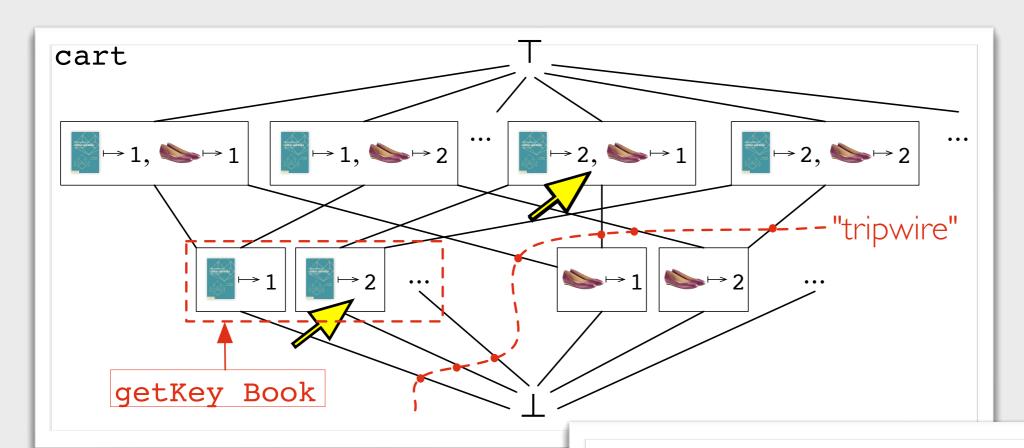




- Writes must be commutative and inflationary
- Threshold sets must be pairwise incompatible

```
data Item = Book | Shoes | ...

p = do
    cart <- newEmptyMap
    fork (insert Shoes 1 cart)
    fork (insert Book 2 cart)
    getKey Book cart -- returns 2</pre>
```

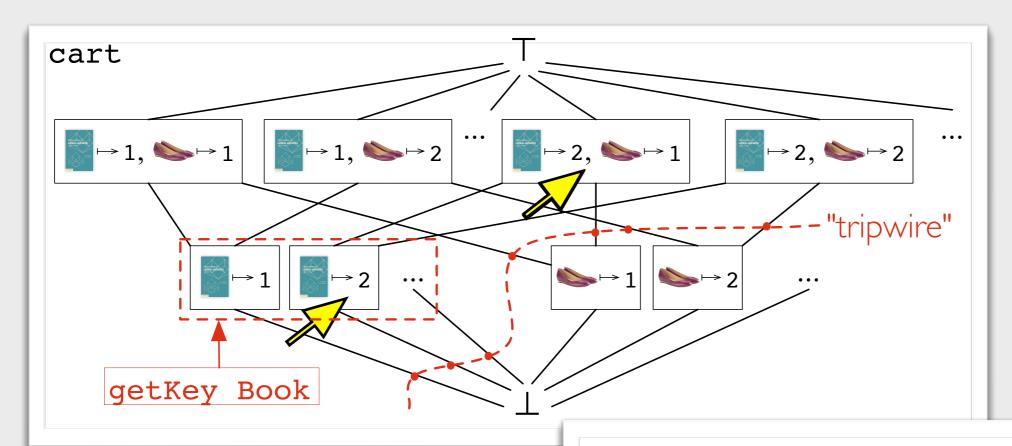


- Writes must be commutative and inflationary
- Threshold sets must be pairwise incompatible

\
library obligations

```
data Item = Book | Shoes | ...

p = do
    cart <- newEmptyMap
    fork (insert Shoes 1 cart)
    fork (insert Book 2 cart)
    getKey Book cart -- returns 2</pre>
```



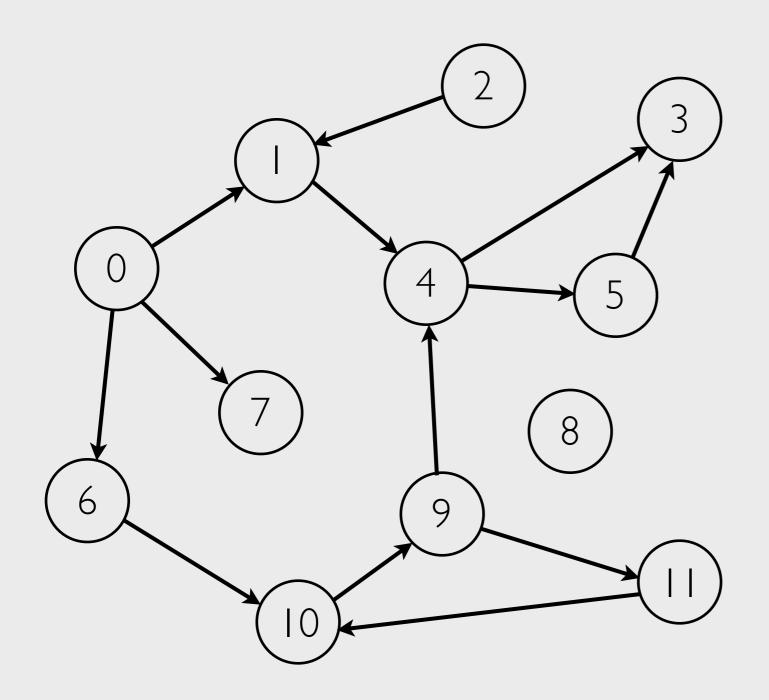
- Writes must be commutative and inflationary
- Threshold sets must be pairwise incompatible

library obligations

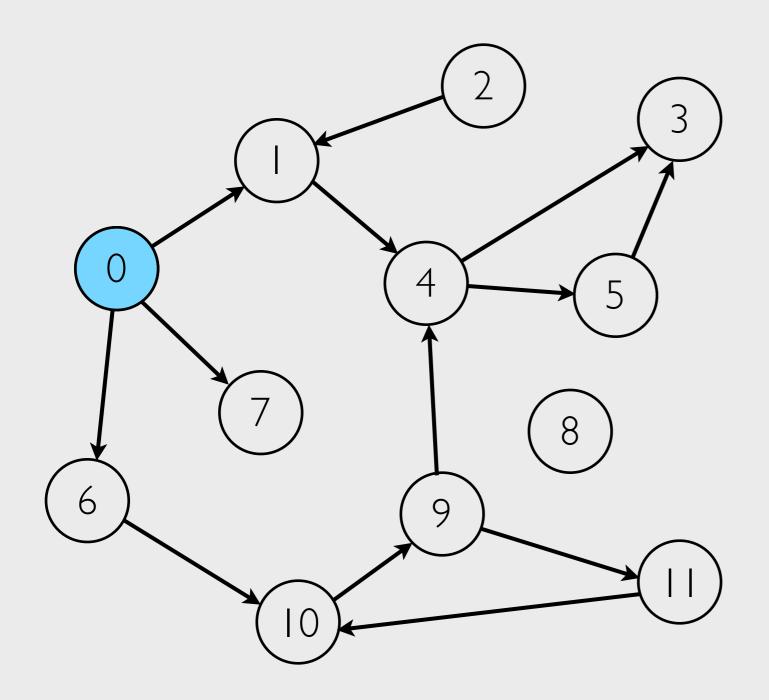
```
data Item = Book | Shoes | ...

p = do
    cart <- newEmptyMap
    fork (insert Shoes 1 cart)
    fork (insert Book 2 cart)
    getKey Book cart -- returns 2</pre>
```

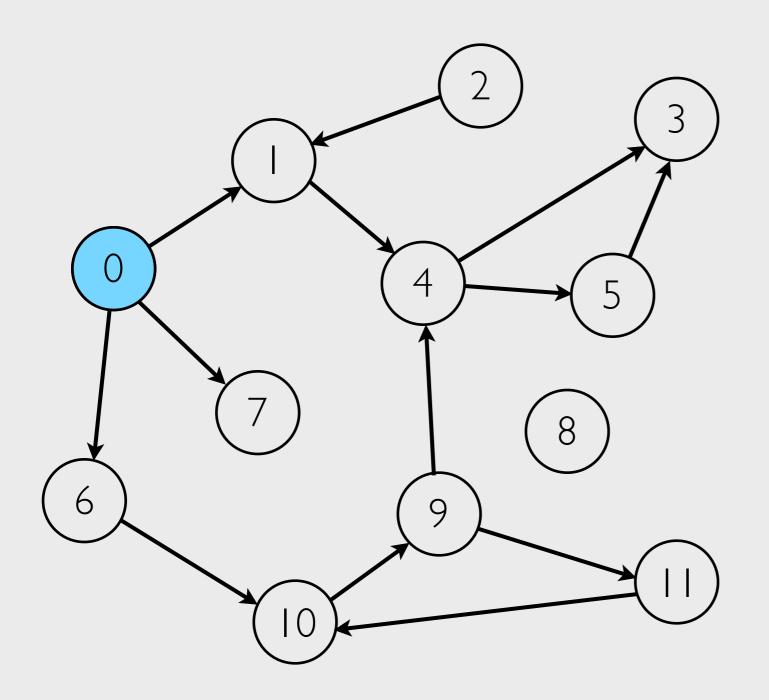
client guarantee

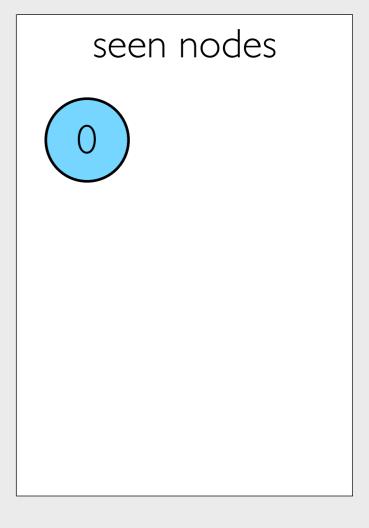


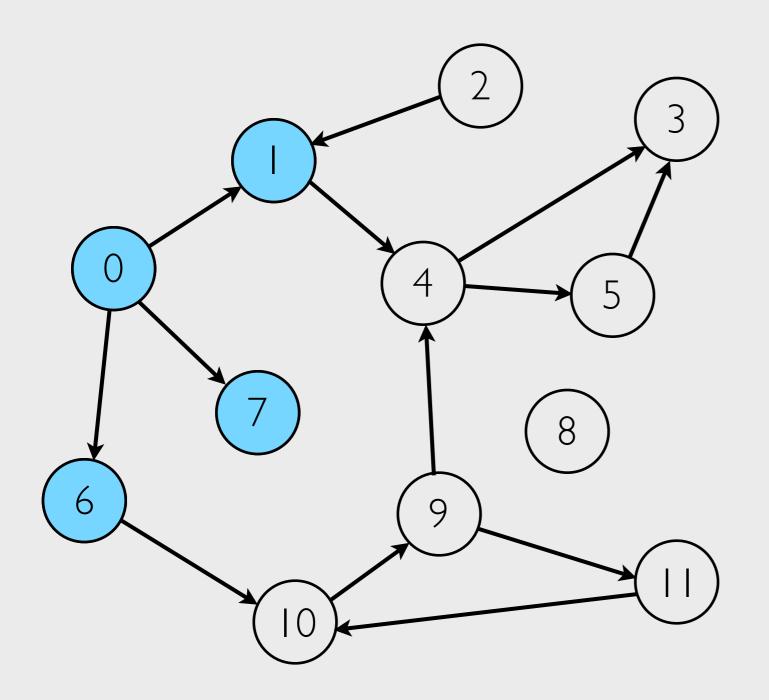
seen nodes

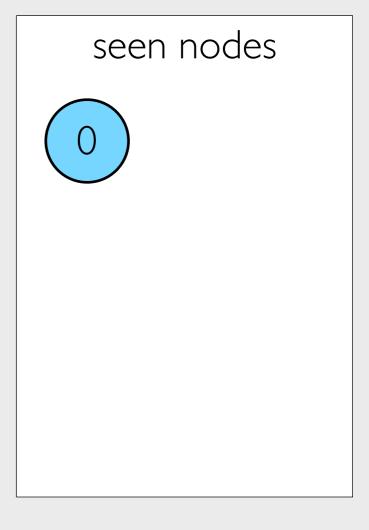


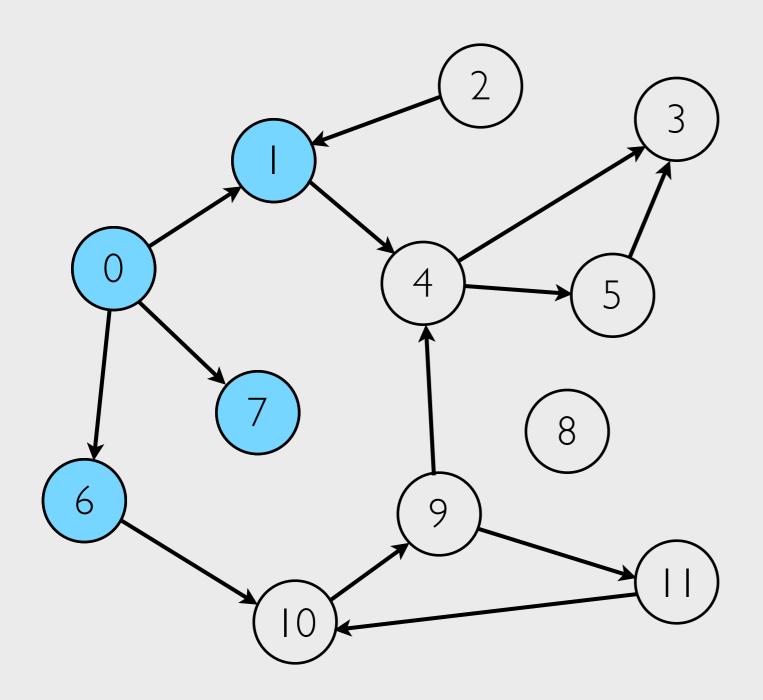
seen nodes

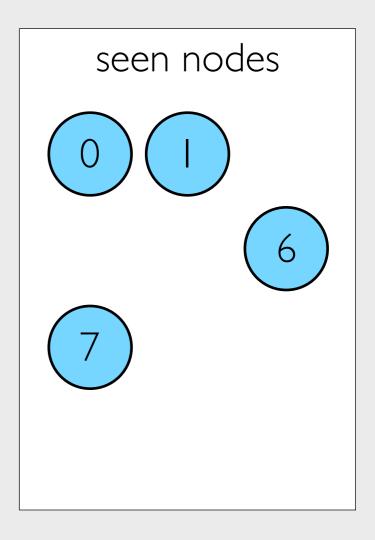


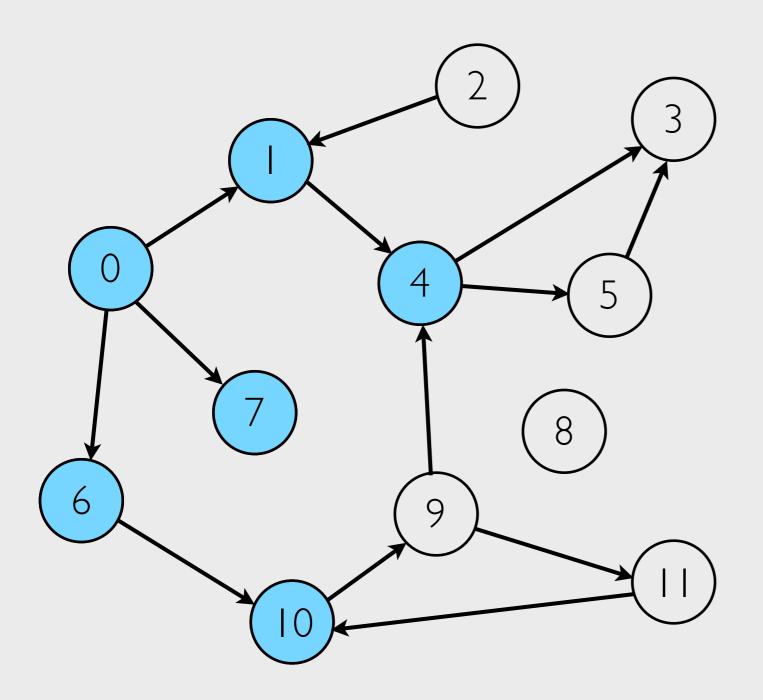


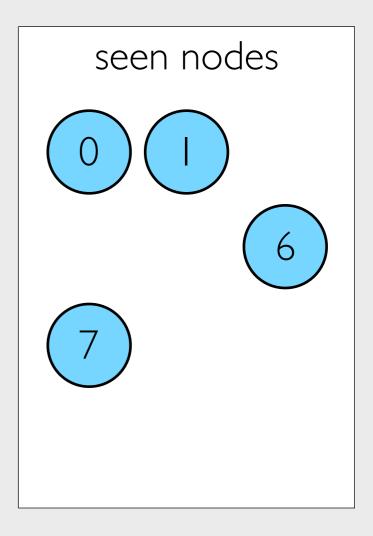


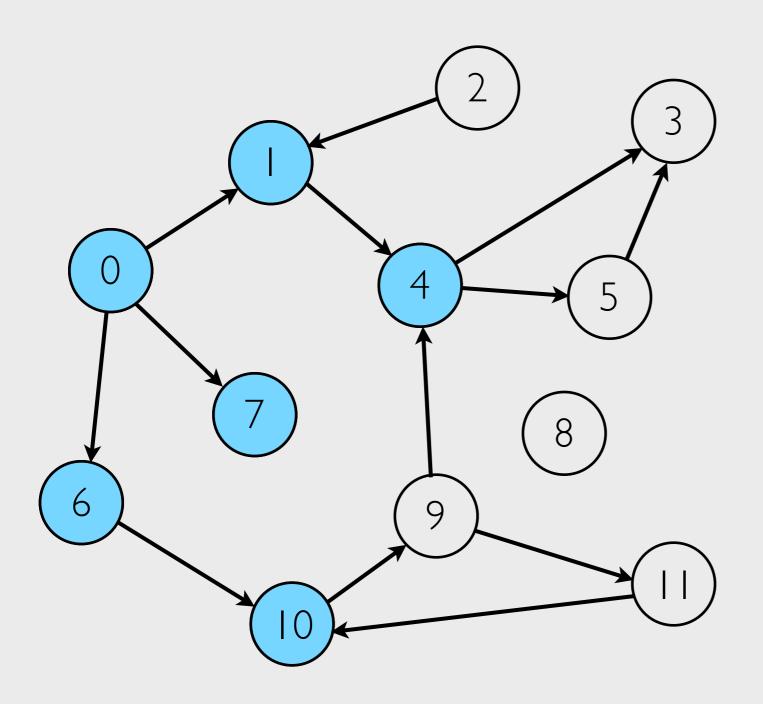


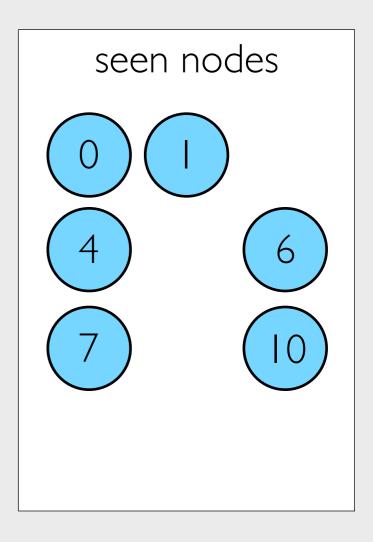


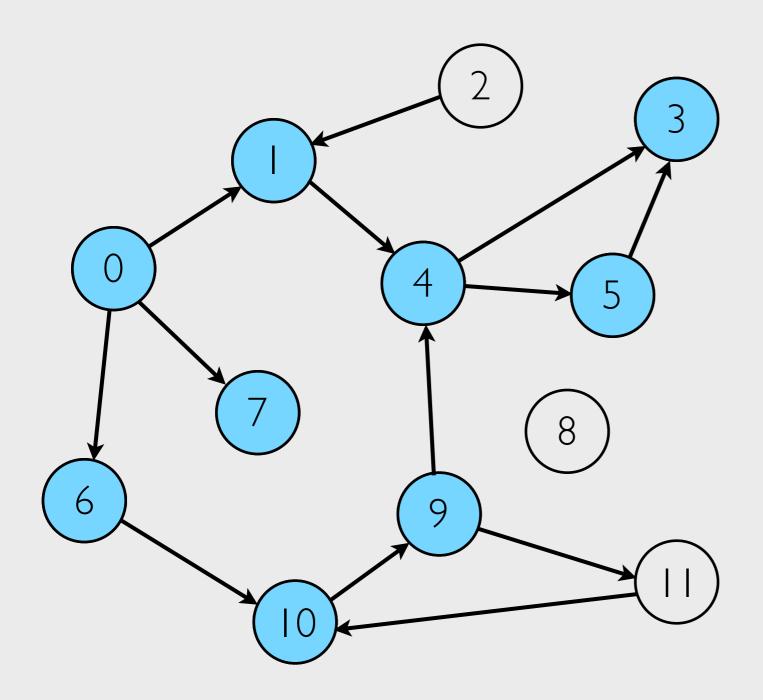


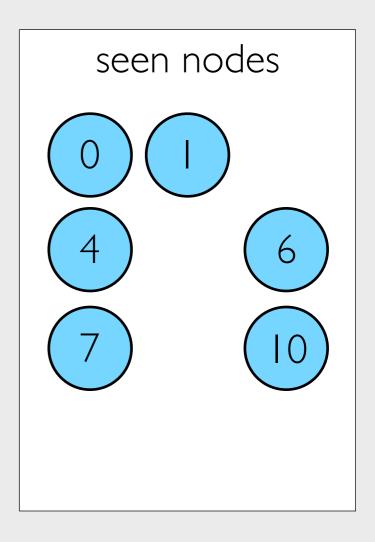


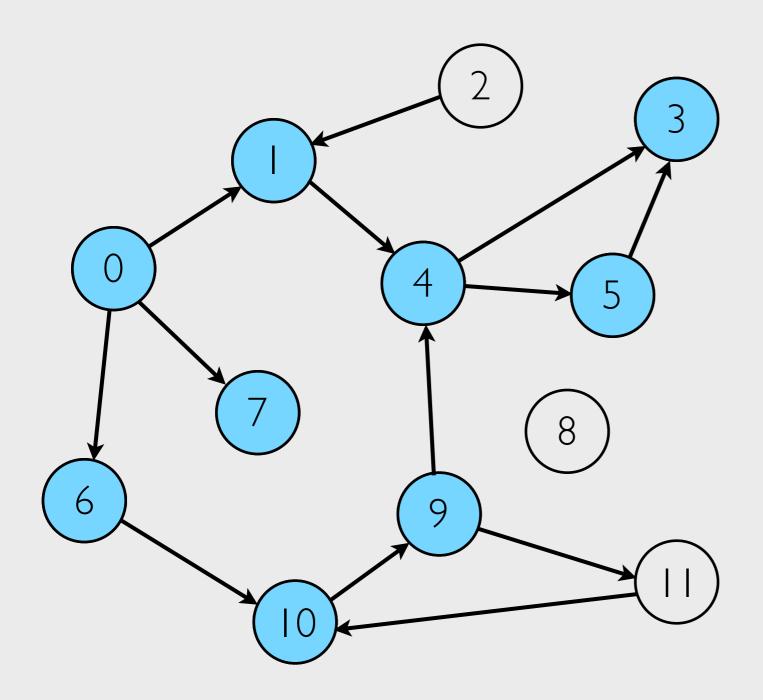


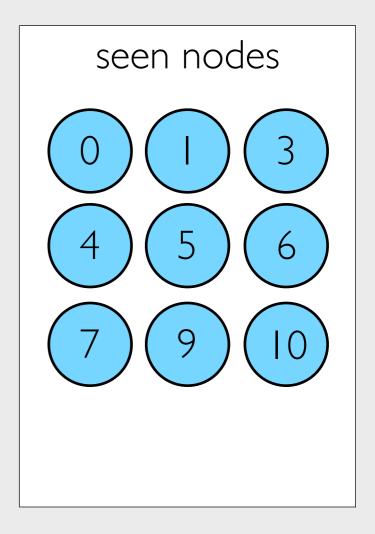


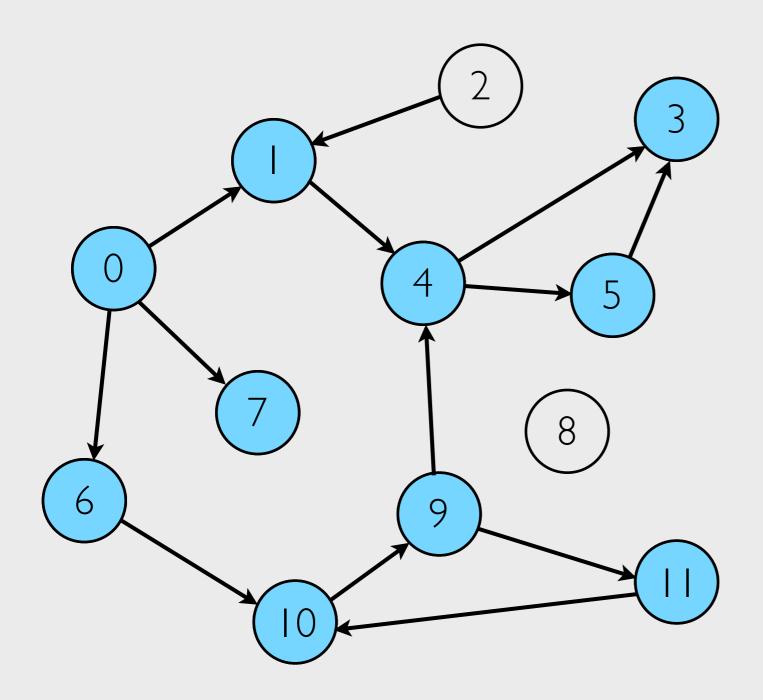


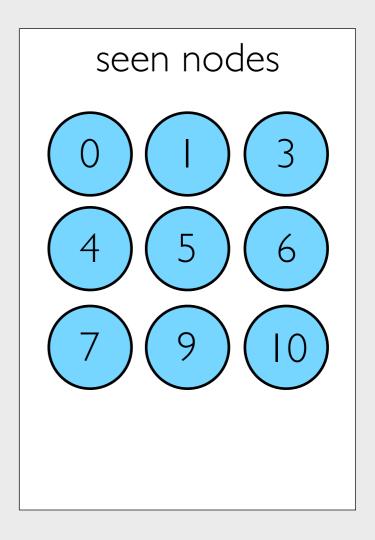


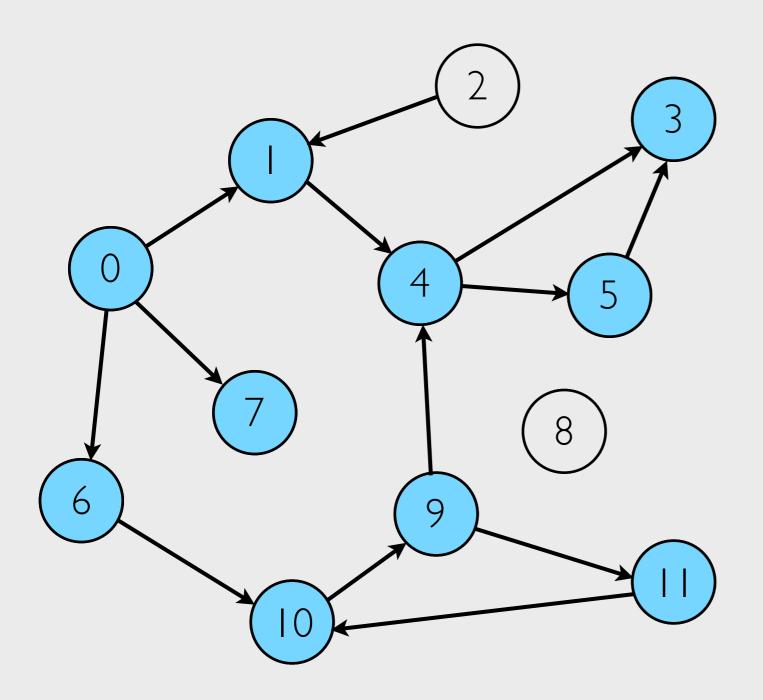


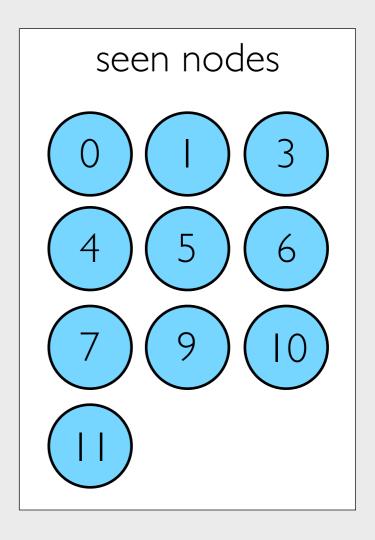




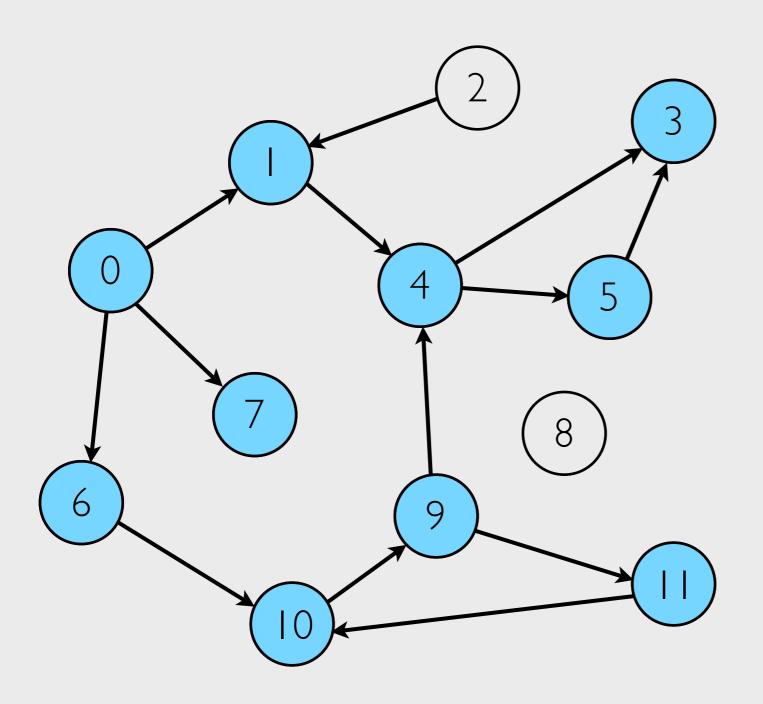


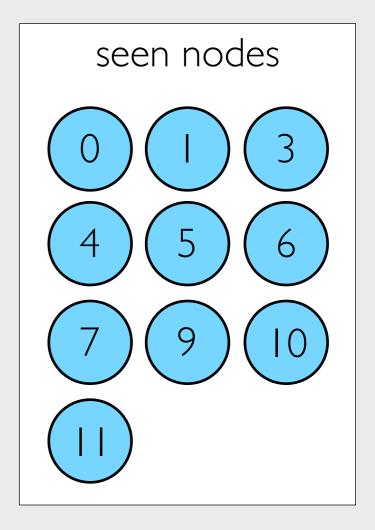




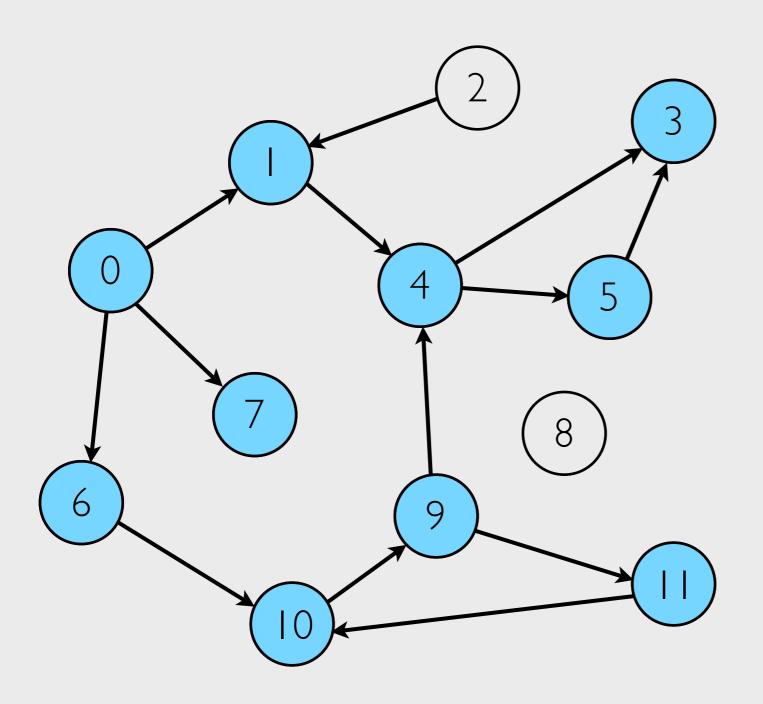


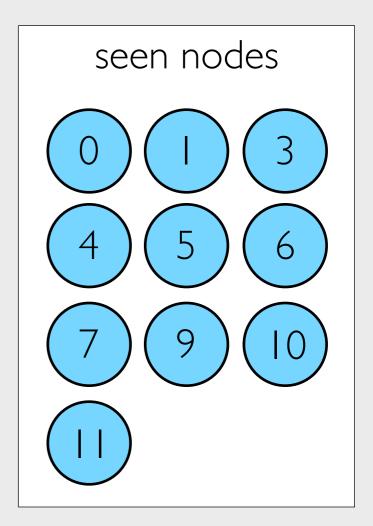
Events are updates that change an LVar's state





Events are updates that change an LVar's state Event handlers listen for events and launch callbacks in response

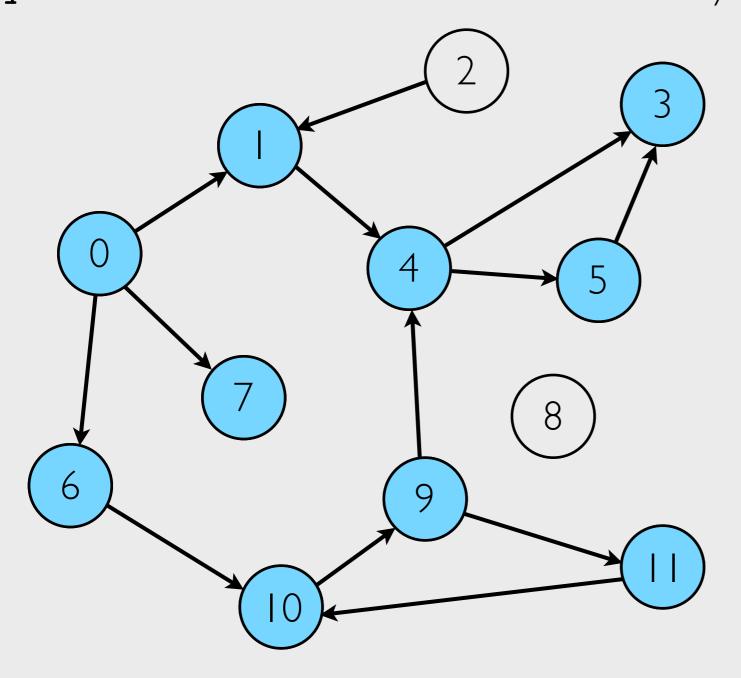


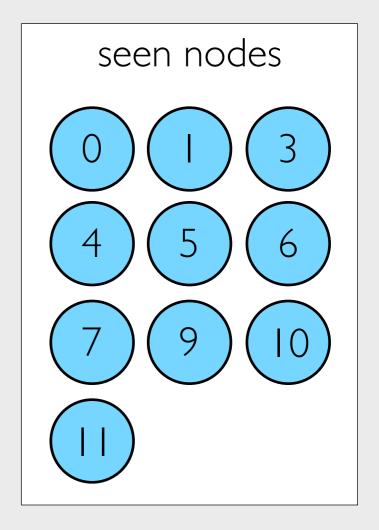


Events are updates that change an LVar's state

Event handlers listen for events and launch callbacks in response

quiesce blocks until all callbacks launched by a given handler are done running

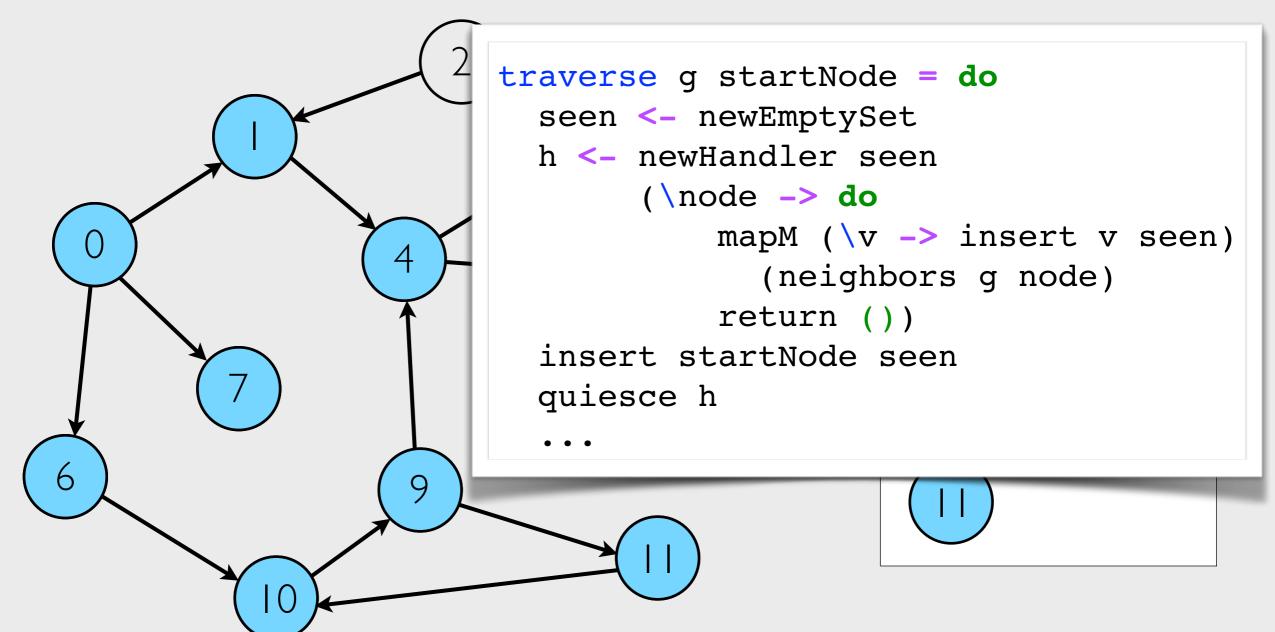




Events are updates that change an LVar's state

Event handlers listen for events and launch callbacks in response

quiesce blocks until all callbacks launched by a given handler are done running



Attempts to write to a frozen LVar raise a write-after-freeze exception

Attempts to write to a frozen LVar raise a write-after-freeze exception

```
Theorem 1 (Quasi-Determinism). If \sigma \hookrightarrow^* \sigma' and \sigma \hookrightarrow^* \sigma'', and neither \sigma' nor \sigma'' can take a step, then either:

1. \sigma' = \sigma'' up to a permutation on locations \pi, or
2. \sigma' = \text{error} or \sigma'' = \text{error}.

[POPL'14] Insert v seen)

Theorem 1 (Quasi-Determinism). If \sigma \hookrightarrow^* \sigma' and \sigma \hookrightarrow^* \sigma'', insert v seen)

Theorem 1 (Quasi-Determinism). If \sigma \hookrightarrow^* \sigma' and \sigma \hookrightarrow^* \sigma'', insert v seen)

Theorem 1 (Quasi-Determinism). If \sigma \hookrightarrow^* \sigma' and \sigma \hookrightarrow^* \sigma'', insert v seen)

Theorem 1 (Quasi-Determinism). If \sigma \hookrightarrow^* \sigma' and \sigma \hookrightarrow^* \sigma'', insert v seen)

Theorem 1 (Quasi-Determinism). If \sigma \hookrightarrow^* \sigma' and \sigma \hookrightarrow^* \sigma'', insert v seen)

Theorem 1 (Quasi-Determinism). If \sigma \hookrightarrow^* \sigma' and \sigma \hookrightarrow^* \sigma'', insert v seen)

Theorem 2 (Quasi-Determinism). If \sigma \hookrightarrow^* \sigma' and \sigma \hookrightarrow^* \sigma'', insert v seen)

Theorem 3 (Quasi-Determinism). If \sigma \hookrightarrow^* \sigma' and \sigma \hookrightarrow^* \sigma'', insert v seen)

Theorem 3 (Quasi-Determinism). If \sigma \hookrightarrow^* \sigma' and \sigma \hookrightarrow^* \sigma'', insert v seen)

Theorem 4 (Quasi-Determinism). If \sigma \hookrightarrow^* \sigma' and \sigma \hookrightarrow^* \sigma'', insert v seen)
```

```
Theorem 1 (Quasi-Determinism). If \sigma \hookrightarrow^* \sigma' and \sigma \hookrightarrow^* \sigma'', do and neither \sigma' nor \sigma'' can take a step, then either:

1. \sigma' = \sigma'' up to a permutation on locations \pi, or
2. \sigma' = \text{error } \sigma \sigma'' = \text{error}.

[POPL'14] Insert v seen)

g node)

return ())

insert startNode seen

quiesce h

freeze seen
```

```
Theorem 1 (Quasi-Determinism). If \sigma \hookrightarrow^* \sigma' and \sigma \hookrightarrow^* \sigma'', and neither \sigma' nor \sigma'' can take a step, then either:

1. \sigma' = \sigma'' up to a permutation on locations \pi, or
2. \sigma' = \text{error } \sigma \sigma'' = \text{error}.

[POPL'14] Insert v seen)

[(Book,1),(Shoes,1)] insert startNode seen

[Quasi-Determinism). If \sigma \hookrightarrow^* \sigma' and \sigma \hookrightarrow^* \sigma'', in sert v seen)

[(Book,1),(Shoes,1)]
```

```
Theorem 1 (Quasi-Determinism). If \sigma \hookrightarrow^* \sigma' and \sigma \hookrightarrow^* \sigma'', and neither \sigma' nor \sigma'' can take a step, then either:

1. \sigma' = \sigma'' up to a permutation on locations \pi, or
2. \sigma' = \text{error } \text{or } \sigma'' = \text{error}.

[POPL'14] Insert v seen g node)

return ())

insert startNode seen

[B 1)]

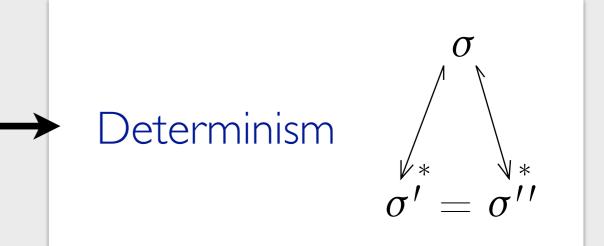
[CBook,1),(Shoes,1)] or error.
```

Determinism σ σ \star^* $\sigma'=\sigma''$

[POPL'14]

Independence

$$\frac{\langle S; e \rangle \hookrightarrow \langle S'; e' \rangle}{\langle S \sqcup_S S''; e \rangle \hookrightarrow \langle S' \sqcup_S S''; e' \rangle}$$



[POPL '14]

Independence

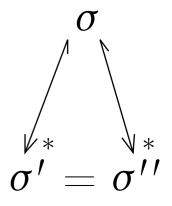
$$\frac{\langle S; e \rangle \longleftrightarrow \langle S'; e' \rangle}{\langle S \sqcup_S S''; e \rangle \longleftrightarrow \langle S' \sqcup_S S''; e' \rangle}$$

[O'Hearn et al., 2001]

Frame rule

$$\frac{\{p\}\ c\ \{q\}}{\{p*r\}\ c\ \{q*r\}}$$

Determinism

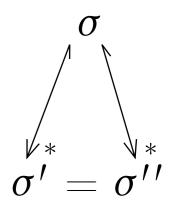


[POPL '14]

Independence

$$\frac{\langle S; e \rangle \hookrightarrow \langle S'; e' \rangle}{\langle S \sqcup_S S''; e \rangle \hookrightarrow \langle S' \sqcup_S S''; e' \rangle}$$

Determinism



[O'Hearn et al., 2001]

Frame rule

$$\frac{\{p\}\ c\ \{q\}}{\{p*r\}\ c\ \{q*r\}}$$

4.3 The Frame Problem

In the last section of part 3, in proving that one person could get into conversation with another, we were obliged to add the hypothesis that if a person has a telephone he still has it after looking up a number in the telephone book.

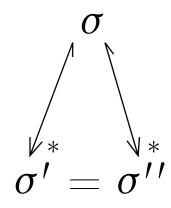
[McCarthy and Hayes, 1969]

[POPL '14]

Independence

$$\frac{\langle S; e \rangle \hookrightarrow \langle S'; e' \rangle}{\langle S \sqcup_S S''; e \rangle \hookrightarrow \langle S' \sqcup_S S''; e' \rangle}$$

Determinism



[O'Hearn et al., 2001]

Frame rule

$$\frac{\{p\}\ c\ \{q\}}{\{p*r\}\ c\ \{q*r\}}$$

4.3 The Frame Problem

In the last section of part 3, in proving that one person could get into conversation with another, we were obliged to add the hypothesis that if a person has a telephone he still has it after looking up a number in the telephone book.

[McCarthy and Hayes, 1969]

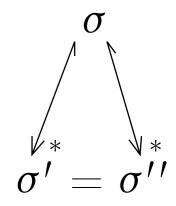




Independence
$$\langle S; e \rangle \hookrightarrow \langle S'; e' \rangle$$

$$\overline{\langle S \sqcup_S S''; e \rangle} \hookrightarrow \langle S' \sqcup_S S''; e' \rangle$$

Determinism



[O'Hearn et al., 2001]

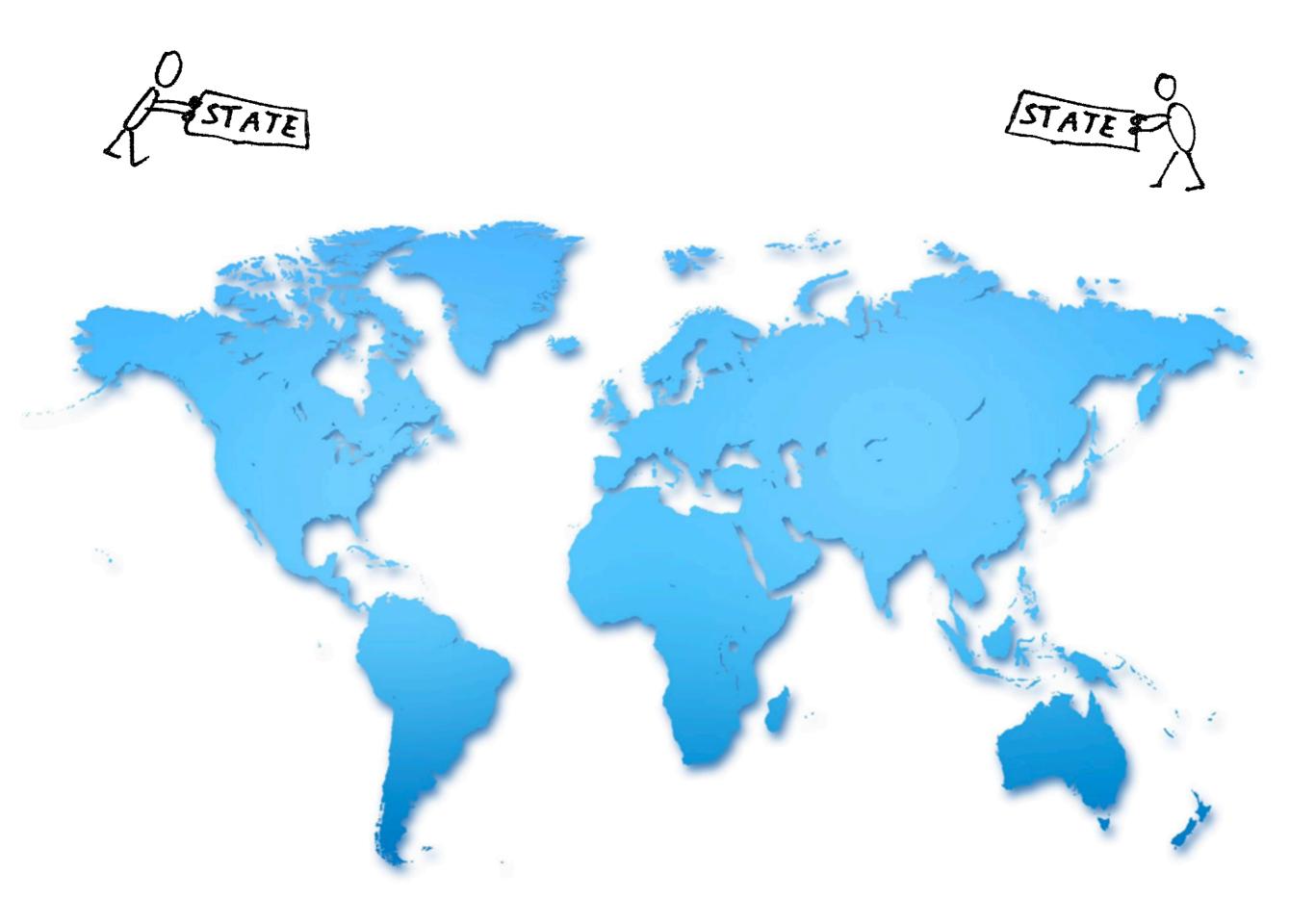
Frame rule

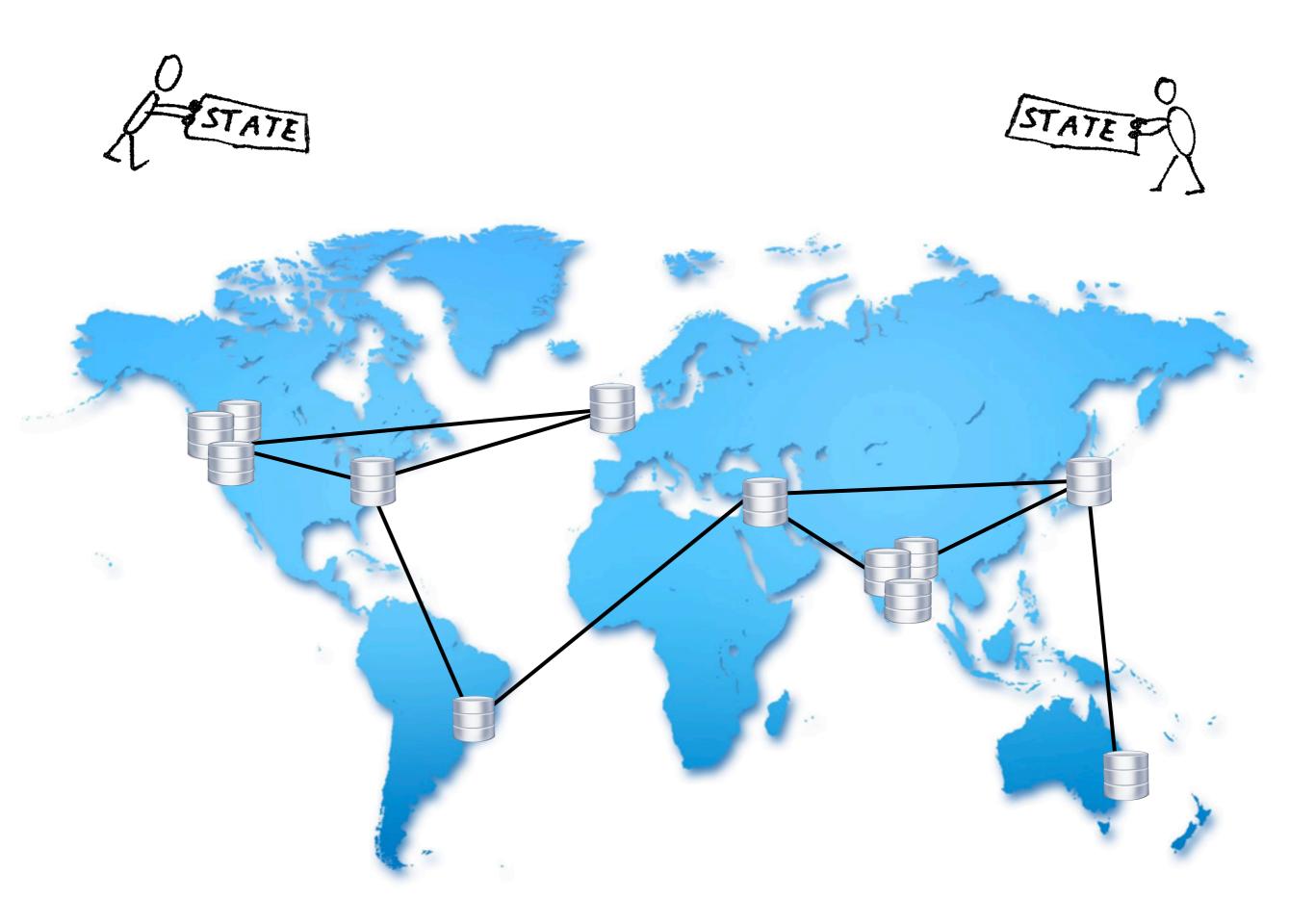
$$\frac{\{p\}\ c\ \{q\}}{\{p*r\}\ c\ \{q*r\}}$$

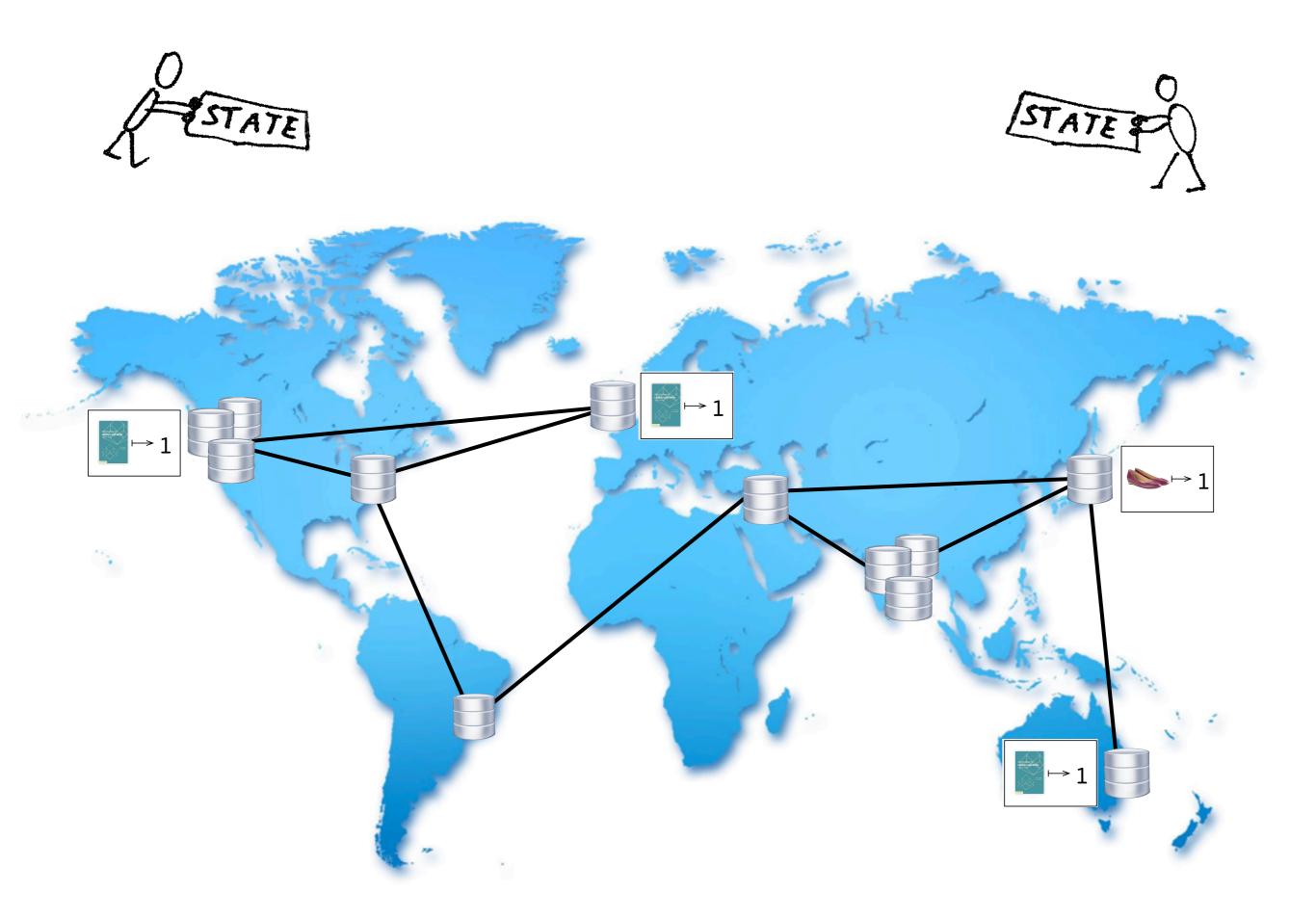
The Frame Problem 4.3

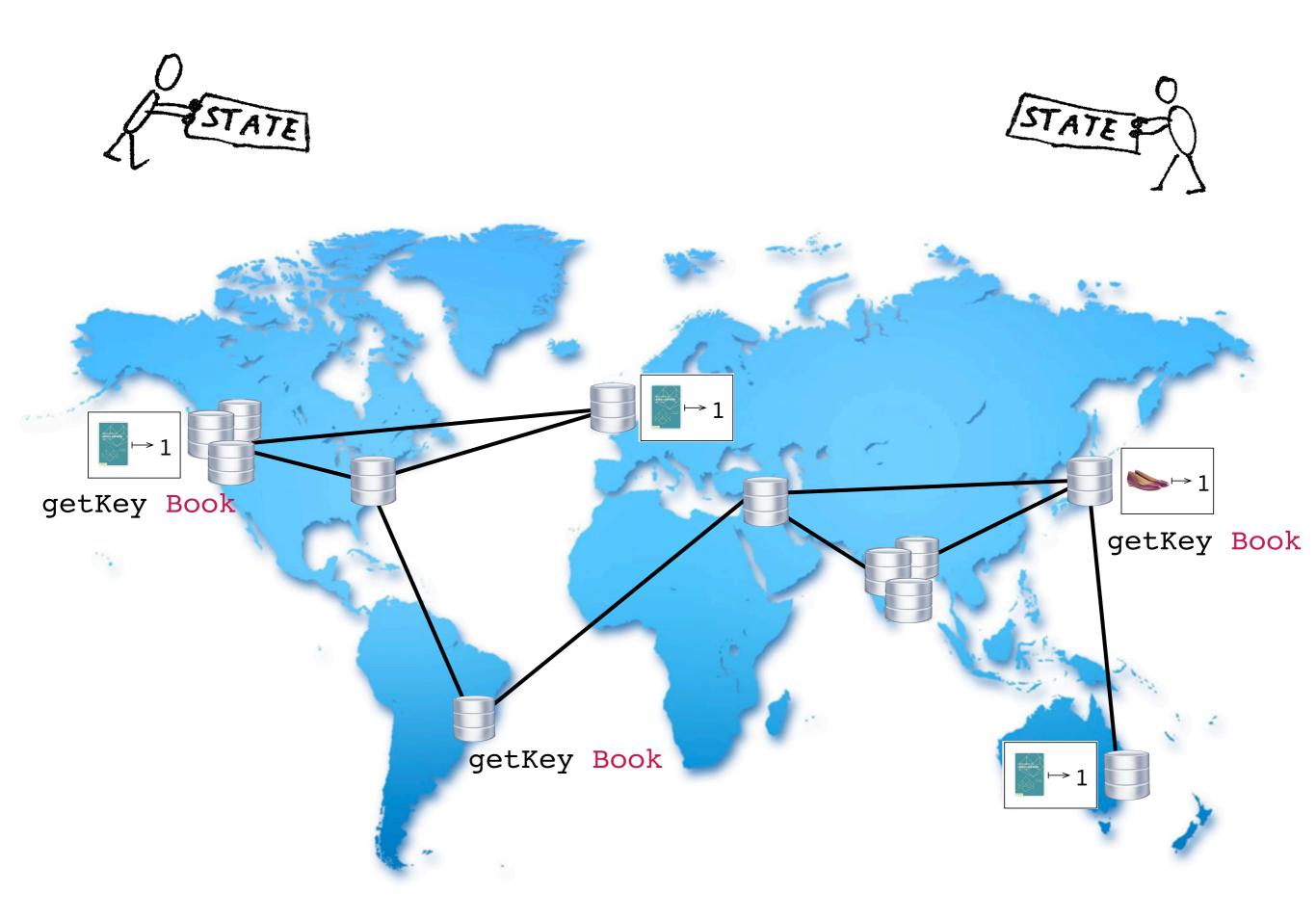
In the last section of part 3, in proving that one person could get into conversation with another, we were obliged to add the hypothesis that if a person has a telephone he still has it after looking up a number in the telephone book.

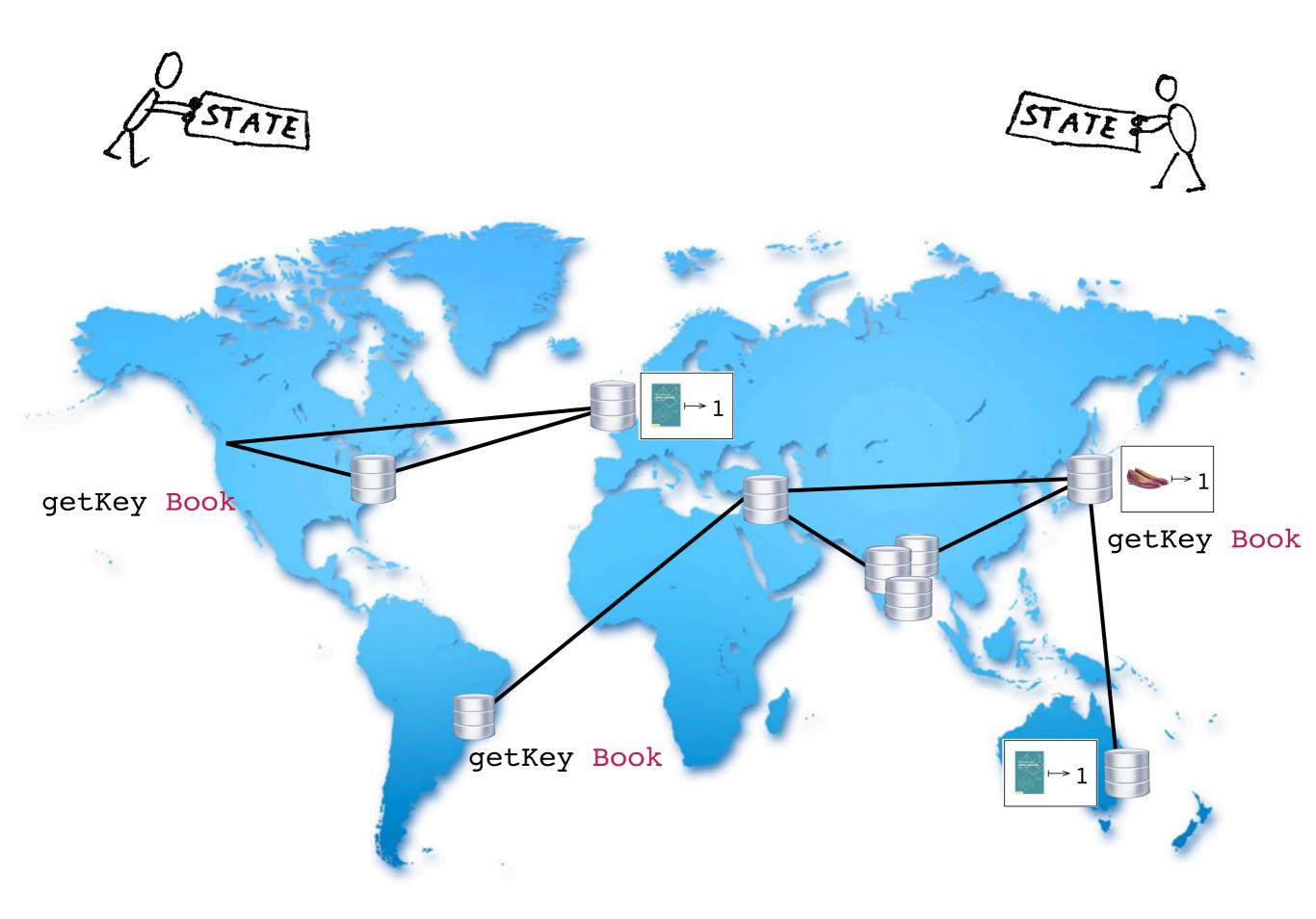
[McCarthy and Hayes, 1969]

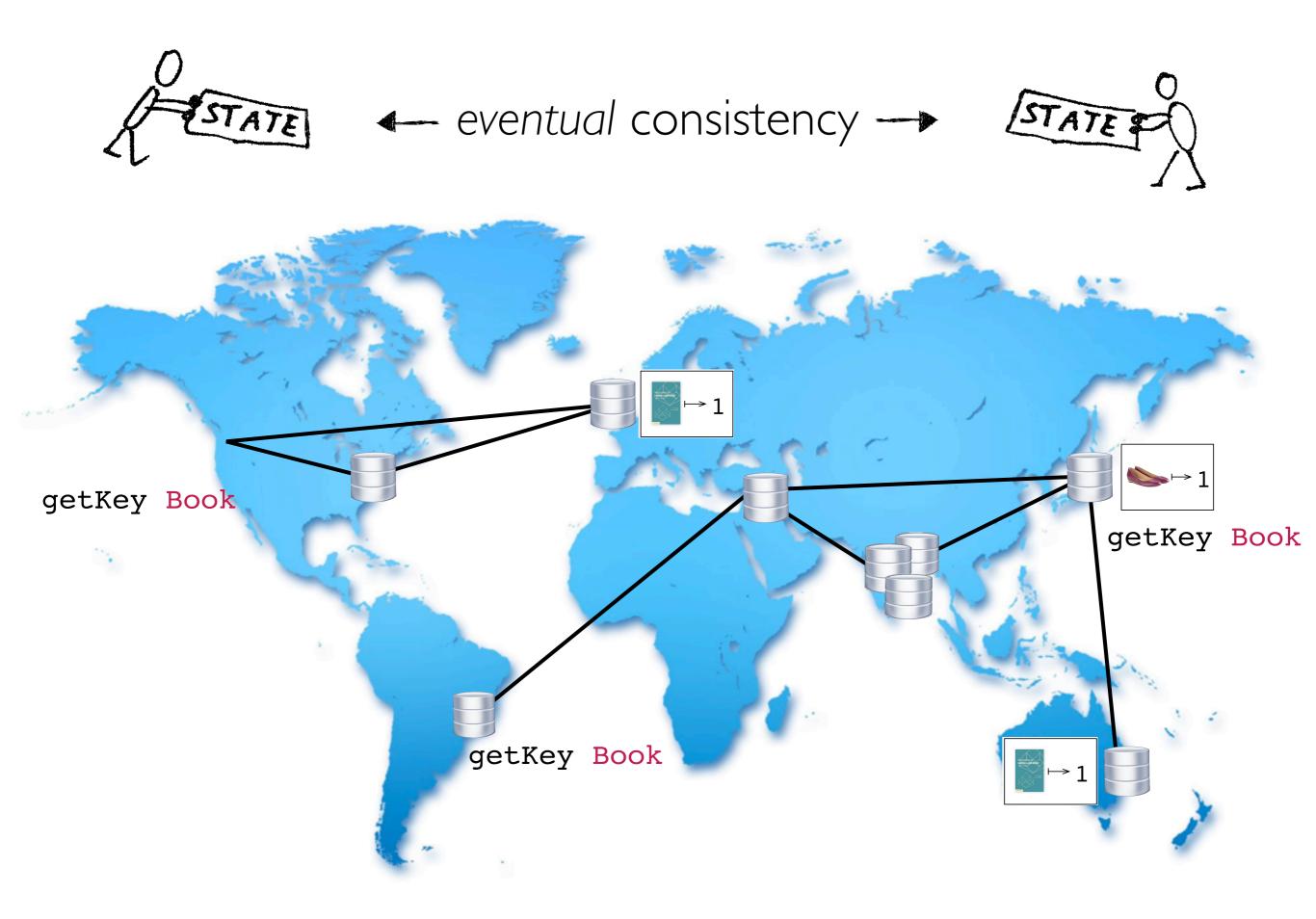












Dynamo: Amazon's Highly Available Key-value Store

Giuseppe DeCandia, Deniz Hastorun, Madan Jampani, Gunavardhan Kakulapati, Avinash Lakshman, Alex Pilchin, Swaminathan Sivasubramanian, Peter Vosshall and Werner Vogels

Amazon.com

ABSTRACT

Reliability at massive scale is one of the biggest challenges we face at Amazon.com, one of the largest e-commerce operations in the world; even the slightest outage has significant financial consequences and impacts customer trust. The Amazon.com platform, which provides services for many web sites worldwide, is implemented on top of an infrastructure of tens of thousands of servers and network components located in many datacenters around the world. At this scale, small and large components fail continuously and the way persistent state is managed in the face of these failures drives the reliability and scalability of the software systems.

This paper presents the design and implementation of Dynamo, a highly available key-value storage system that some of Amazon's core services use to provide an "always-on" experience. To achieve this level of availability, Dynamo sacrifices consistency under certain failure scenarios. It makes extensive use of object versioning and application-assisted conflict resolution in a manner that provides a novel interface for developers to use.

Categories and Subject Descriptors

D.4.2 [Operating Systems]: Storage Management; D.4.5 [Operating Systems]: Reliability; D.4.2 [Operating Systems]: Performance;

General Terms

Algorithms, Management, Measurement, Performance, Design, Reliability.

1. INTRODUCTION

Amazon runs a world-wide e-commerce platform that serves tens of millions customers at peak times using tens of thousands of servers located in many data centers around the world. There are strict operational requirements on Amazon's platform in terms of performance, reliability and efficiency, and to support continuous growth the platform needs to be highly scalable. Reliability is one of the most important requirements because even the slightest outage has significant financial consequences and impacts customer trust. In addition, to support continuous growth, the platform needs to be highly scalable.

Permission to make digital or hard copies of all or part of this work for personal or classroom use is granted without fee provided that copies are not made or distributed for profit or commercial advantage and that copies bear this notice and the full citation on the first page. To copy otherwise, or republish, to post on servers or to redistribute to lists, requires prior specific permission and/or a fee.

SOSP'07, October 14–17, 2007, Stevenson, Washington, USA. Copyright 2007 ACM 978-1-59593-591-5/07/0010...\$5.00. One of the lessons our organization has learned from operating Amazon's platform is that the reliability and scalability of a system is dependent on how its application state is managed. Amazon uses a highly decentralized, loosely coupled, service oriented architecture consisting of hundreds of services. In this environment there is a particular need for storage technologies that are always available. For example, customers should be able to view and add items to their shopping cart even if disks are failing, network routes are flapping, or data centers are being destroyed by tornados. Therefore, the service responsible for managing shopping carts requires that it can always write to and read from its data store, and that its data needs to be available across multiple data centers.

Dealing with failures in an infrastructure comprised of millions of components is our standard mode of operation; there are always a small but significant number of server and network components that are failing at any given time. As such Amazon's software systems need to be constructed in a manner that treats failure handling as the normal case without impacting availability or performance.

To meet the reliability and scaling needs, Amazon has developed a number of storage technologies, of which the Amazon Simple Storage Service (also available outside of Amazon and known as Amazon S3), is probably the best known. This paper presents the design and implementation of Dynamo, another highly available and scalable distributed data store built for Amazon's platform. Dynamo is used to manage the state of services that have very high reliability requirements and need tight control over the tradeoffs between availability, consistency, cost-effectiveness and performance. Amazon's platform has a very diverse set of applications with different storage requirements. A select set of applications requires a storage technology that is flexible enough to let application designers configure their data store appropriately based on these tradeoffs to achieve high availability and guaranteed performance in the most cost effective manner.

There are many services on Amazon's platform that only need primary-key access to a data store. For many services, such as those that provide best seller lists, shopping carts, customer preferences, session management, sales rank, and product catalog, the common pattern of using a relational database would lead to inefficiencies and limit scale and availability. Dynamo provides a simple primary-key only interface to meet the requirements of these applications.

Dynamo uses a synthesis of well known techniques to achieve scalability and availability: Data is partitioned and replicated using consistent hashing [10], and consistency is facilitated by object versioning [12]. The consistency among replicas during updates is maintained by a quorum-like technique and a decentralized replica synchronization protocol. Dynamo employs

Dynamo: Amazon's Highly Available Key-value Store

Giuseppe DeCandia, Deniz Hastorun, Madan Jampani, Gunavardhan Kakulapati, Avinash Lakshman, Alex Pilchin, Swaminathan Sivasubramanian, Peter Vosshall and Werner Vogels

Amazon.com

ABSTRACT

Reliability at massive scale is one of the biggest challenges we face at Amazon.com, one of the largest e-commerce operations in the world; even the slightest outage has significant financial consequences and impacts customer trust. The Amazon.com platform, which provides services for many web sites worldwide, is implemented on top of an infrastructure of tens of thousands of servers and network components located in many datacenters around the world. At this scale, small and large components fail continuously and the way persistent state is managed in the face of these failures drives the reliability and scalability of the software systems.

This paper presents the design and implementation of Dynamo, a highly available key-value storage system that some of Amazon's core services use to provide an "always-on" experience. To achieve this level of availability, Dynamo sacrifices consistency under certain failure scenarios. It makes extensive use of object versioning and application-assisted conflict resolution in a manner that provides a novel interface for developers to use.

Categories and Subject Descriptors

D.4.2 [Operating Systems]: Storage Management; D.4.5 [Operating Systems]: Reliability; D.4.2 [Operating Systems]: Performance;

General Terms

Algorithms, Management, Measurement, Performance, Design, Reliability.

One of the lessons our organization has learned from operating Amazon's platform is that the reliability and scalability of a system is dependent on how its application state is managed. Amazon uses a highly decentralized, loosely coupled, service oriented architecture consisting of hundreds of services. In this environment there is a particular need for storage technologies that are always available. For example, customers should be able to view and add items to their shopping cart even if disks are failing, network routes are flapping, or data centers are being destroyed by tornados. Therefore, the service responsible for managing shopping carts requires that it can always write to and read from its data store, and that its data needs to be available across multiple data centers.

Dealing with failures in an infrastructure comprised of millions of components is our standard mode of operation; there are always a small but significant number of server and network components that are failing at any given time. As such Amazon's software systems need to be constructed in a manner that treats failure handling as the normal case without impacting availability or performance.

To meet the reliability and scaling needs, Amazon has developed a number of storage technologies, of which the Amazon Simple Storage Service (also available outside of Amazon and known as Amazon S3), is probably the best known. This paper presents the design and implementation of Dynamo, another highly available and scalable distributed data store built for Amazon's platform. Dynamo is used to manage the state of services that have very high reliability requirements and need tight control over the

m has a very diverse set of e requirements. A select set of chnology that is flexible enough gure their data store appropriately achieve high availability and nost cost effective manner.

azon's platform that only need re. For many services, such as iists, shopping carts, customer , sales rank, and product catalog, elational database would lead to availability. Dynamo provides a see to meet the requirements of

known techniques to achieve is partitioned and replicated d consistency is facilitated by sistency among replicas during uorum-like technique and a on protocol. Dynamo employs

since the application is aware of the data schema it can decide on the conflict resolution method that is best suited for its client's experience. For instance, the application that maintains customer shopping carts can choose to "merge" the conflicting versions and return a single unified shopping cart.

Conflict-Free Replicated Data Types*

Marc Shapiro^{1,5}, Nuno Preguiça^{1,2}, Carlos Baquero³, and Marek Zawirski^{1,4}

INRIA, Paris, France
 CITI, Universidade Nova de Lisboa, Portugal
 Universidade do Minho, Portugal
 UPMC, Paris, France
 LIP6, Paris, France

Abstract. Replicating data under Eventual Consistency (EC) allows any replica to accept updates without remote synchronisation. This ensures performance and scalability in large-scale distributed systems (e.g., clouds). However, published EC approaches are ad-hoc and error-prone. Under a formal Strong Eventual Consistency (SEC) model, we study sufficient conditions for convergence. A data type that satisfies these conditions is called a Conflict-free Replicated Data Type (CRDT). Replicas of any CRDT are guaranteed to converge in a self-stabilising manner, despite any number of failures. This paper formalises two popular approaches (state- and operation-based) and their relevant sufficient conditions. We study a number of useful CRDTs, such as sets with clean semantics, supporting both add and remove operations, and consider in depth the more complex Graph data type. CRDT types can be composed to develop large-scale distributed applications, and have interesting theoretical properties.

Keywords: Eventual Consistency, Replicated Shared Objects, Large-Scale Distributed Systems.

1 Introduction

Replication and consistency are essential features of any large distributed system, such as the WWW, peer-to-peer, or cloud computing platforms. The standard "strong consistency" approach serialises updates in a global total order [10]. This constitutes a performance and scalability bottleneck. Furthermore, strong consistency conflicts with availability and partition-tolerance [8].

When network delays are large or partitioning is an issue, as in delay-tolerant networks, disconnected operation, cloud computing, or P2P systems, eventual consistency promises better availability and performance [17]21]. An update executes at some replica, without synchronisation; later, it is sent to the other

Dynamo: Amazon's Highly Available Key-value Store

Giuseppe DeCandia, Deniz Hastorun, Madan Jampani, Gunavardhan Kakulapati, Avinash Lakshman, Alex Pilchin, Swaminathan Sivasubramanian, Peter Vosshall and Werner Vogels

Amazon.com

ABSTRACT

Reliability at massive scale is one of the biggest challenges we face at Amazon.com, one of the largest e-commerce operations in the world; even the slightest outage has significant financial consequences and impacts customer trust. The Amazon.com platform, which provides services for many web sites worldwide, is implemented on top of an infrastructure of tens of thousands of servers and network components located in many datacenters around the world. At this scale, small and large components fail continuously and the way persistent state is managed in the face of these failures drives the reliability and scalability of the software systems.

This paper presents the design and implementation of Dynamo, a highly available key-value storage system that some of Amazon's core services use to provide an "always-on" experience. To achieve this level of availability, Dynamo sacrifices consistency under certain failure scenarios. It makes extensive use of object versioning and application-assisted conflict resolution in a manner that provides a novel interface for developers to use.

Categories and Subject Descriptors

D.4.2 [Operating Systems]: Storage Management; D.4.5 [Operating Systems]: Reliability; D.4.2 [Operating Systems]: Performance;

General Terms

Algorithms, Management, Measurement, Performance, Design, Reliability.

One of the lessons our organization has learned from operating Amazon's platform is that the reliability and scalability of a system is dependent on how its application state is managed. Amazon uses a highly decentralized, loosely coupled, service oriented architecture consisting of hundreds of services. In this environment there is a particular need for storage technologies that are always available. For example, customers should be able to view and add items to their shopping cart even if disks are failing, network routes are flapping, or data centers are being destroyed by tornados. Therefore, the service responsible for managing shopping carts requires that it can always write to and read from its data store, and that its data needs to be available across multiple data centers.

Dealing with failures in an infrastructure comprised of millions of components is our standard mode of operation; there are always a small but significant number of server and network components that are failing at any given time. As such Amazon's software systems need to be constructed in a manner that treats failure handling as the normal case without impacting availability or performance.

To meet the reliability and scaling needs, Amazon has developed a number of storage technologies, of which the Amazon Simple Storage Service (also available outside of Amazon and known as Amazon S3), is probably the best known. This paper presents the design and implementation of Dynamo, another highly available and scalable distributed data store built for Amazon's platform. Dynamo is used to manage the state of services that have very high reliability requirements and need tight control over the

m has a very diverse set of e requirements. A select set of chnology that is flexible enough gure their data store appropriately achieve high availability and nost cost effective manner.

azon's platform that only need re. For many services, such as sists, shopping carts, customer sales rank, and product catalog, elational database would lead to availability. Dynamo provides a se to meet the requirements of

known techniques to achieve is partitioned and replicated d consistency is facilitated by sistency among replicas during uorum-like technique and a non protocol. Dynamo employs

n is aware of the data schema it n method that is best suited for the application that maintains ose to "merge" the conflicting ed shopping cart.

[Shapiro et al., SSS '11]

Conflict-Free Replicated Data Types*

Marc Shapiro^{1,5}, Nuno Preguiça^{1,2}, Carlos Baquero³, and Marek Zawirski^{1,4}

INRIA, Paris, France
 CITI, Universidade Nova de Lisboa, Portugal
 Universidade do Minho, Portugal
 UPMC, Paris, France
 LIP6, Paris, France

Abstract. Replicating data under Eventual Consistency (EC) allows any replica to accept updates without remote synchronisation. This ensures performance and scalability in large-scale distributed systems (e.g., clouds). However, published EC approaches are ad-hoc and error-prone. Under a formal Strong Eventual Consistency (SEC) model, we study sufficient conditions for convergence. A data type that satisfies these conditions is called a Conflict-free Replicated Data Type (CRDT). Replicas of any CRDT are guaranteed to converge in a self-stabilising manner, despite any number of failures. This paper formalises two popular approaches (state- and operation-based) and their relevant sufficient conditions. We study a number of useful CRDTs, such as sets with clean semantics, supporting both add and remove operations, and consider in depth the more complex Graph data type. CRDT types can be composed to develop large-scale distributed applications, and have interesting theoretical properties.

Keywords: Eventual Consistency, Replicated Shared Objects, Large-Scale Distributed Systems.

1 Introduction

Replication and consistency are essential features of any large distributed system, such as the WWW, peer-to-peer, or cloud computing platforms. The standard "strong consistency" approach serialises updates in a global total order [10]. This constitutes a performance and scalability bottleneck. Furthermore, strong consistency conflicts with availability and partition-tolerance [8].

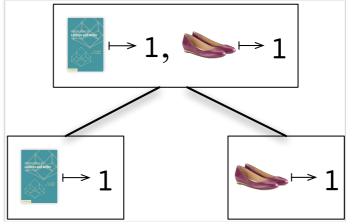
When network delays are large or partitioning is an issue, as in delay-tolerant networks, disconnected operation, cloud computing, or P2P systems, eventual consistency promises better availability and performance [17]21]. An update executes at some replica, without synchronisation; later, it is sent to the other

Dynamo: Amazon's Highly Available Key-value Store

Giuseppe DeCandia, Deniz Hastorun, Madan Jampani, Gunavardhan Kakulapati, Avinash Lakshman, Alex Pilchin, Swaminathan Sivasubramanian, Peter Vosshall and Werner Vogels

Amazon.com

ABSTRACT



D.4.2 [Operating Systems]: Storage Management; D.4.5 [Operating Systems]: Reliability; D.4.2 [Operating Systems]: Performance:

General Terms

Algorithms, Management, Measurement, Performance, Design, Reliability.

n is aware of the data schema it n method that is best suited for the application that maintains se to "merge" the conflicting ed shopping cart.

One of the lessons our organization has learned from operating Amazon's platform is that the reliability and scalability of a

azon spational is unat the remaining and scatability of a tem is dependent on how its application state is managed. azon uses a highly decentralized, loosely coupled, service ented architecture consisting of hundreds of services. In this ironment there is a particular need for storage technologies are always available. For example, customers should be able view and add items to their shopping cart even if disks are ing, network routes are flapping, or data centers are being troyed by tornados. Therefore, the service responsible for naging shopping carts requires that it can always write to and from its data store, and that its data needs to be available oss multiple data centers.

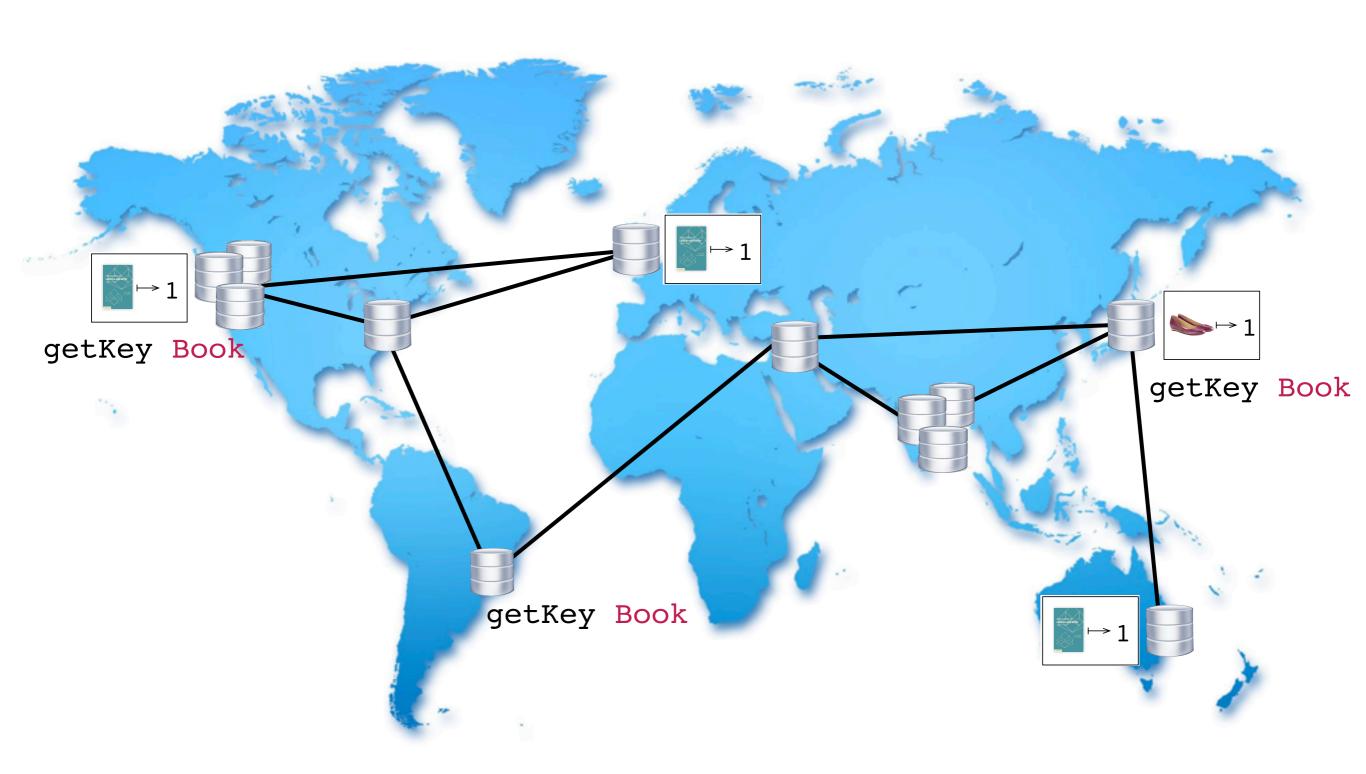
aling with failures in an infrastructure comprised of millions of nponents is our standard mode of operation; there are always a all but significant number of server and network components t are failing at any given time. As such Amazon's software tems need to be constructed in a manner that treats failure dling as the normal case without impacting availability or formance.

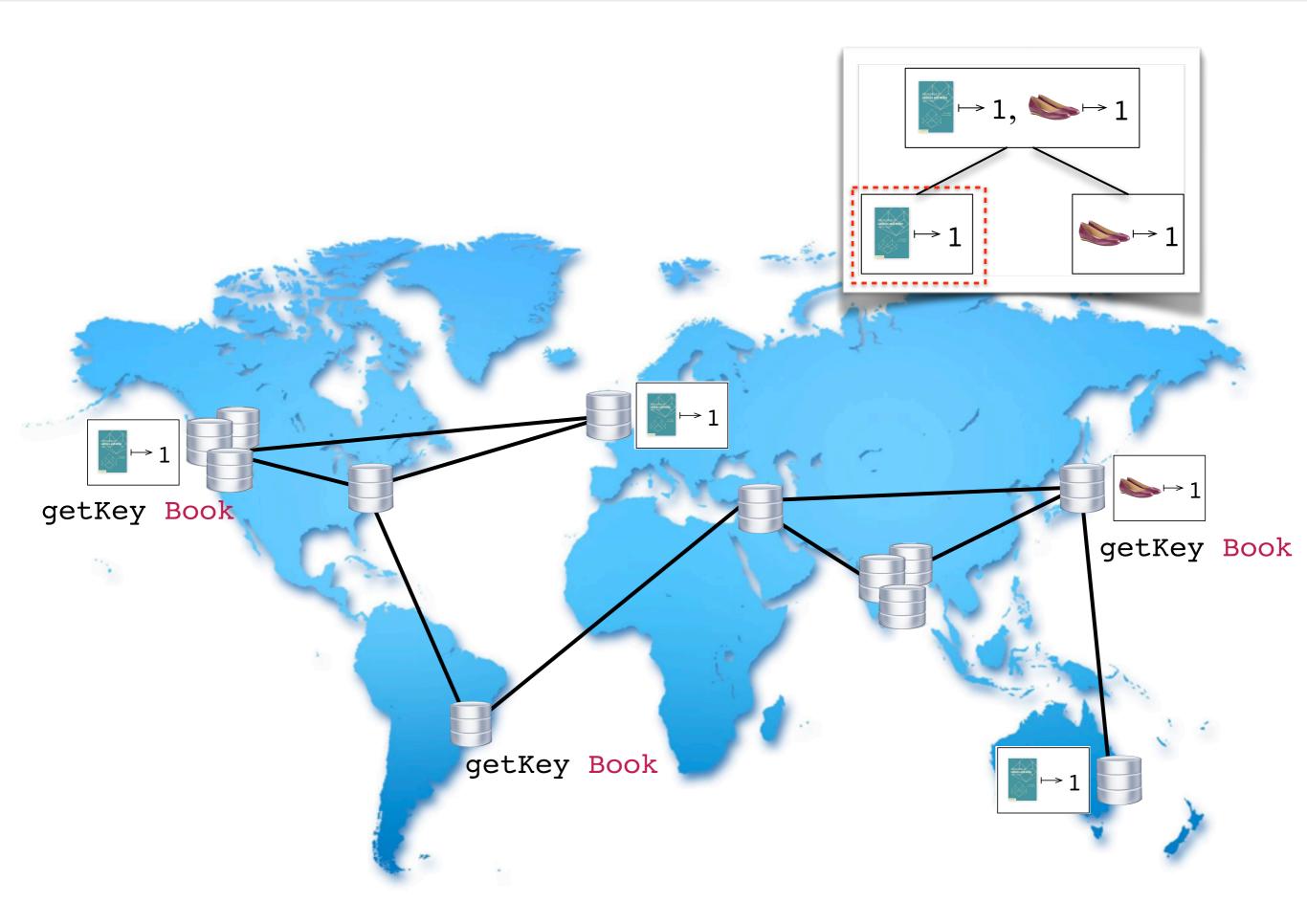
meet the reliability and scaling needs, Amazon has developed a number of storage technologies, of which the Amazon Simple Storage Service (also available outside of Amazon and known as Amazon S3), is probably the best known. This paper presents the design and implementation of Dynamo, another highly available and scalable distributed data store built for Amazon's platform. Dynamo is used to manage the state of services that have very high reliability requirements and need tight control over the

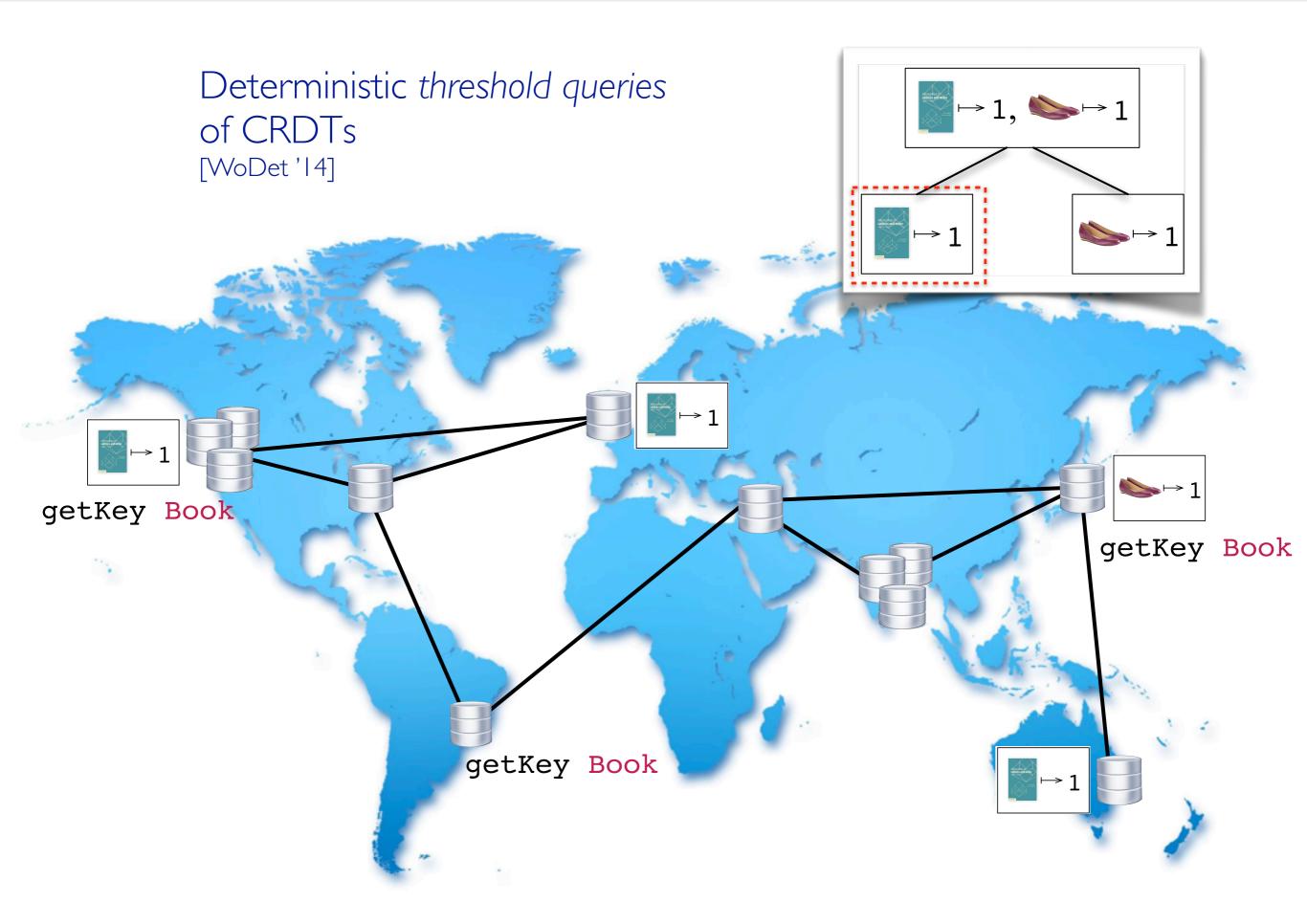
m has a very diverse set of e requirements. A select set of chnology that is flexible enough gure their data store appropriately achieve high availability and lost cost effective manner.

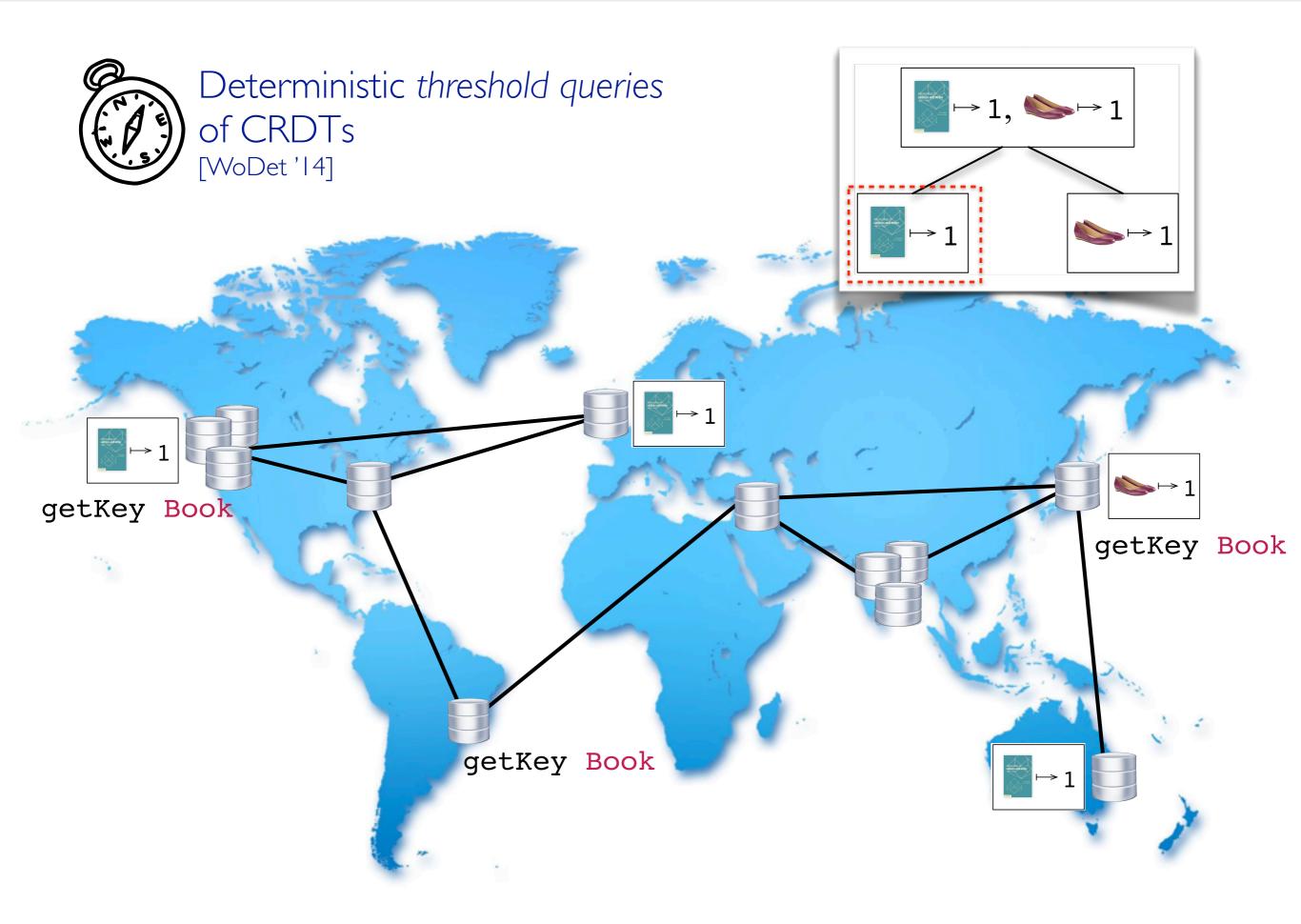
azon's platform that only need re. For many services, such as iists, shopping carts, customer , sales rank, and product catalog, elational database would lead to availability. Dynamo provides a se to meet the requirements of

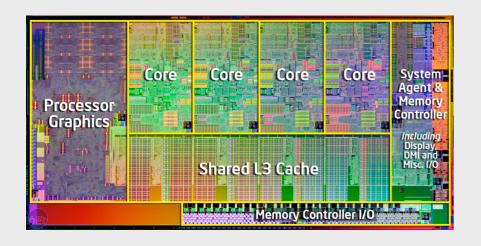
known techniques to achieve is partitioned and replicated d consistency is facilitated by sistency among replicas during uorum-like technique and a on protocol. Dynamo employs









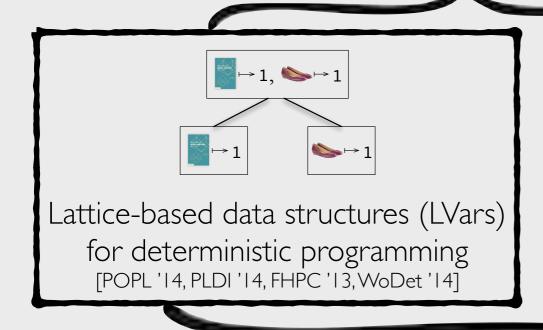




Parallel systems

Distributed systems

language-based approaches



Non-invasive DSLs for productive parallelism [ECOOP '17]

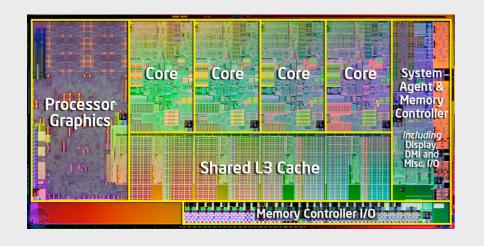


SMT-based verification of neural networks
[SysML'18]



Guiding principle:

Find the right high-level abstractions to enable efficient computation

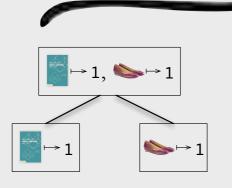




Parallel systems

Distributed systems

language-based approaches



Lattice-based data structures (LVars) for deterministic programming [POPL '14, PLDI '14, FHPC '13, WoDet '14]





SMT-based verification of neural networks
[SysML'18]

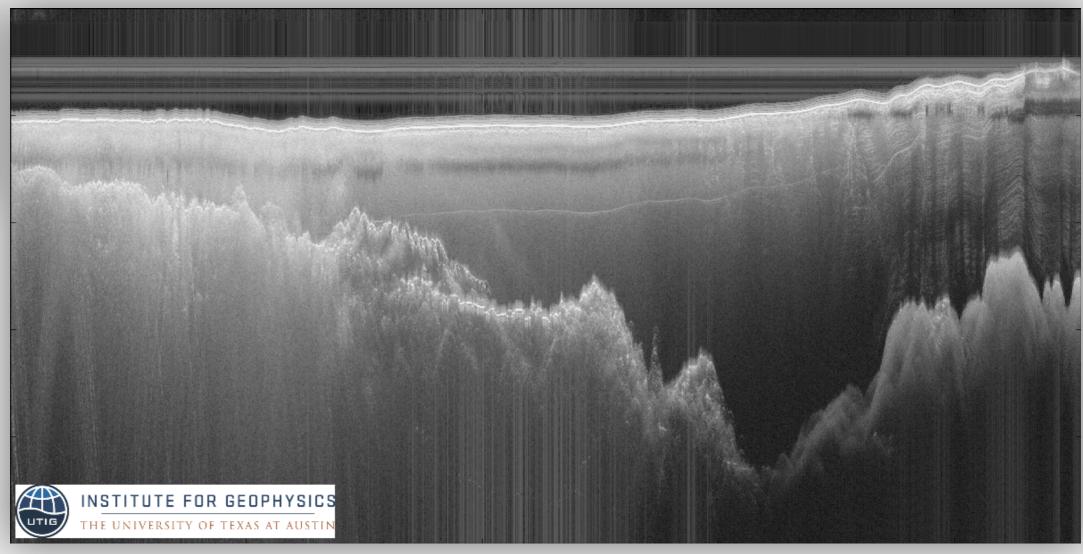


Guiding principle:

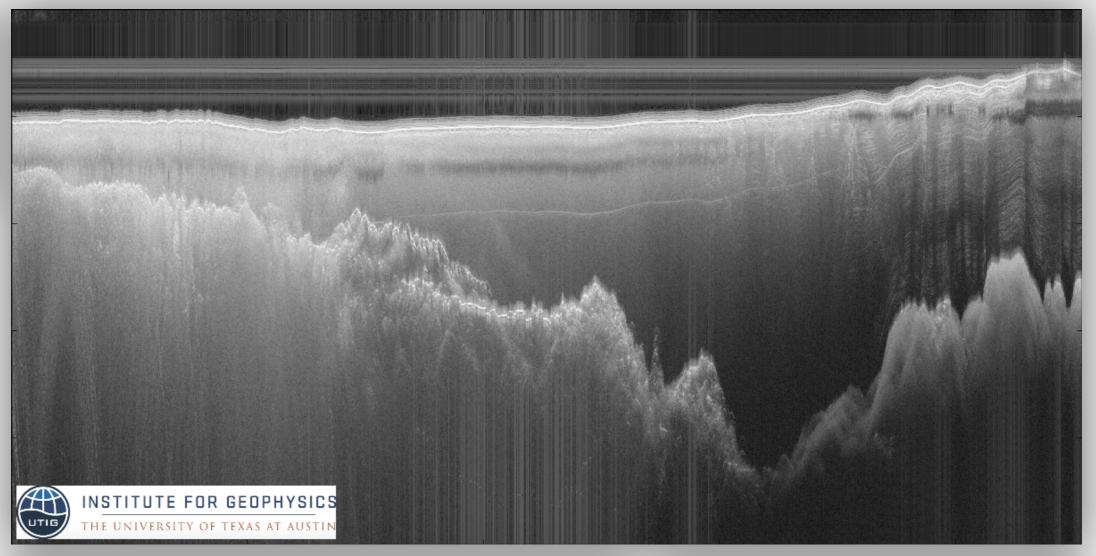
Find the right high-level abstractions to enable efficient computation

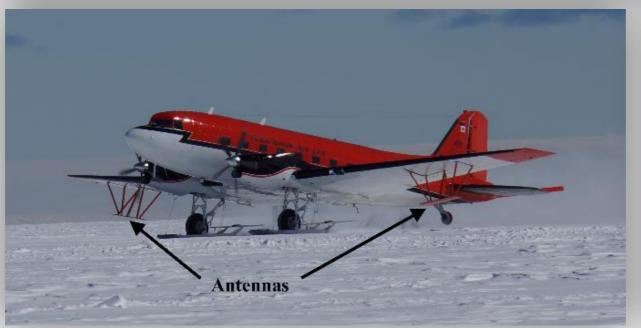








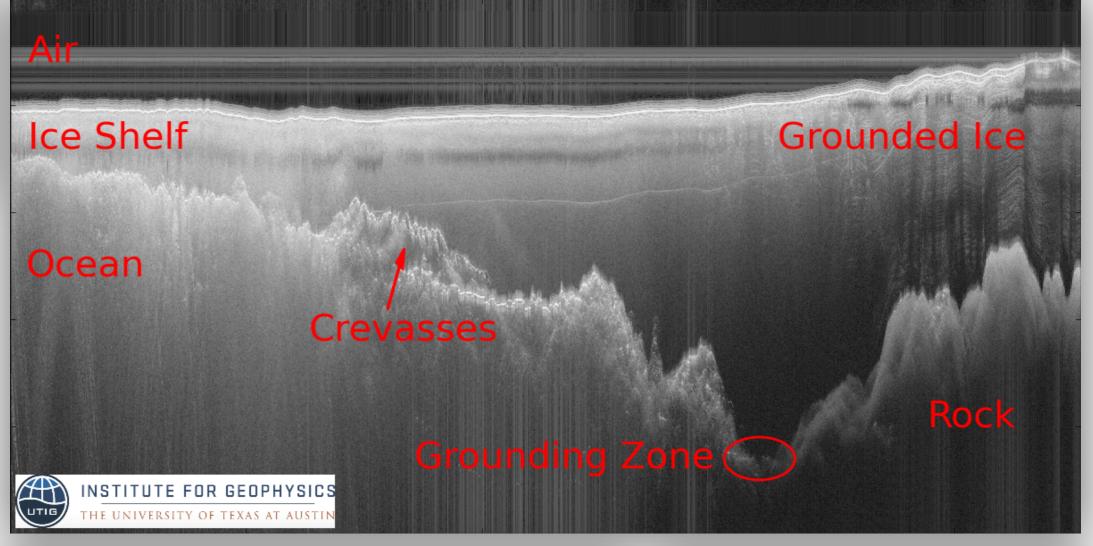


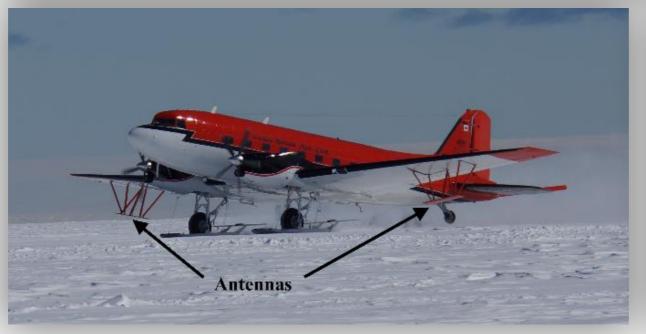




Source: http://lindzey.github.io/blog/2015/07/27/a-brief-introduction-to-ice-penetrating-radar/









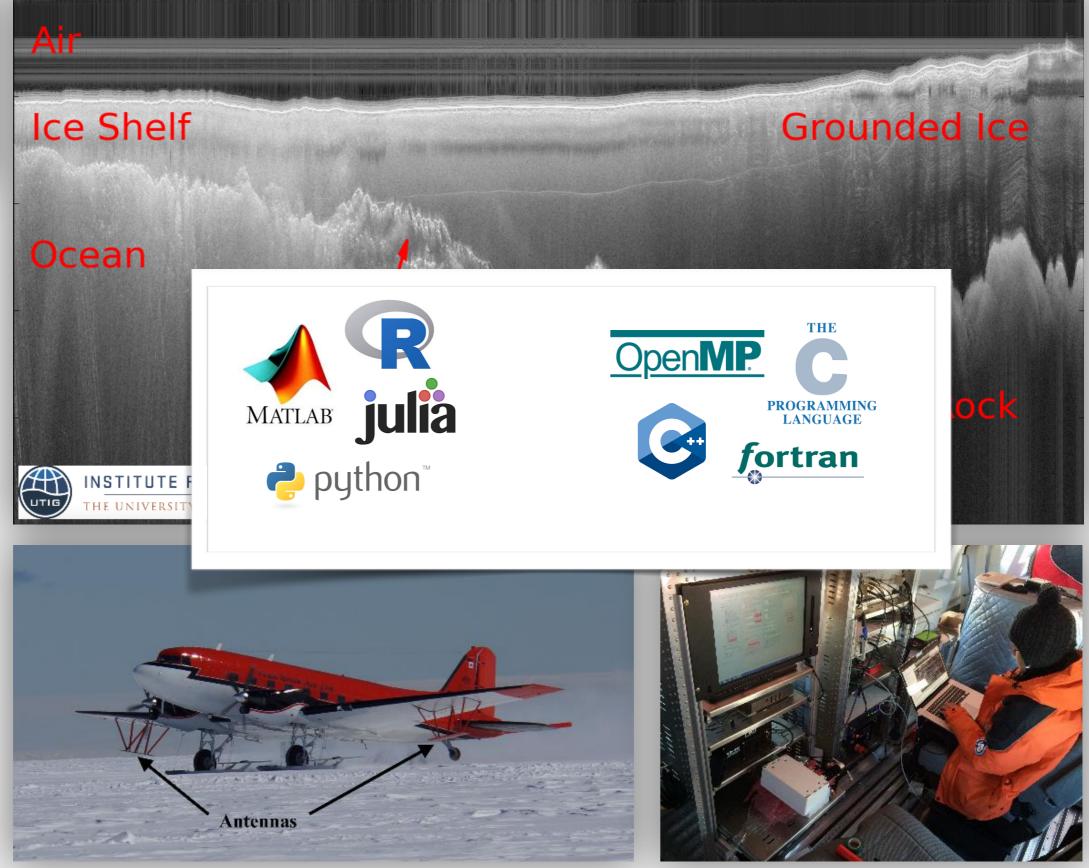
Source: http://lindzey.github.io/blog/2015/07/27/a-brief-introduction-to-ice-penetrating-radar/





Source: http://lindzey.github.io/blog/2015/07/27/a-brief-introduction-to-ice-penetrating-radar/



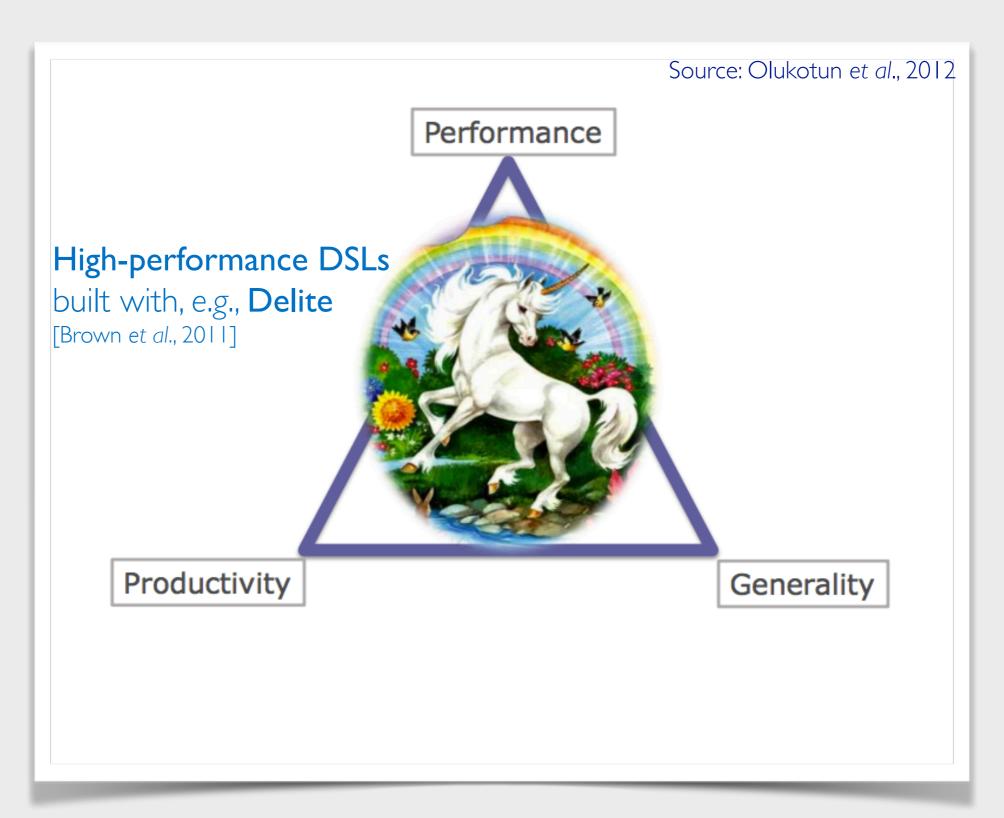


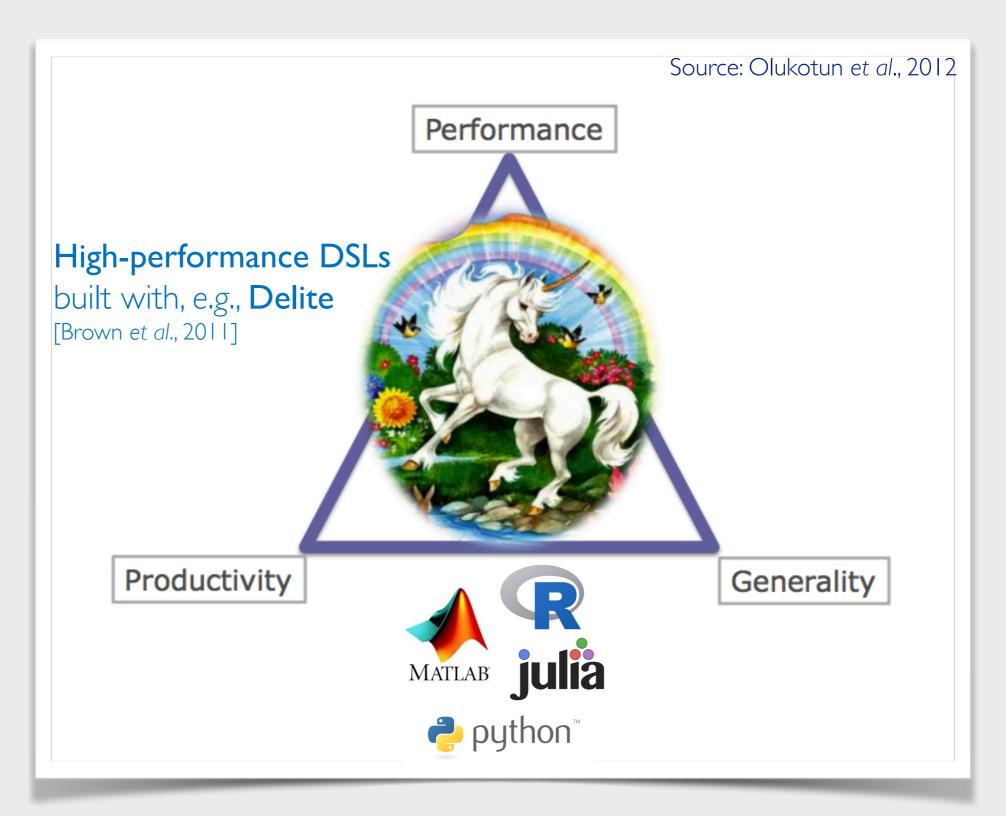
Source: http://lindzey.github.io/blog/2015/07/27/a-brief-introduction-to-ice-penetrating-radar/

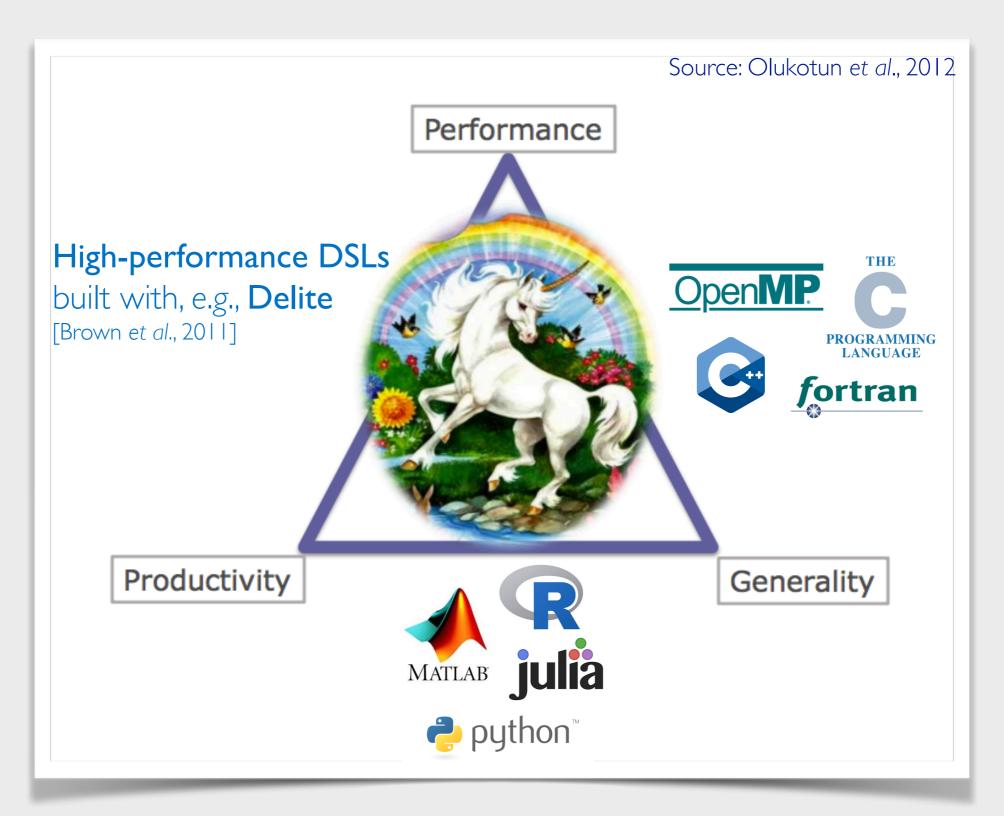


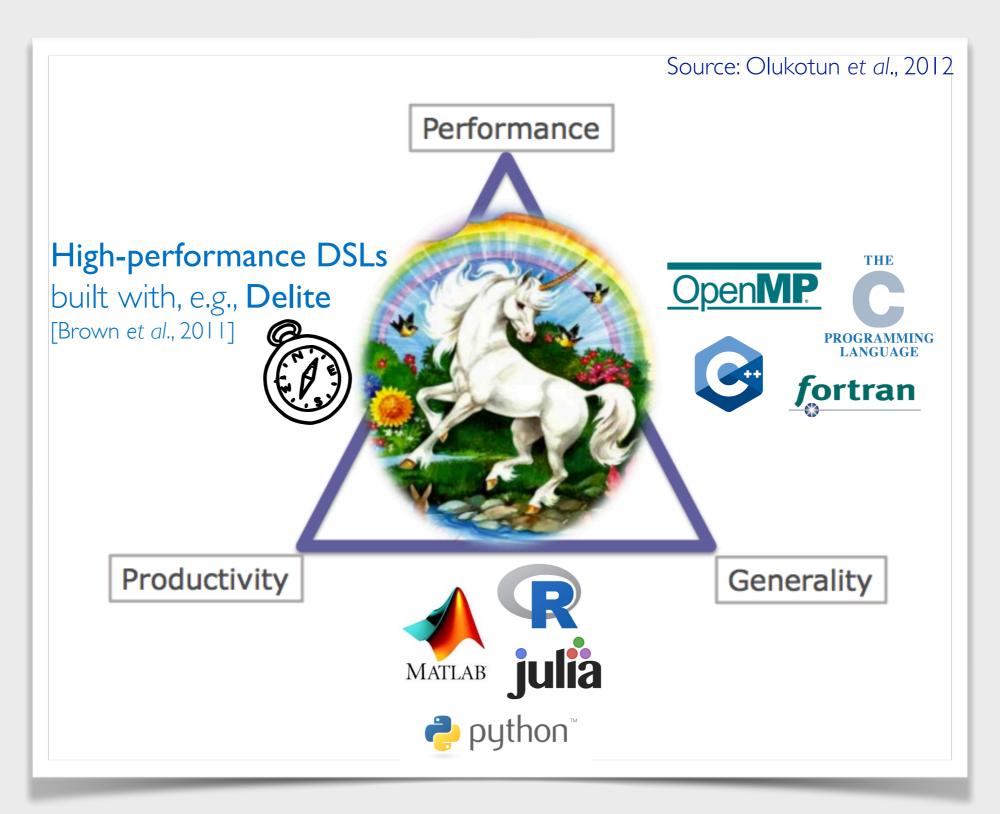


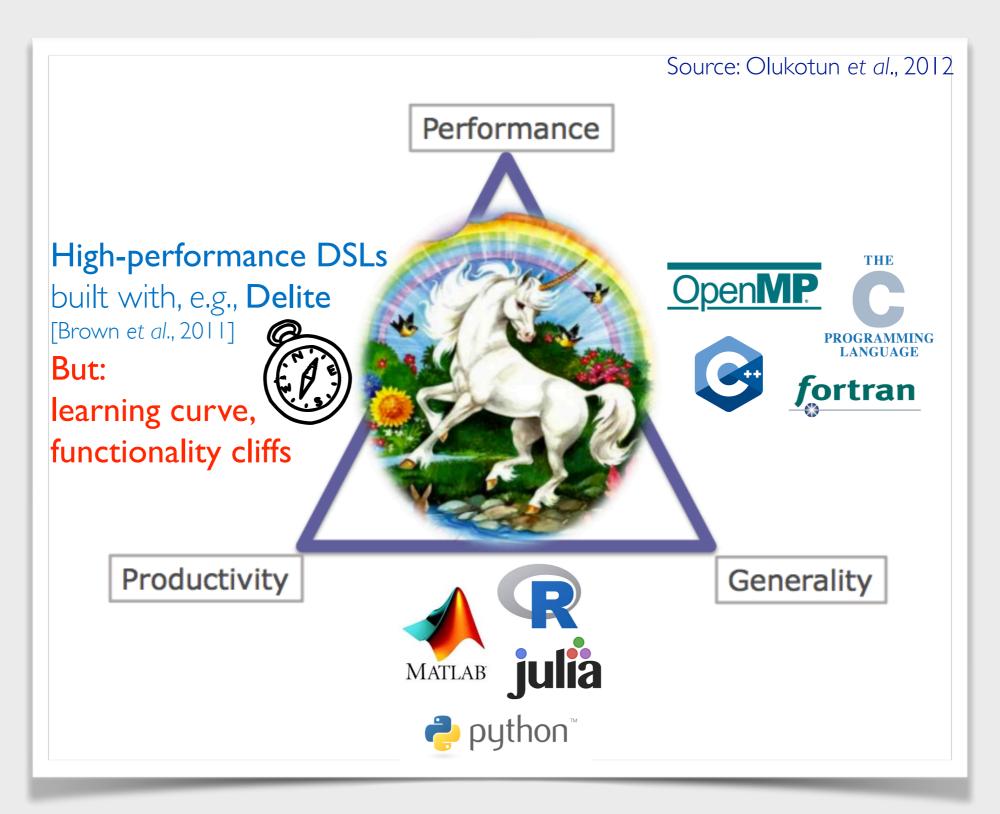
Source: http://lindzey.github.io/blog/2015/07/27/a-brief-introduction-to-ice-penetrating-radar/











ParallelAccelerator [ECOOP'17]



ParallelAccelerator

[ECOOP '17]

A non-invasive DSL embedded in julia



Supports additional runstencil construct

A combination compiler-library solution

Library mode for development and debugging

Native mode for high performance at deployment

ParallelAccelerator

[ECOOP '17]

A non-invasive DSL embedded in julia



Supports additional runstencil construct

A combination compiler-library solution

Library mode for development and debugging

Native mode for high performance at deployment

github.com/IntelLabs/ParallelAccelerator.jl

@acc example: Black-Scholes option pricing



```
using ParallelAccelerator
@acc function blackscholes(sptprice, strike, rate, volatility, time)
    logterm = log10(sptprice ./ strike)
    powterm = .5 .* volatility .* volatility
    den = volatility .* sqrt(time)
    d1 = (((rate .+ powterm) .* time) .+ logterm) ./ den
    d2 = d1 .- den
    NofXd1 = 0.5 .+ 0.5 .* erf(0.707106781 .* d1)
    NofXd2 = 0.5 .+ 0.5 .* erf(0.707106781 .* d2)
    futureValue = strike .* exp(- rate .* time)
    c1 = futureValue .* NofXd2
    call = sptprice .* NofXd1 .- c1
    put = call .- futureValue .+ sptprice
end
put = blackscholes(sptprice, initStrike, rate, volatility, time)
```

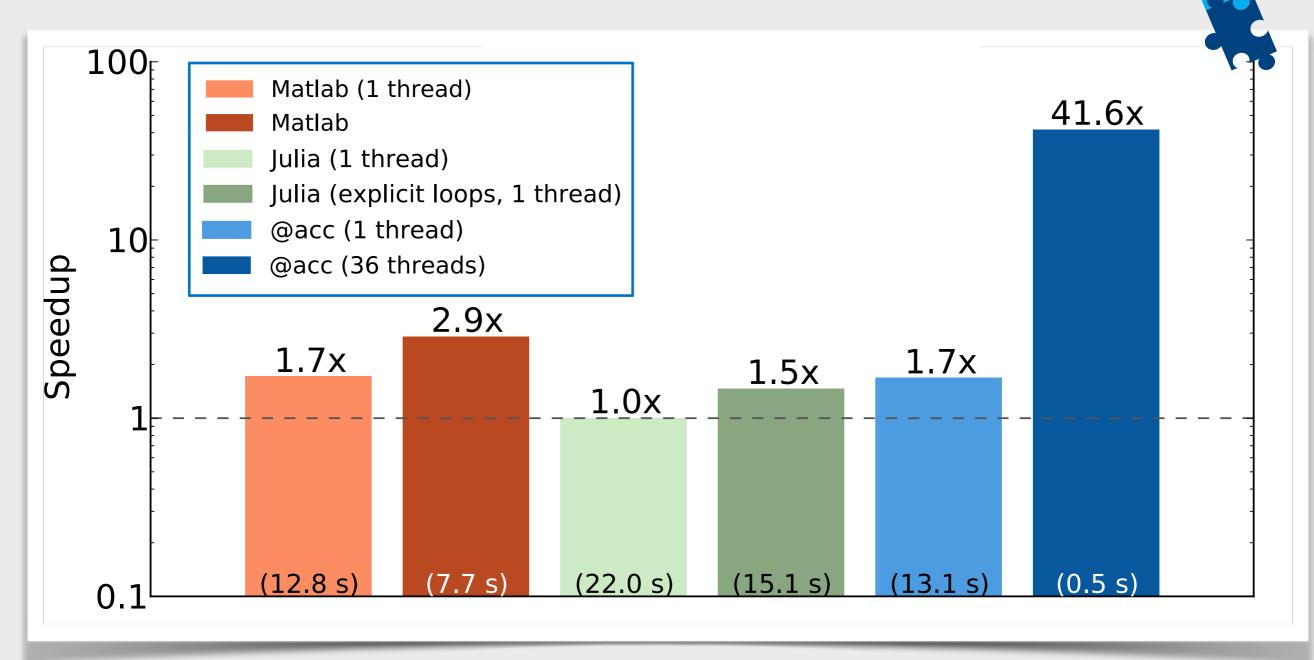


```
using ParallelAccelerator
@acc function blackscholes(sptprice, strike, rate, volatility, time)
    logterm = log10(sptprice ./ strike)
    powterm = .5 .* volatility .* volatility
    den = volatility .* sqrt(time)
    d1 = (((rate .+ powterm) .* time) .+ logterm) ./ den
    d2 = d1 . – den
    NofXd1 = 0.5 .+ 0.5 .* erf(0.707106781 .* d1)
NofXd2 = 0.5 .+ 0.5 .* erf(0.707106781 .* d2)
    futureValue = strike .* exp(- rate .* time)
    c1 = futureValue .* NofXd2
    call = sptprice * NofXd1 - c1
    put = call .- futureValue .+ sptprice
end
put = blackscholes(sptprice, initStrike, rate, volatility, time)
```



```
using ParallelAccelerator
@acc function blackscholes(sptprice, strike, rate, volatility, time)
    logterm = log10(sptprice ./ strike)
    powterm = .5 .* volatility .* volatility
    den = volatility .* sqrt(time)
    d1 = (((rate .+ powterm) .* time) .+ logterm) ./ den
    d2 = d1 . – den
    NofXd1 = 0.5 .+ 0.5 .* erf(0.707106781 .* d1)
NofXd2 = 0.5 .+ 0.5 .* erf(0.707106781 .* d2)
    futureValue = strike .* exp(- rate .* time)
    c1 = futureValue .* NofXd2
    call = sptprice * NofXd1 - c1
    put = call .- futureValue .+ sptprice
end
put = blackscholes(sptprice, initStrike, rate, volatility, time)
```

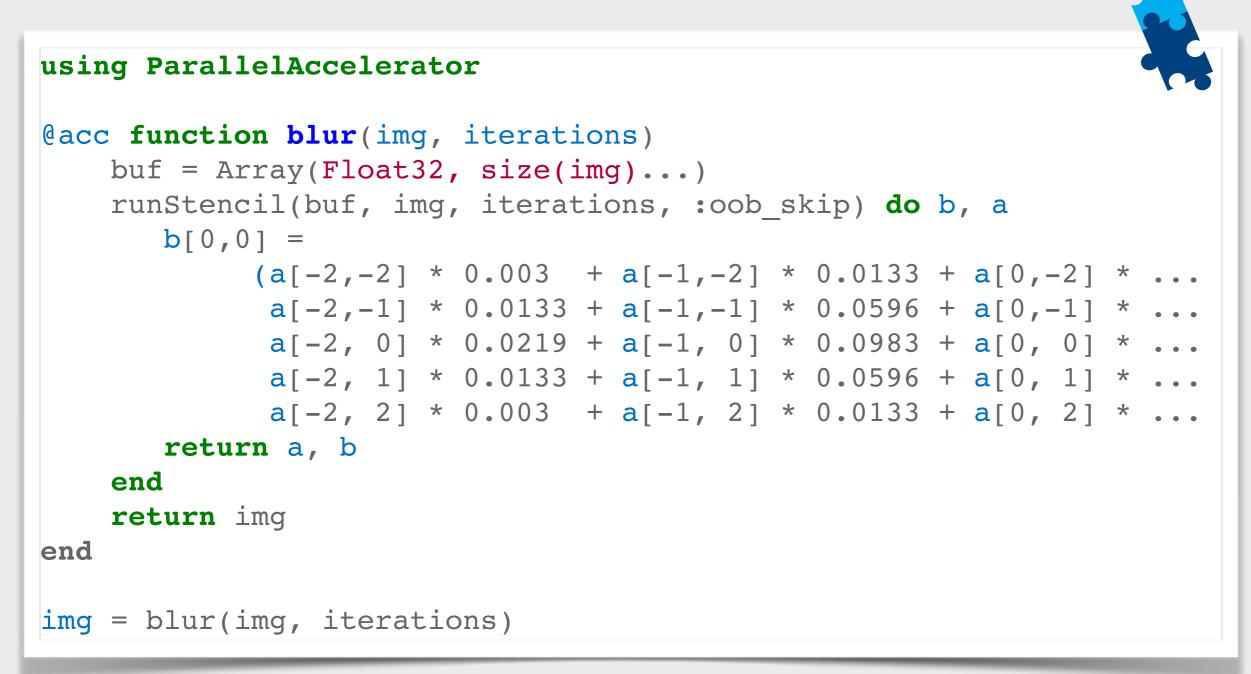
```
using ParallelAccelerator
@acc function blackscholes(sptprice, strike, rate, volatility, time)
   logterm = log10(sptprice ./ strike)
   powterm = .5 .* volatility .* volatility
   den = volatility .* sqrt(time)
   d1 = (((rate .+ powterm) .* time) .+ logterm) ./ den
   d2 = d1 den
   futureValue = strike .* exp(- rate .* time)
   call = sptprice * NofXd1 .- c1
   put = call .- futureValue .+ sptpri
                                       Translates pointwise array
end
                                   operations like .+, .-, .*, and ./
put = blackscholes(sptprice, initStrike
                                    to data-parallel map operations
```



Running on arrays of 100 million elements

2 Intel(R) Xeon(R) CPU E5-2699 v3 @ 2.3GHz processors, 18 cores each (36 cores total) 128 GB RAM Julia version 0.5.0; Matlab version R2015a

runStencil example: Gaussian blur

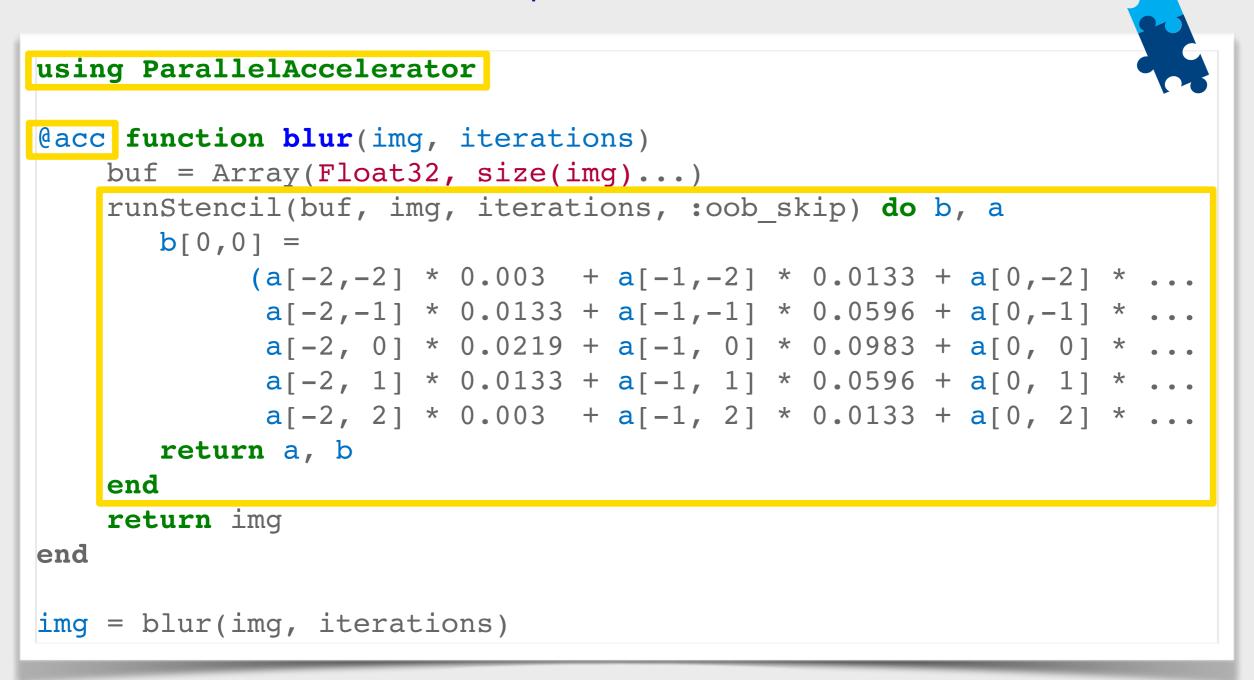


runStencil example: Gaussian blur

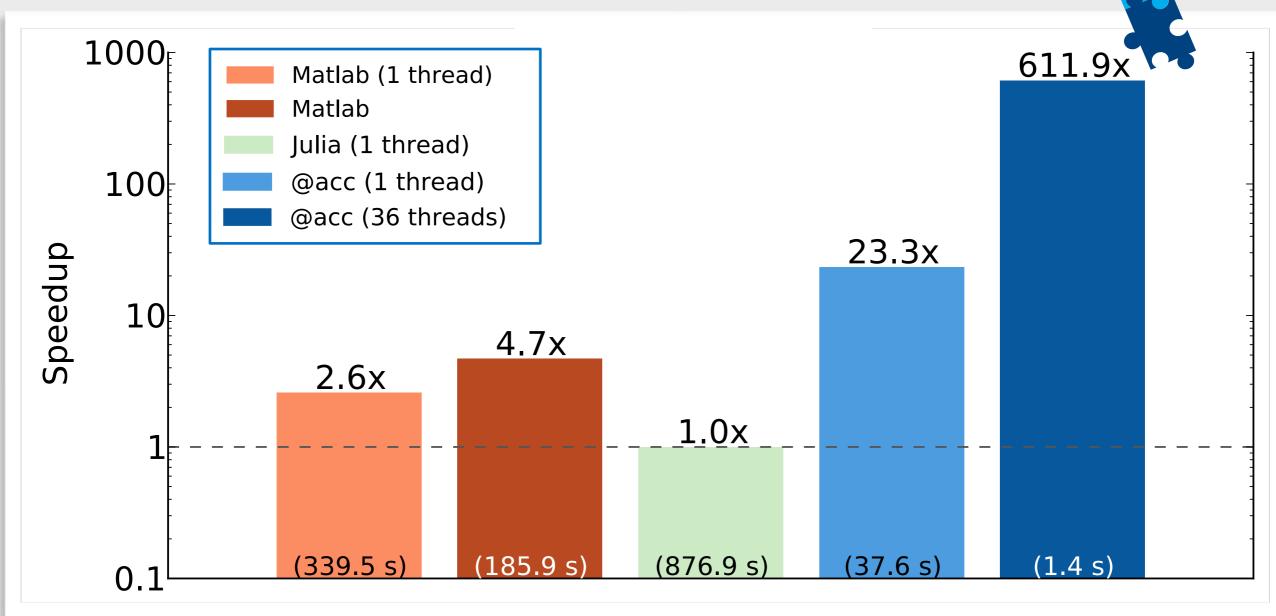


```
using ParallelAccelerator
@acc function blur(img, iterations)
    buf = Array(Float32, size(img)...)
    runStencil(buf, img, iterations, :oob_skip) do b, a
       b[0,0] =
            (a[-2,-2] * 0.003 + a[-1,-2] * 0.0133 + a[0,-2] * ...
             a[-2,-1] * 0.0133 + a[-1,-1] * 0.0596 + a[0,-1] * ...
             a[-2, 0] * 0.0219 + a[-1, 0] * 0.0983 + a[0, 0] * ...
             a[-2, 1] * 0.0133 + a[-1, 1] * 0.0596 + a[0, 1] * ...
             a[-2, 2] * 0.003 + a[-1, 2] * 0.0133 + a[0, 2] * ...
       return a, b
    end
    return img
end
img = blur(img, iterations)
```

runStencil example: Gaussian blur







Running on a 7095x5322 source image for 100 iterations

2 Intel(R) Xeon(R) CPU E5-2699 v3 @ 2.3GHz processors, 18 cores each (36 cores total) 128 GB RAM Julia version 0.5.0; Matlab version R2015a

Impact of ParallelAccelerator...

[Truong et al., PLDI '16]

Latte: A Language, Compiler, and Runtime for Elegant and Efficient Deep Neural Networks

Leonard Truong

Intel Labs / UC Berkeley, USA leonard.truong@intel.com

Hai Liu
Intel Labs, USA
hai liu@intel com

Rajkishore Barik
Intel Labs, USA
rajkishore.barik@intel.com

Chick Markley
UC Berkeley, USA

Ehsan Totoni Intel Labs, USA ehsan.totoni@intel.com

Armando Fox
UC Berkeley, USA
fox@cs berkeley edu

Impact of ParallelAccelerator...

[Truong et al., PLDI '16]

Latte: A Language, Compiler, and Runtime for

Elegan' --- I Fee --- No. -- No. --- N

[Totoni et al., ICS '17]

Leonard Truong
Intel Labs / UC Berkeley, US
leonard.truong@intel.com

Hai Liu
Intel Labs, USA

HPAT: High Performance Analytics with Scripting Ease-of-Use

Ehsan Totoni Intel Labs, USA ehsan.totoni@intel.com Todd A. Anderson Intel Labs, USA todd.a.anderson@intel.com Tatiana Shpeisman Intel Labs, USA tatiana.shpeisman@intel.com

ABSTRACT

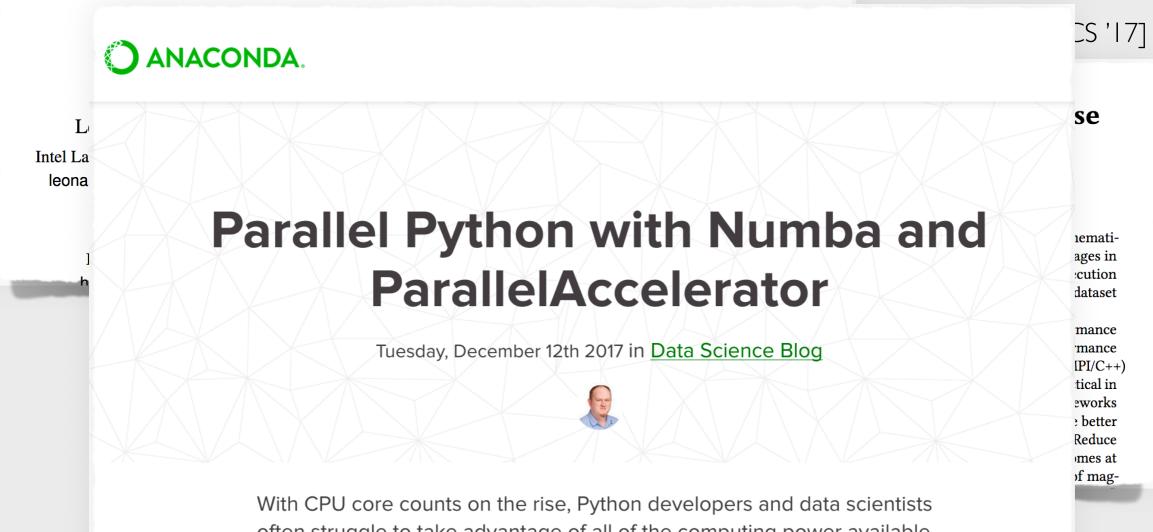
Big data analytics requires high programmer productivity and high performance simultaneously on large-scale clusters. However, current big data analytics frameworks (e.g. Apache Spark) have prohibitive runtime overheads since they are library-based. We introduce a novel auto-parallelizing compiler approach that exploits the characteristics of the data analytics domain such as the map/reduce parallel pattern and is robust, unlike previous auto-parallelization methods. Using this approach, we build High Performance Analytics Toolkit (HPAT), which parallelizes high-level scripting (Julia) programs automatically, generates efficient MPI/C++ code, and provides resiliency. Furthermore, it provides automatic optimizations for scripting programs, such as fusion of array operations. Thus, HPAT is 369× to 2033× faster than Spark on the Cori supercomputer

as MATLAB, R, Python, and Julia since they express mathematical operations naturally and are the most productive languages in practice [14, 30]. High performance requires efficient execution on large-scale distributed-memory clusters due to extreme dataset sizes.

Currently, there is a significant productivity and performance gap in the big data analytics domain. A typical High Performance Computing (HPC) approach of writing low-level codes (e.g. MPI/C++) is beyond the expertise of most data scientists and is not practical in their interactive workflows. Existing big data analytics frameworks such as Apache Hadoop [37] and Apache Spark [40] provide better productivity for big data analytics on clusters using the MapReduce programming paradigm [15]. However, this productivity comes at the cost of performance as these frameworks are orders of mag-

Impact of ParallelAccelerator...

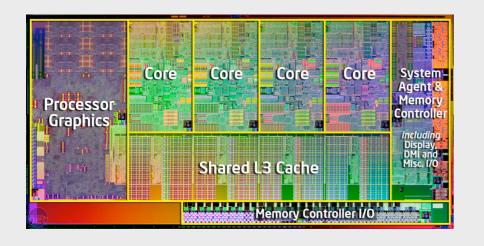
[Truong et al., PLDI '16]

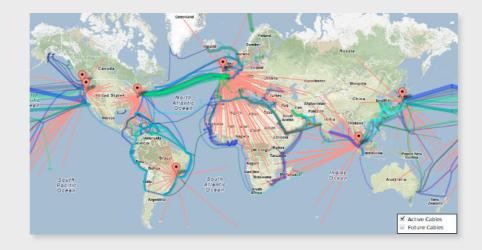


With CPU core counts on the rise, Python developers and data scientists often struggle to take advantage of all of the computing power available to them. CPUs with 20 or more cores are now available, and at the extreme end, the Intel® Xeon Phi™ has 68 cores with 4-way Hyper-Threading. (That's 272 active threads!)

To use multiple cores in a Python program, there are three options. You can use multiple processes, multiple threads, or both. Multiple processes are a common way to split work across multiple CPU cores in Python. Each process runs independently of the others, but there is the

Source: www.anaconda.com/blog/developer-blog/parallel-python-with-numba-and-parallelaccelerator/

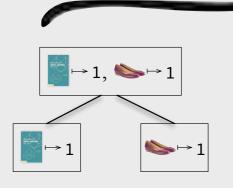




Parallel systems

Distributed systems

language-based approaches



Lattice-based data structures (LVars) for deterministic programming [POPL '14, PLDI '14, FHPC '13, WoDet '14]



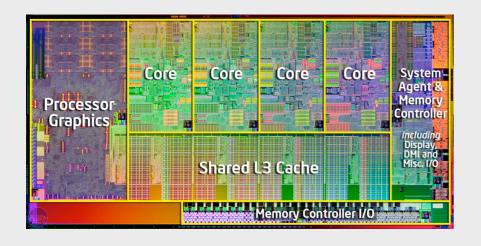


SMT-based verification of neural networks
[SysML'18]



Guiding principle:

Find the right high-level abstractions to enable efficient computation

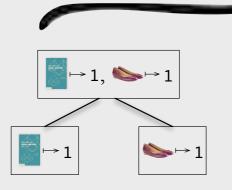




Parallel systems

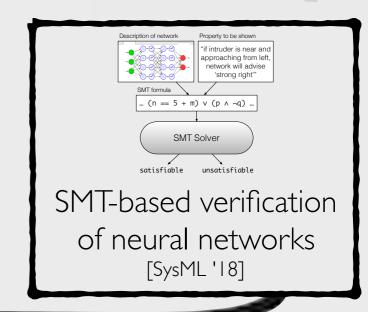
Distributed systems

language-based approaches



Lattice-based data structures (LVars) for deterministic programming [POPL '14, PLDI '14, FHPC '13, WoDet '14]

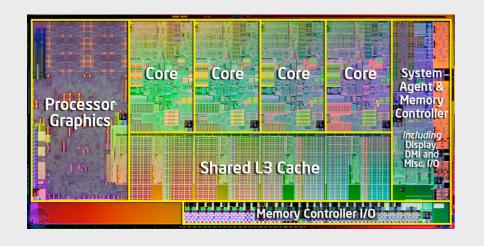
Non-invasive DSLs for productive parallelism [ECOOP'17]



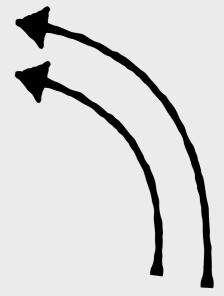


Guiding principle:

Find the right high-level abstractions to enable efficient computation



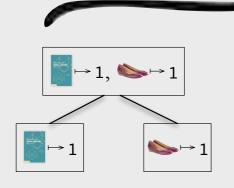




Parallel systems

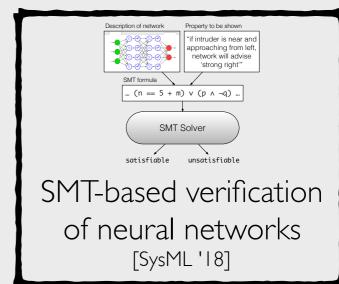
Distributed systems

language-based approaches



Lattice-based data structures (LVars) for deterministic programming [POPL '14, PLDI '14, FHPC '13, WoDet '14]

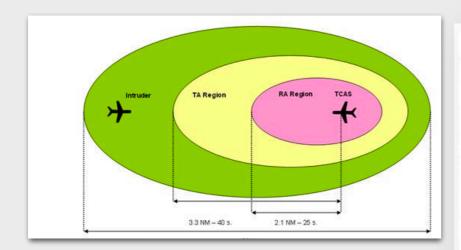
Non-invasive DSLs for productive parallelism [ECOOP'17]





Guiding principle:

Find the right high-level abstractions to enable efficient computation



[Julian et al., 2016]

Policy Compression for Aircraft Collision Avoidance Systems

Kyle D. Julian*, Jessica Lopez[†], Jeffrey S. Brush[†], Michael P. Owen[‡] and Mykel J. Kochenderfer*

*Department of Aeronautics and Astronautics, Stanford University, Stanford, CA, 94305

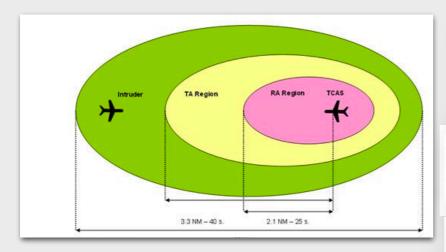
[†]Applied Physics Laboratory, Johns Hopkins University, Laurel, MD, 20723

[‡]Lincoln Laboratory, Massachusetts Institute of Technology, Lexington, MA, 02420

Abstract—One approach to designing the decision making logic for an aircraft collision avoidance system is to frame the problem as Markov decision process and optimize the system using dynamic programming. The resulting strategy can be represented as a numeric table. This methodology has been used in the development of the ACAS X family of collision avoidance systems for manned and unmanned aircraft. However, due to the high dimensionality of the state space, discretizing the state variables can lead to very large tables. To improve storage efficiency, we propose two approaches for compressing the lookup table. The first approach exploits redundancy in the table. The table is decomposed into a set of lower-dimensional tables, some of which can be represented by single tables in areas where the lowerdimensional tables are identical or nearly identical with respect to a similarity metric. The second approach uses a deep neural network to learn a complex non-linear function approximation of the table. With the use of an asymmetric le

is extremely large, requiring hundreds of gigabytes of floating point storage. A simple technique to reduce the size of the score table is to downsample the table after dynamic programming. To minimize the deterioration in decision quality, states are removed in areas where the variation between values in the table are smooth. This allows the table to be downsampled with only minor impact on overall decision performance. The downsampling reduces the size of the table by a factor of 180 from that produced by dynamic programming. For the rest of this paper, we refer to the downsampled ACAS Xu horizontal table as our baseline, original table.

Even after downsampling, the current table requires over 2GB of floating point storage. Discretized score tables like this have been compressed with Gaussian processes [6] and



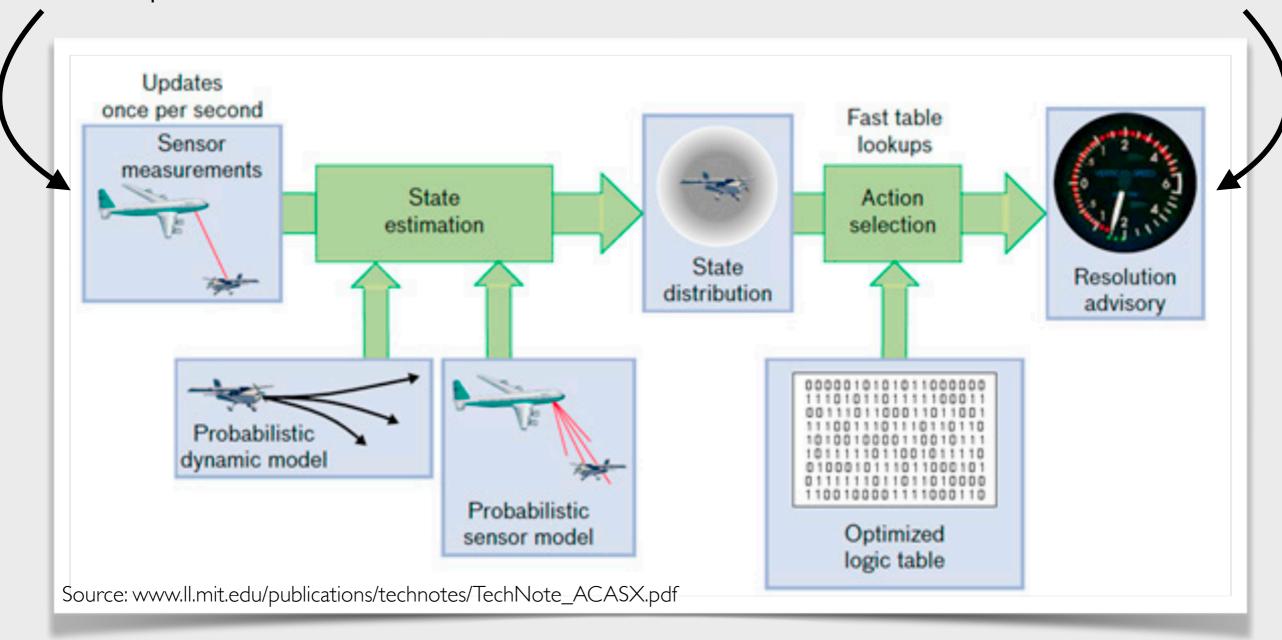
[Julian et al., 2016]

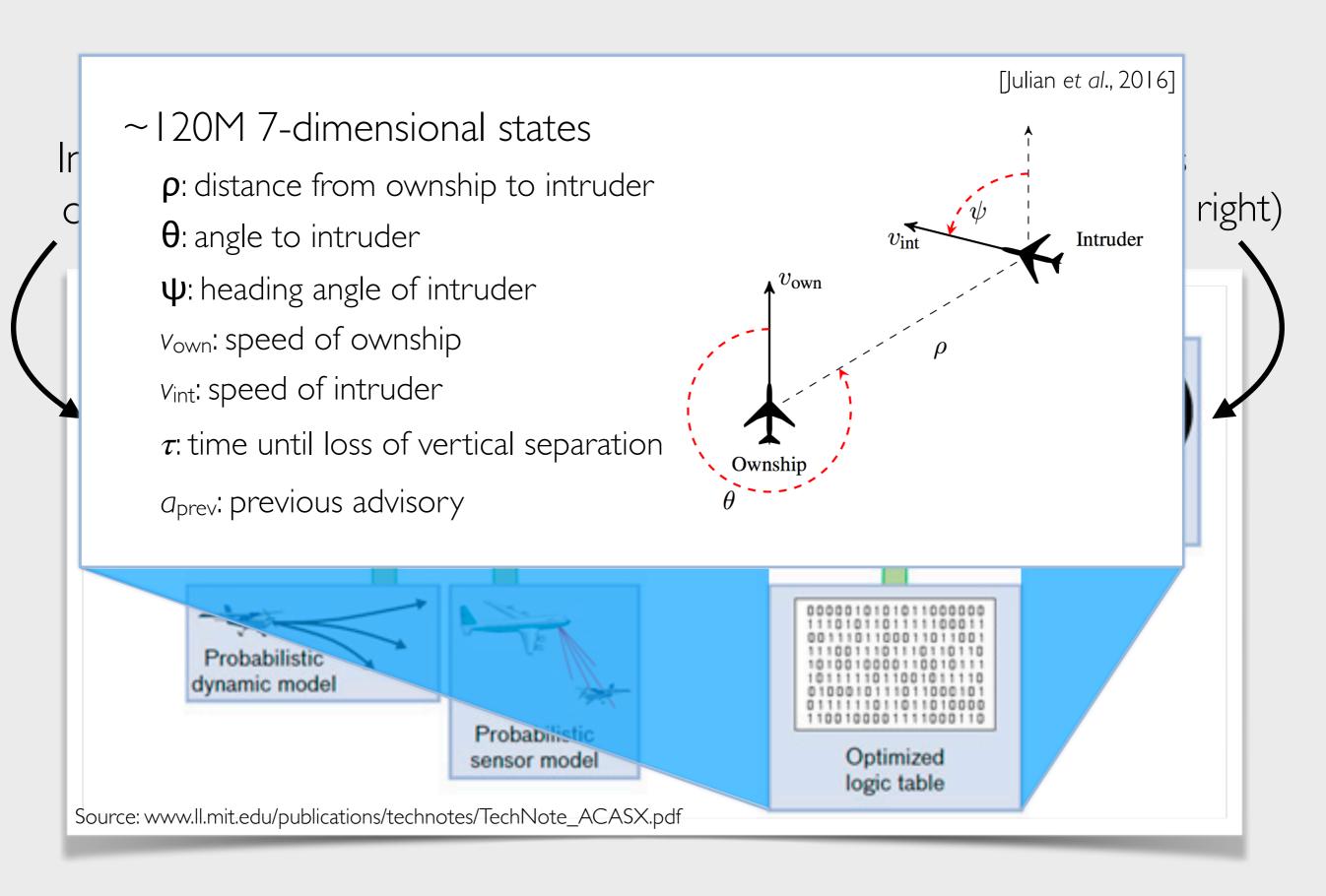
Policy Compression for Aircraft Collision Avoidance Systems

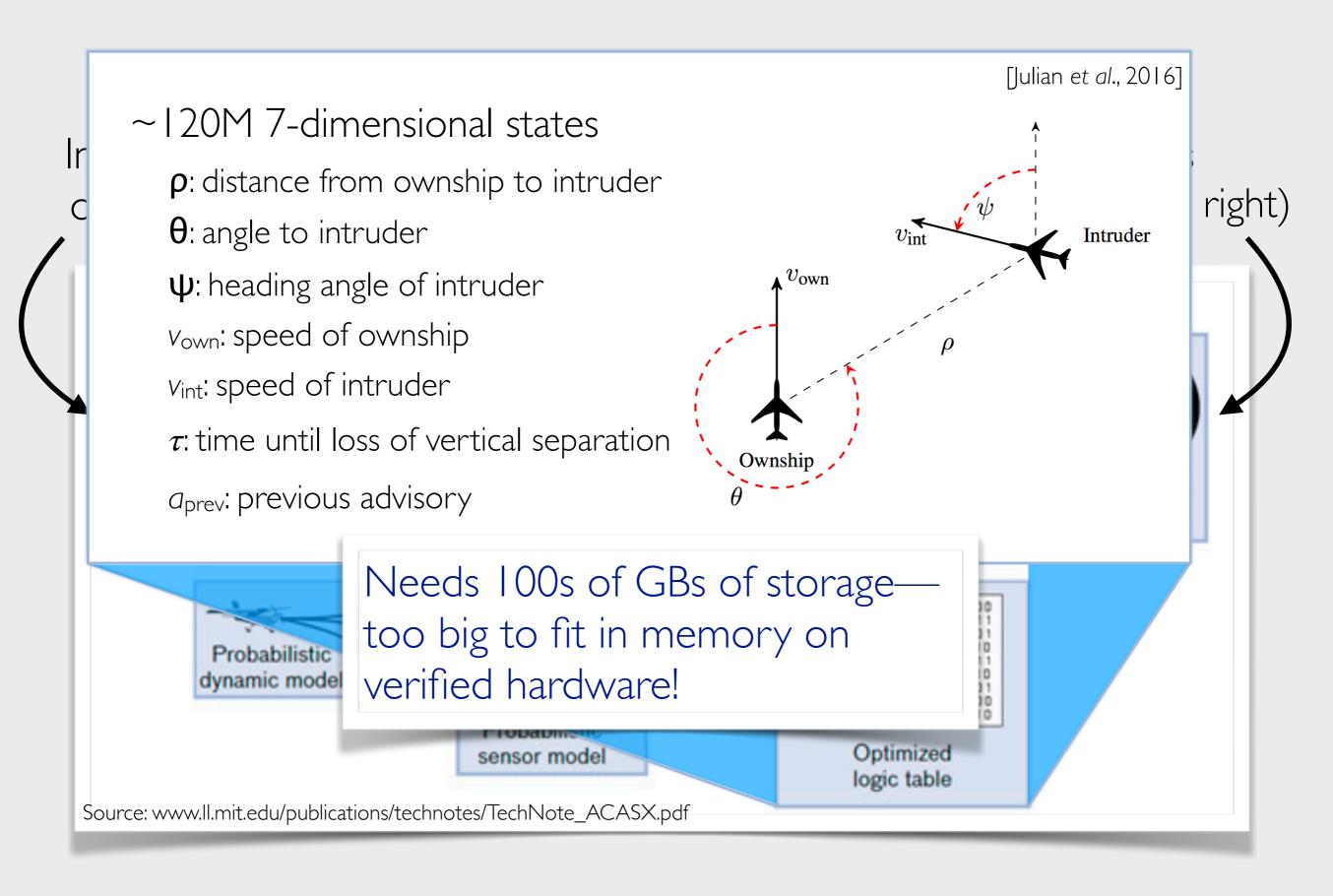
to a similarity metric. The second approach uses a deep neural network to learn a complex non-linear function approximation of the table. With the use of an asymmetric loss function and a preserving the relative preferences of the possible advisories for each state. As a result, the table can be approximately represented by only the parameters of the network, which reduces the required storage space by a factor of 1000. Simulation studies show that system performance is very similar using either

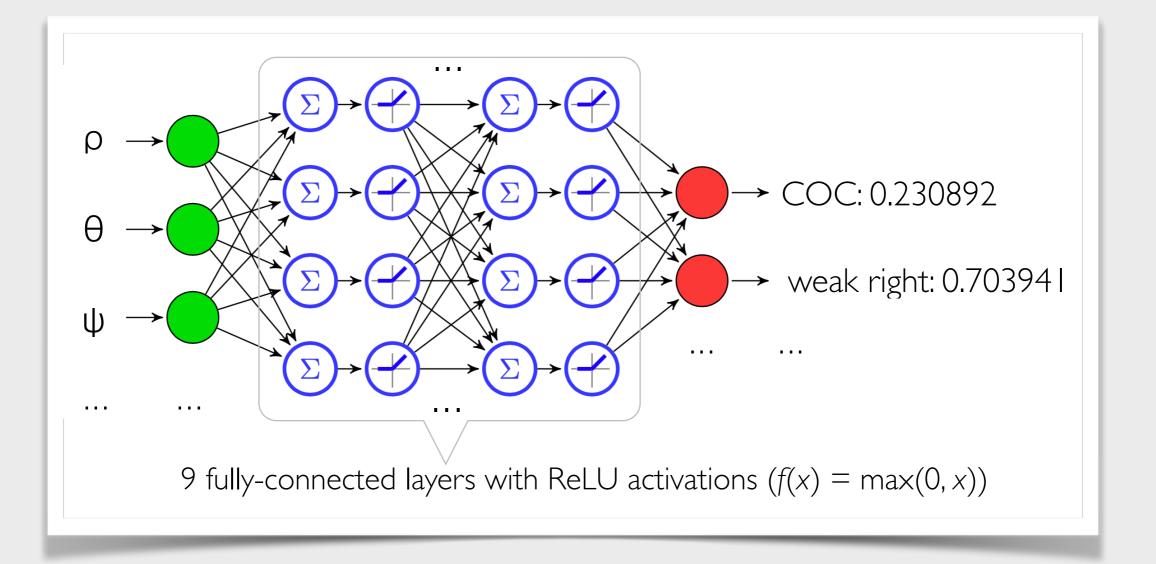
crete representation. Although there are significant certification concerns with neural network representations, which may be addressed in the future, these results indicate a promising way Input: sensor data once per second

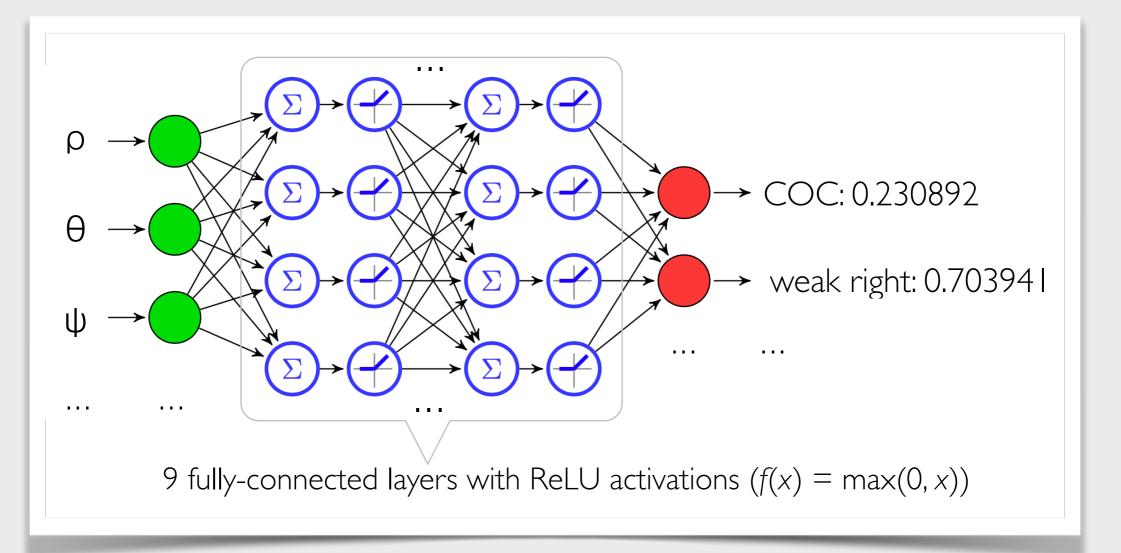
Output: one of five resolution advisories (COC, weak left, weak right, strong left, strong right)

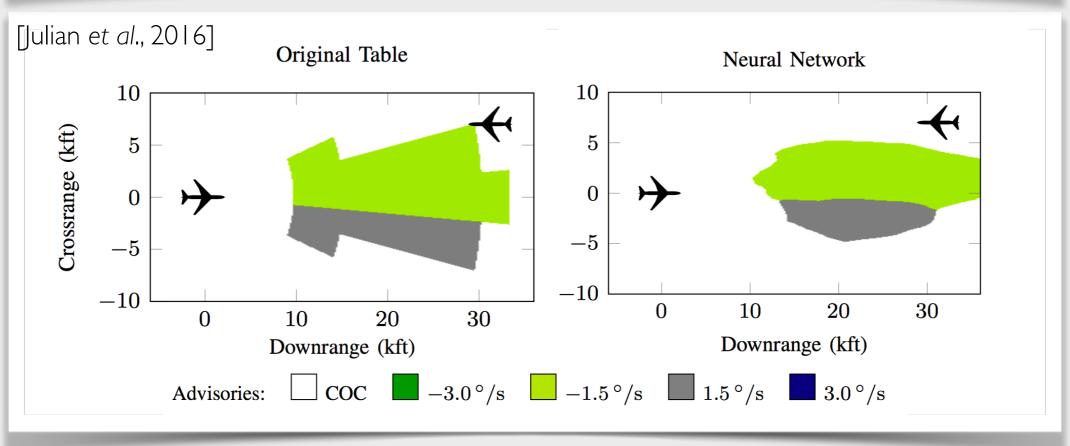








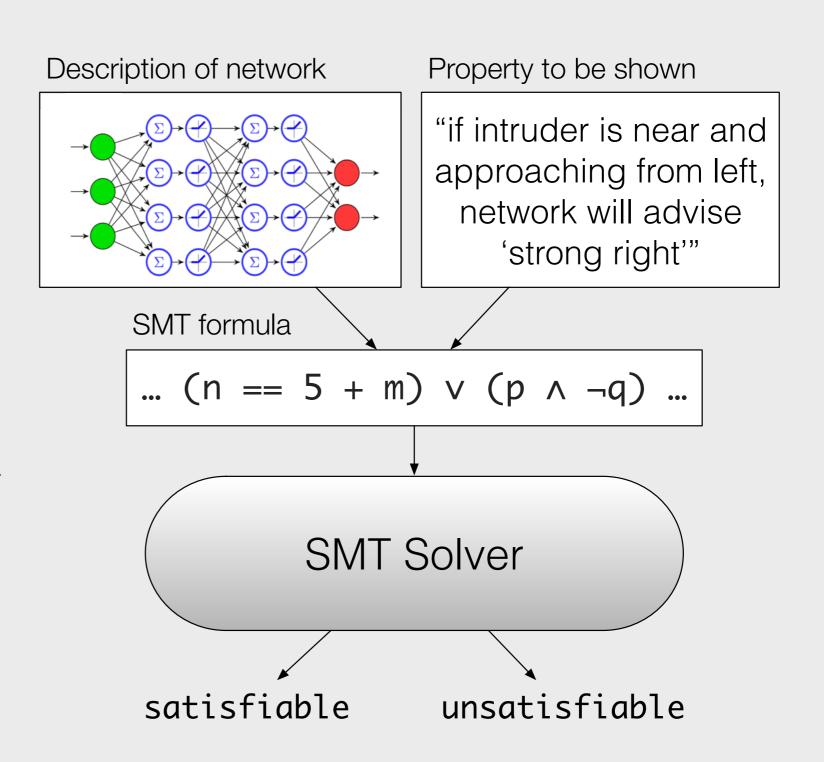




Verification strategy

SAT: determine if a Boolean formula (containing only Boolean variables, parens, A, V, ¬) is satisfiable

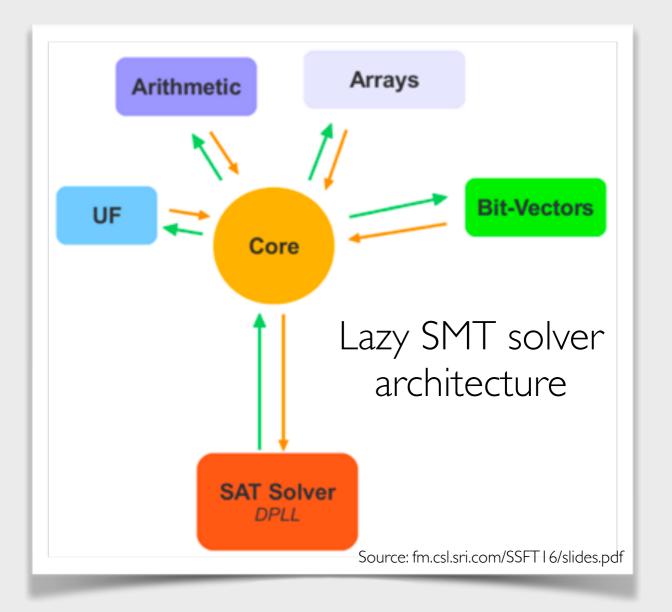
SMT: determine satisfiability of a formula with respect to some theory (e.g., theory of linear real arithmetic)



The virtues of laziness

Eager approach: convert whole SMT formula to SAT formula immediately, then solve with SAT solver

Lazy approach: use theory solvers, each specific to a particular theory

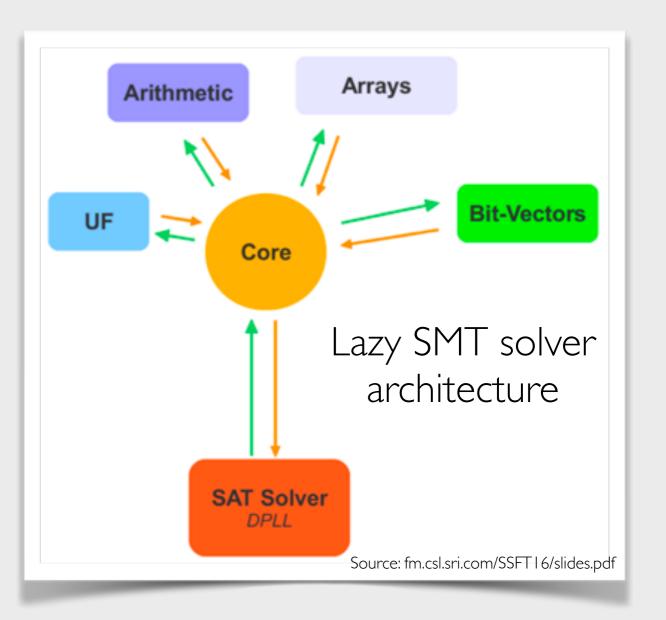


The virtues of laziness

Eager approach: convert whole SMT formula to SAT formula immediately, then solve with SAT solver

Lazy approach: use theory solvers, each specific to a particular theory



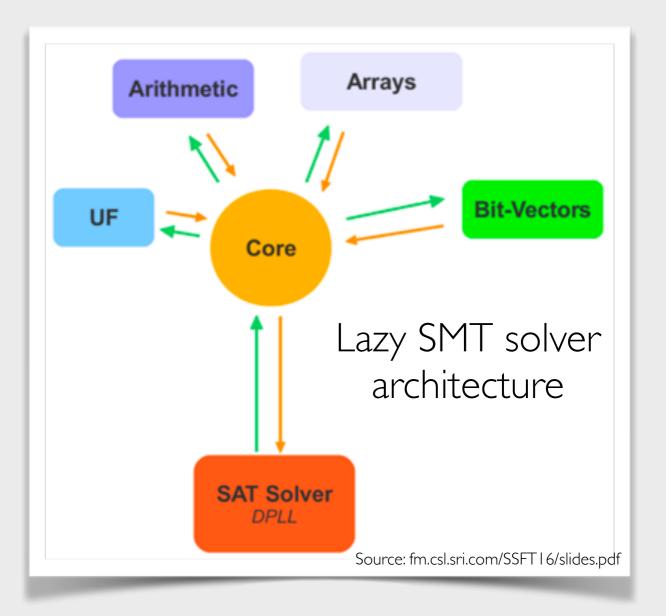


The virtues of laziness

Eager approach: convert whole SMT formula to SAT formula immediately, then solve with SAT solver

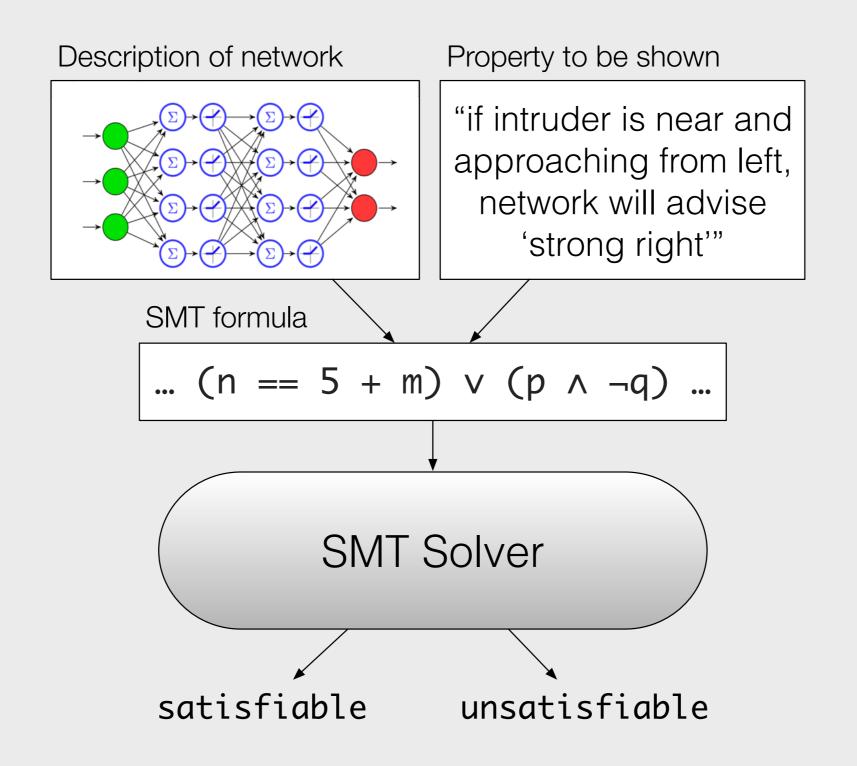
Lazy approach: use theory solvers, each specific to a particular theory

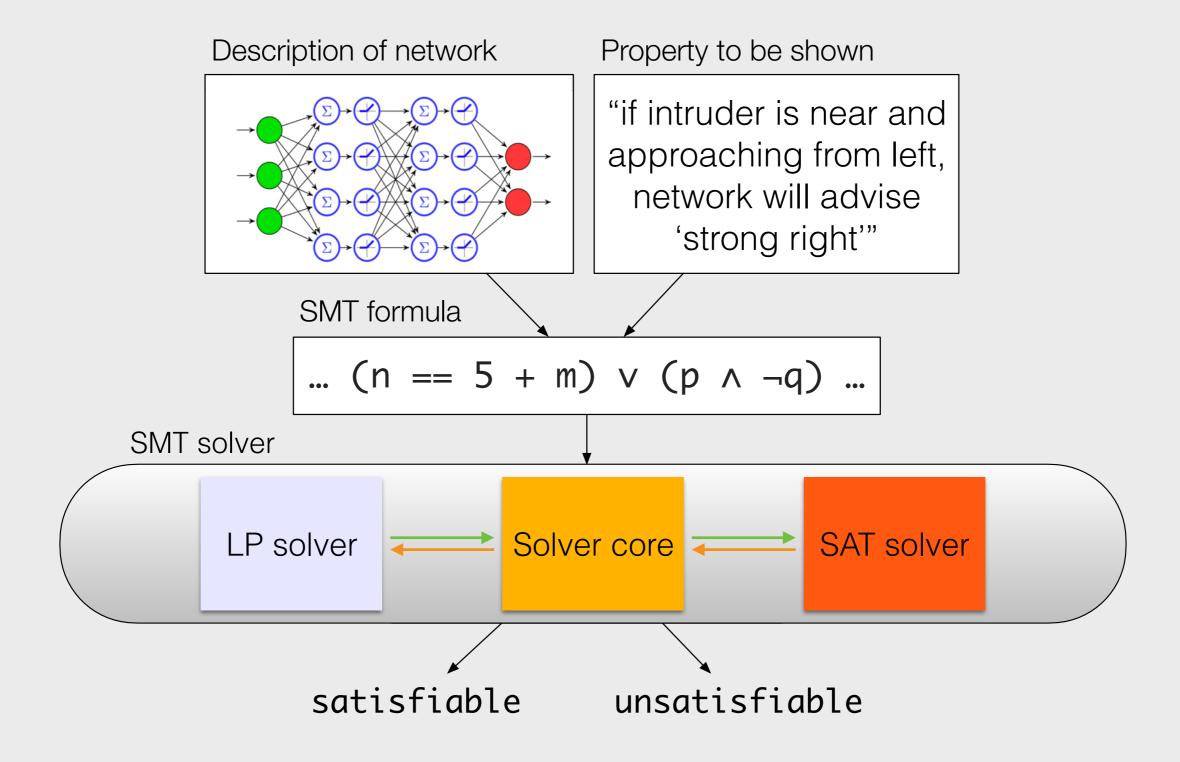


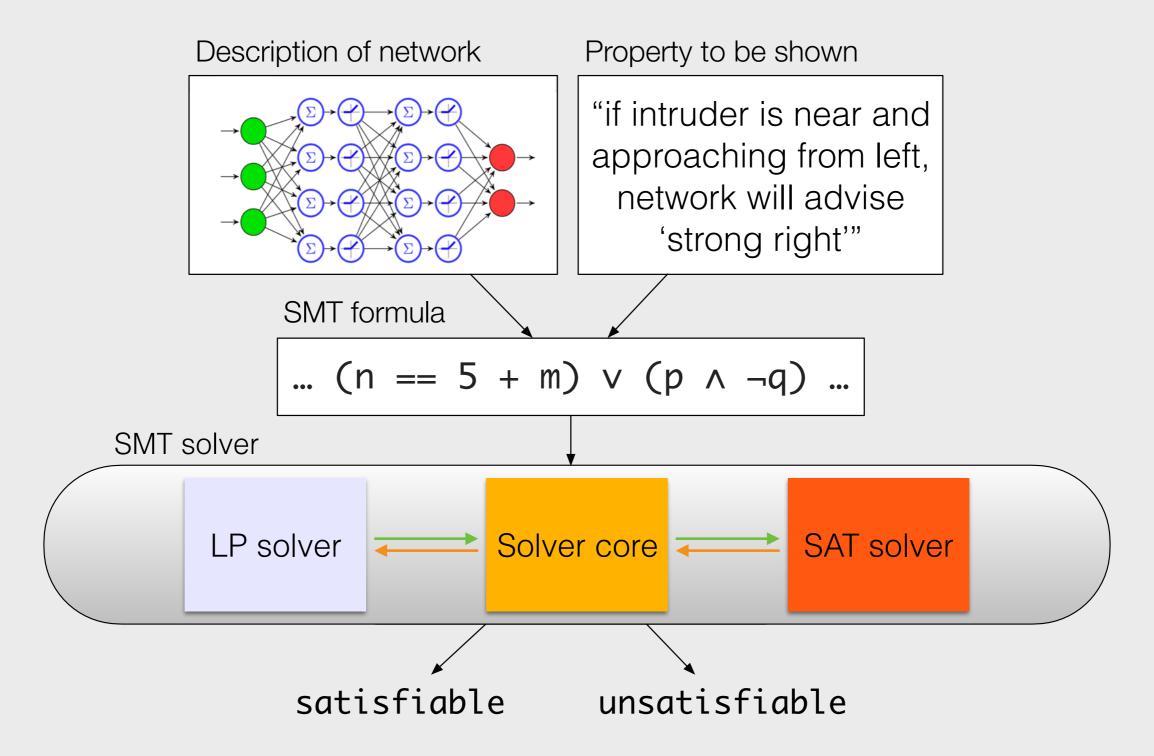


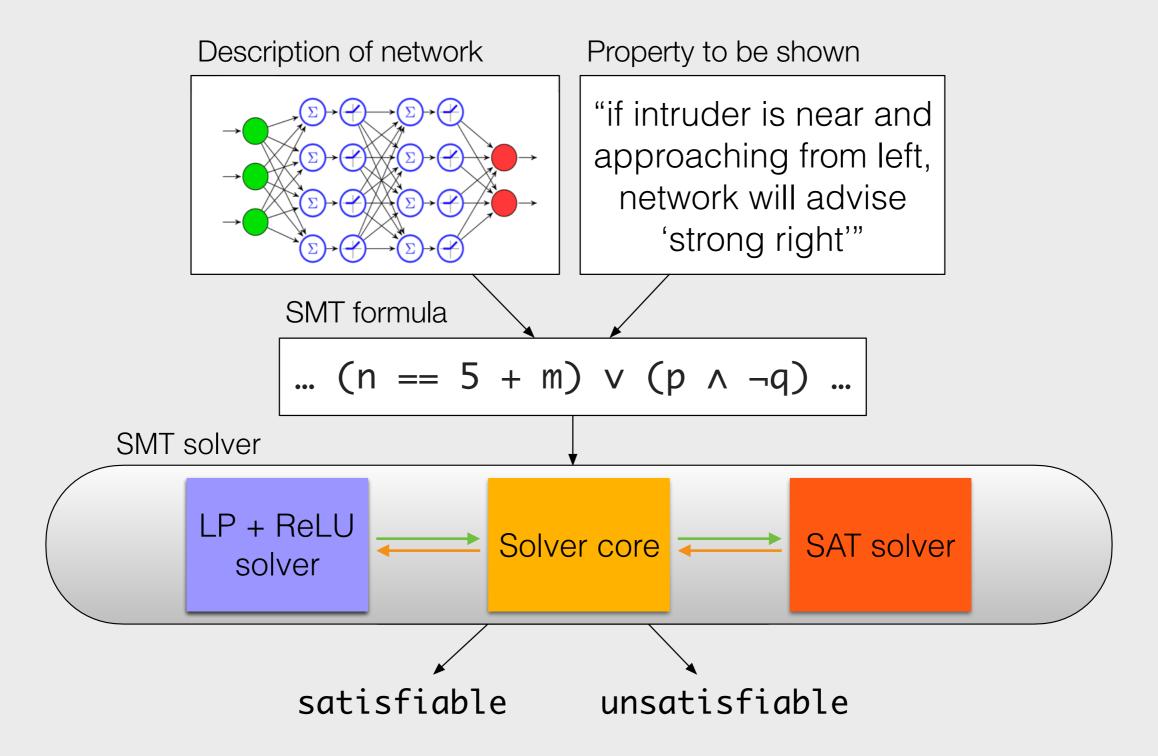


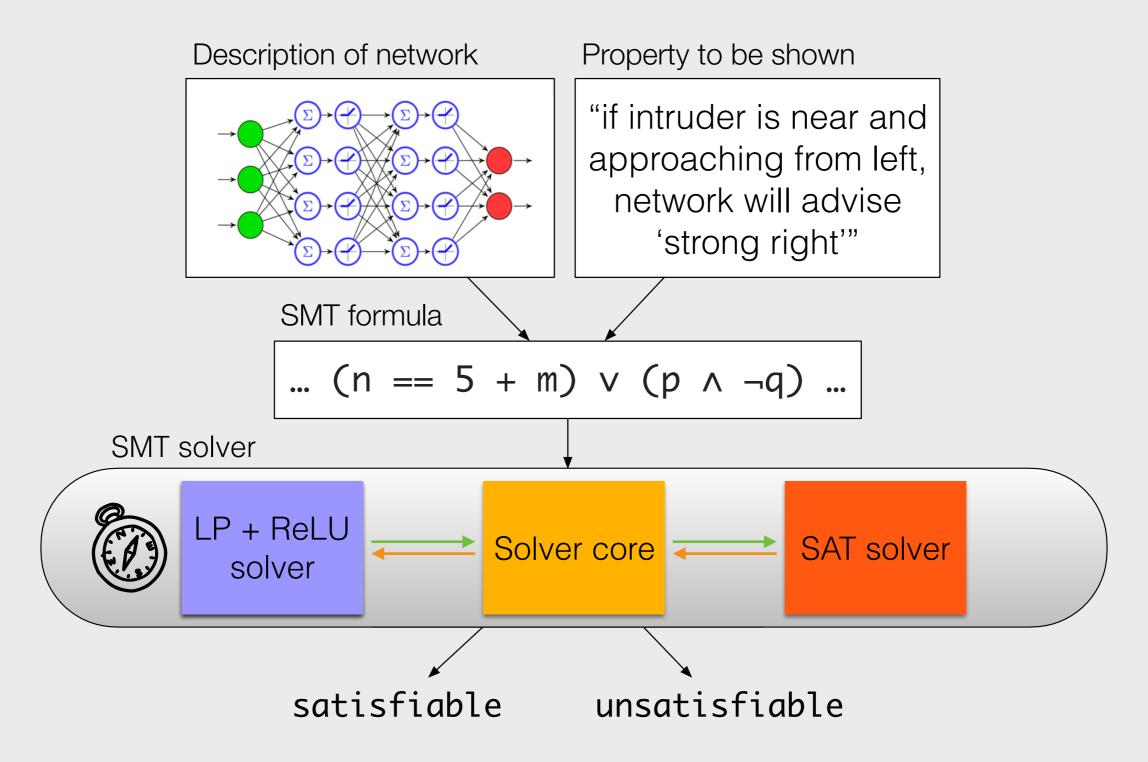
To exploit domain knowledge and unlock efficiency, we need theory solvers specifically for handling neural networks



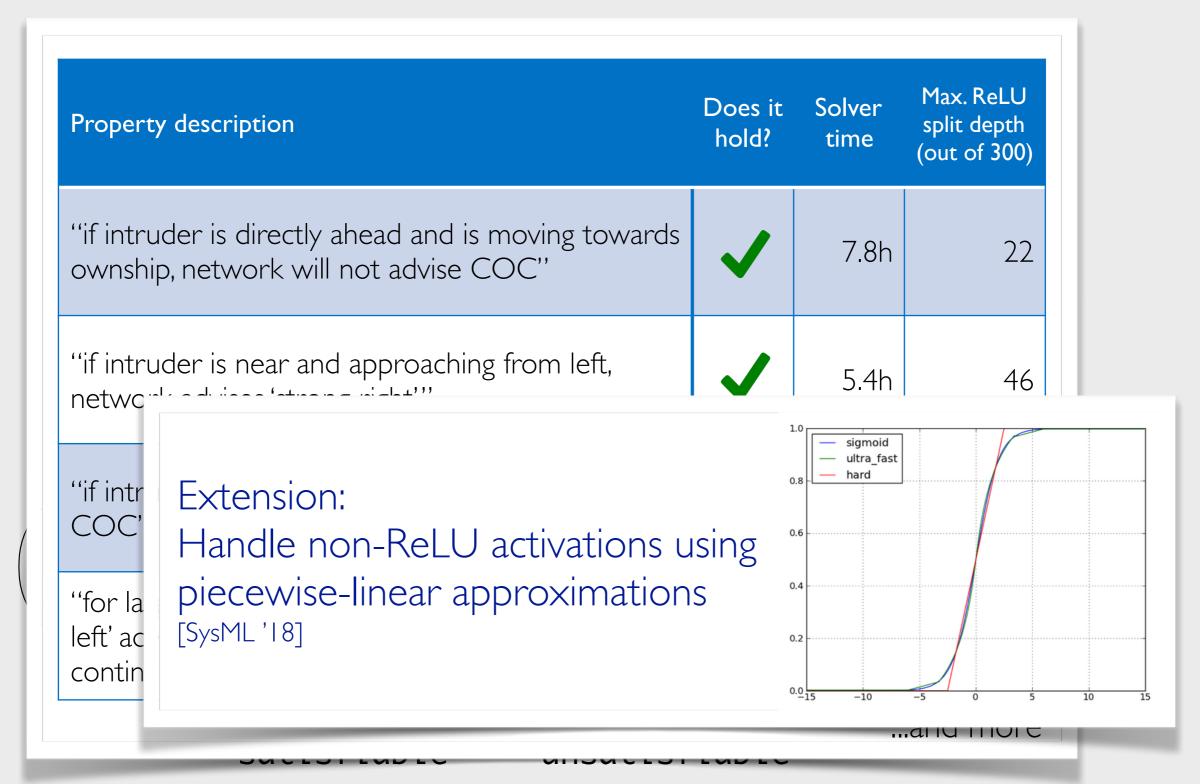








Does it hold?	Solver time	Max. ReLU split depth (out of 300)
✓	7.8h	22
/	5.4h	46
✓	50h	50
X	IIh	69
		hold? time 7.8h 5.4h 50h

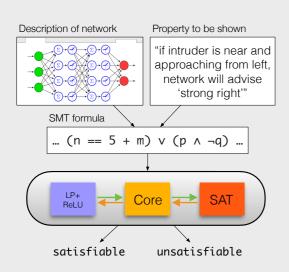








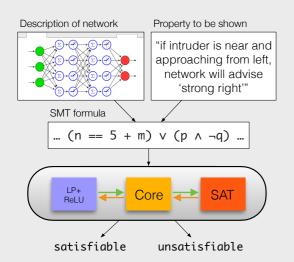




Develop new domain-specific theory solvers for parallel and distributed computing problems

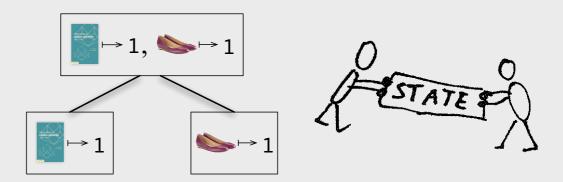






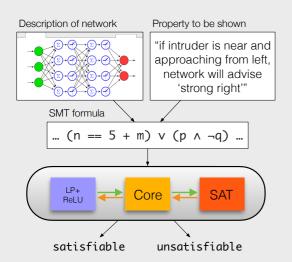
Develop new domain-specific theory solvers for parallel and distributed computing problems

Parallelize and distribute SMT solving with strong determinism guarantees



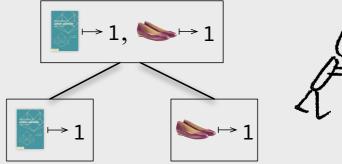






Develop new domain-specific theory solvers for parallel and distributed computing problems

Parallelize and distribute SMT solving with strong determinism guarantees







Long term: **Democratize solver hacking!**Create tools to make it *really easy* to build high-performance domain-specific solvers



Source: Olukotun et al., 2012

composition.al/CMPS290S-2018-09/

CMPS290S, Fall 2018

Home

Course Overview

Readings

Languages and Abstractions for Distributed Programming

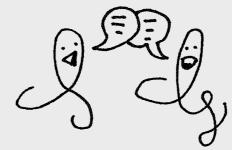
Welcome to CMPS290S, fall 2018 edition!

For more information, read the <u>first-day-of-class course overview</u>, then check out the <u>reading list</u>.

Blog posts

- Mixing Consistency in a Programmable Storage System
- Conflict resolution in collaborative text editing with operational transformation (Part 1 of 2)
- Manufacturing Consensus: An Overview of Distributed
 Consensus Implementations
- Time is Partial, or: why do distributed consistency models and weak memory models look so similar, anyway?
- Implementing a Garbage-Collected Graph CRDT (Part 1 of 2)
- Welcome to the "Languages and Abstractions for Distributed Programming" blog

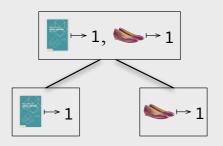
Thank you!



Email: lkuper@ucsc.edu

Papers, etc.: users.soe.ucsc.edu/~lkuper/

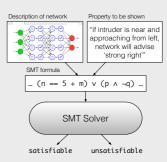
Research blog: composition.al



Lattice-based data structures (LVars) for deterministic programming [POPL'14, PLDI'14, FHPC'13, WoDet'14]



Non-invasive DSLs for productive parallelism [ECOOP'17]



SMT-based verification of safety-critical neural networks
[SysML'18]



Guiding principle: Find the right **high-level abstractions** to enable **efficient** computation

